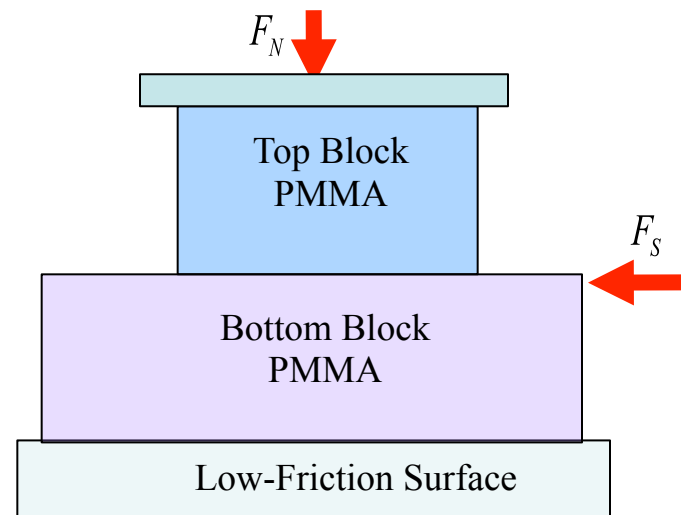


The Onset of Frictional Motion: “Fracture” or “Friction”

Oded Ben-David and Jay Fineberg

*The Racah Institute of Physics
The Hebrew University of Jerusalem*

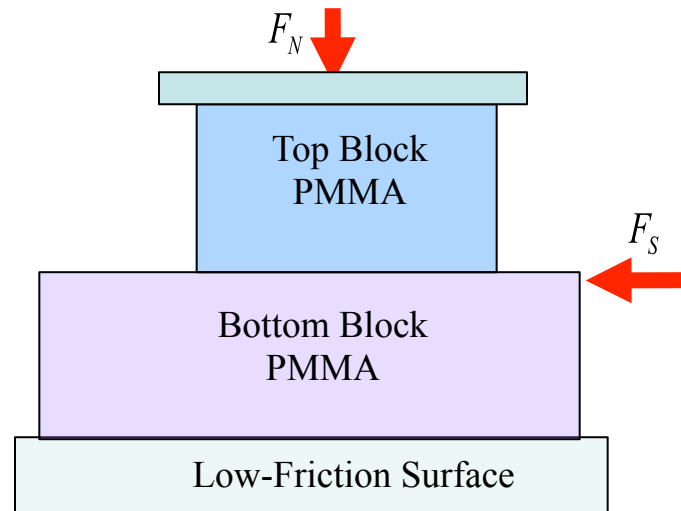


O. Ben-David, G. Cohen, J.F., *Science* **330**, 211 (2010).

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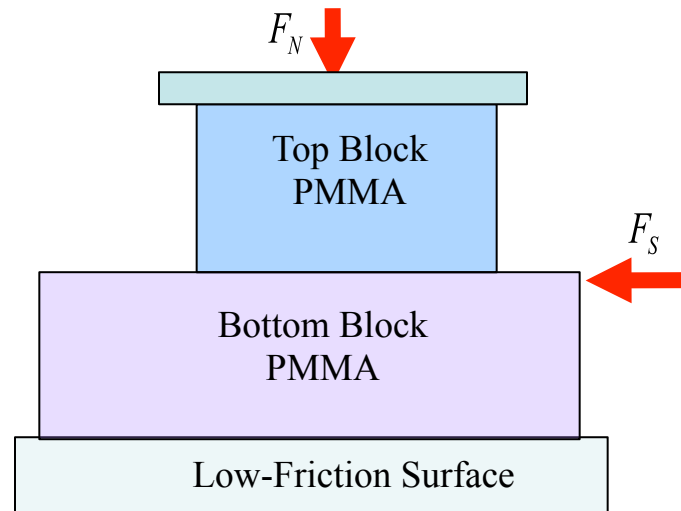


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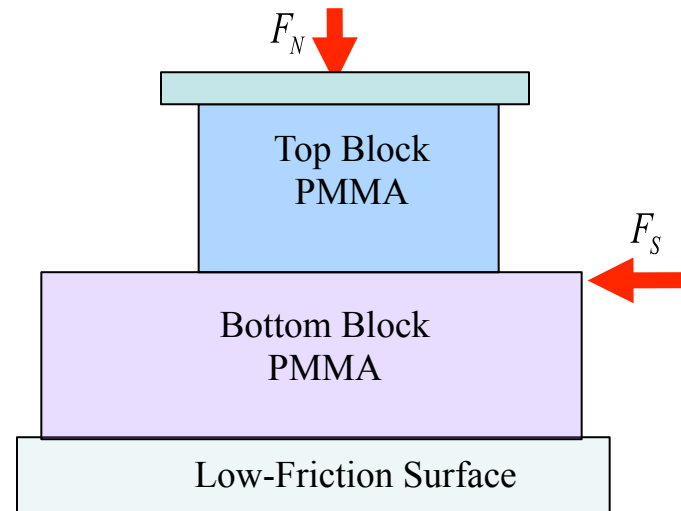
“*Insignificant*” details of loading → *Highly nonuniform* stress distributions

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“*Insignificant*” details of loading → *Highly nonuniform* stress distributions

These dictate:

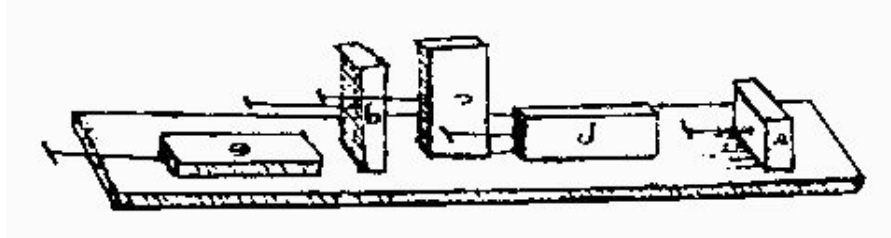
- The *rupture mode* that mediates slip onset
- The *value* of the static “*friction coefficient*”

O. Ben-David, G. Cohen, J.F., *Science* **330**, 211 (2010).

The *Classical* View of Friction



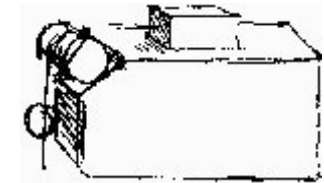
Leonardo Da Vinci (1452-1519)



1. The areas in contact have no effect on friction.
 - If the load of an object is doubled, its friction will also be doubled.
→ $F_S \propto F_N$



Guillaume Amontons (1663-1705)
Charles August Coulomb (1736-1806)



→ “Static” and “Dynamic” friction:

$$F_S = \mu_S F_N (v = 0)$$

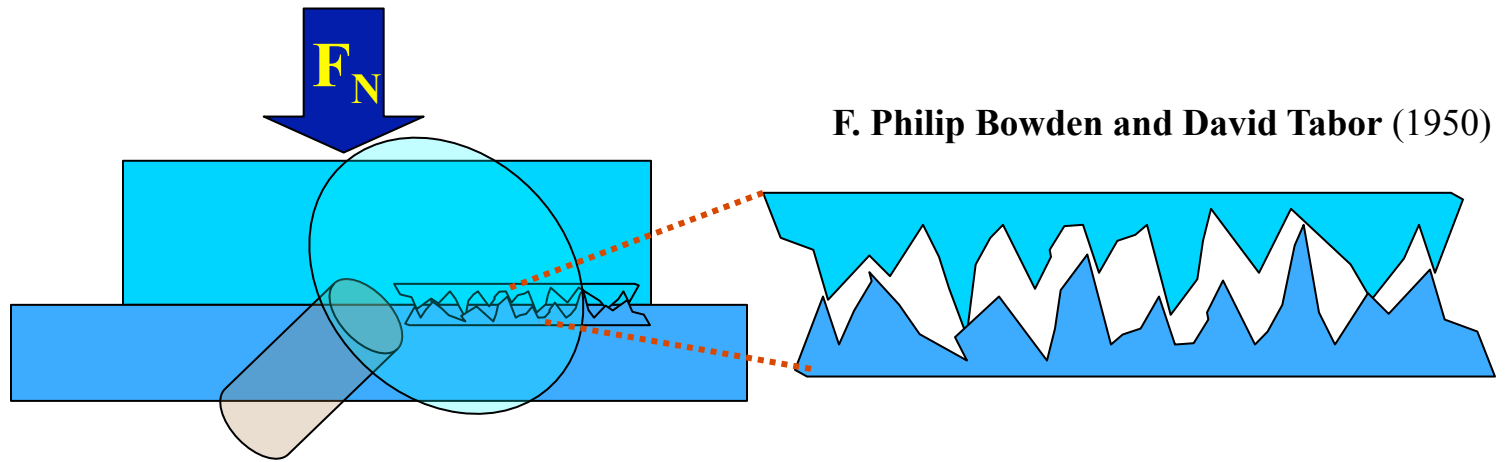
$$F_S = \mu_D F_N (v > 0)$$

μ - Friction Coefficient

The *Classic* View of Friction: $F_S = \mu_S F_N$

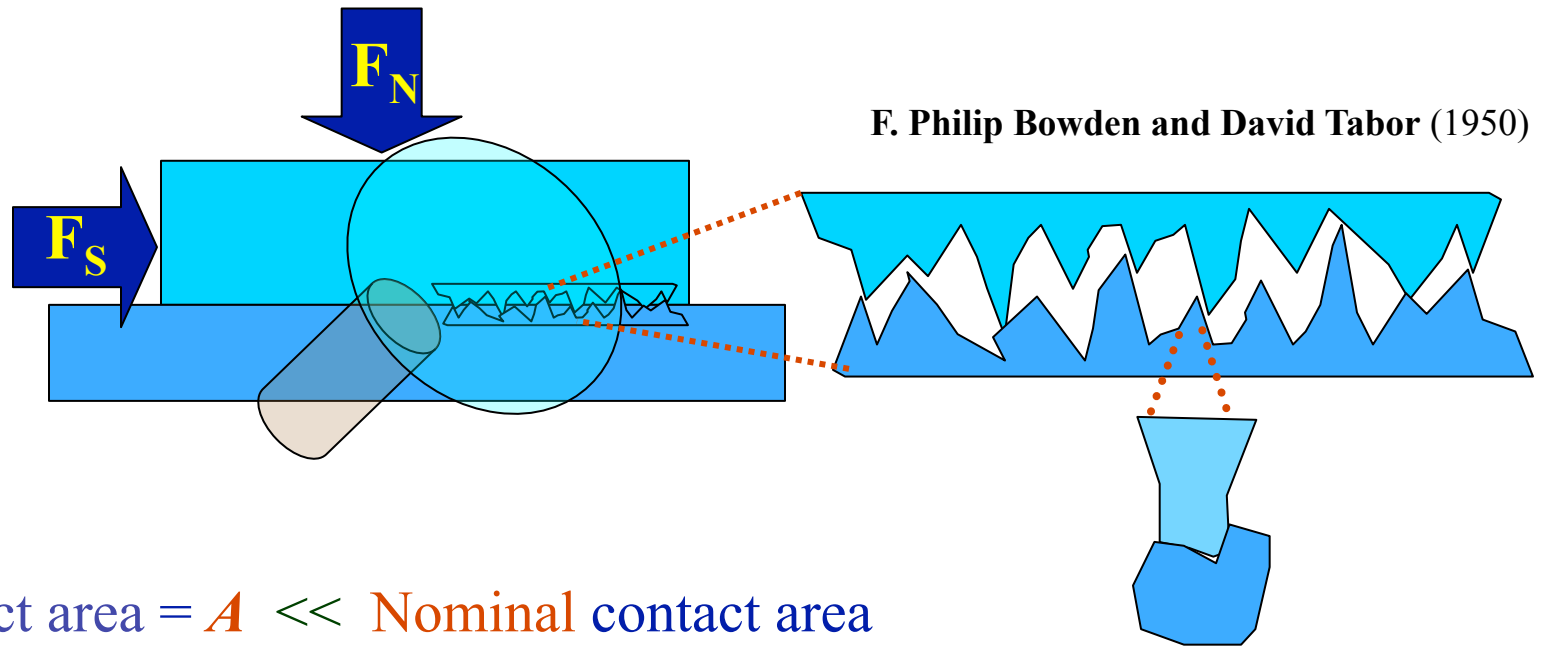
F. Philip Bowden and David Tabor (1950)

The *Classic* View of Friction: $F_S = \mu_S F_N$



- Net contact area = $A \ll$ Nominal contact area

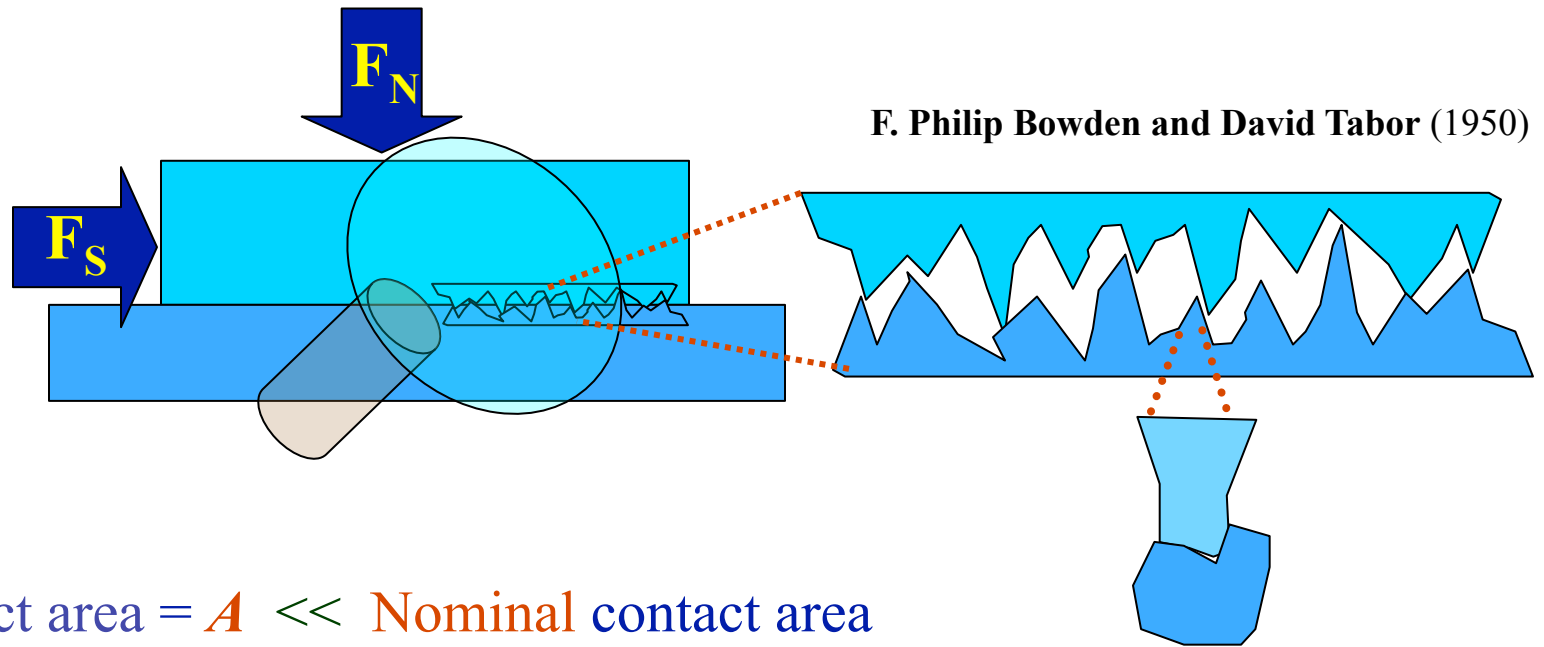
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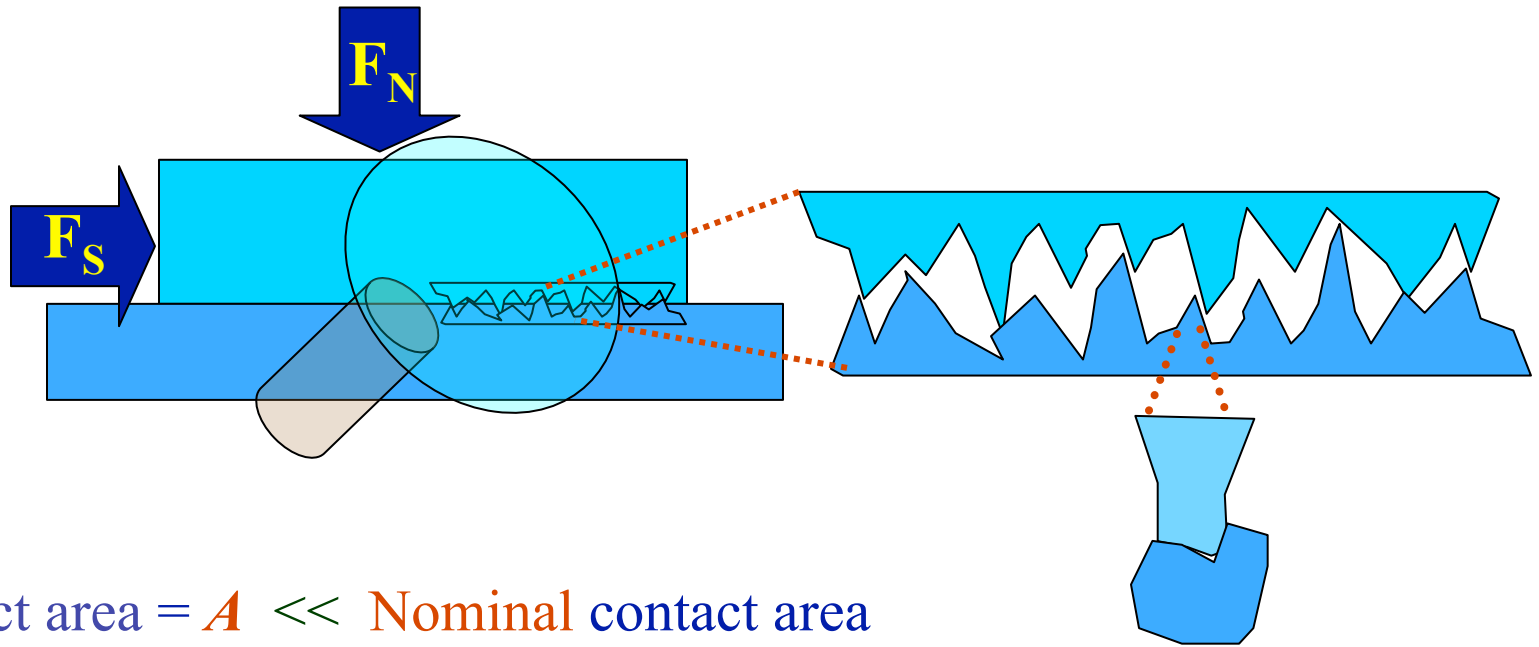
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- Net contact area = $A \ll$ Nominal contact area
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- Slip: *Instantaneous* Fracture of contacts when $F_S = \text{Shear strength} \cdot \text{Area} = \tau_S \cdot A$

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- Slip: *Instantaneous* Fracture of contacts when $F_S = \text{Shear strength} \cdot \text{Area} = \tau_S \cdot A$

- A and τ_S govern the **local** contact strength of a rough interface!
- Note: *Both* A and τ_S may vary *spatially* and *dynamically*

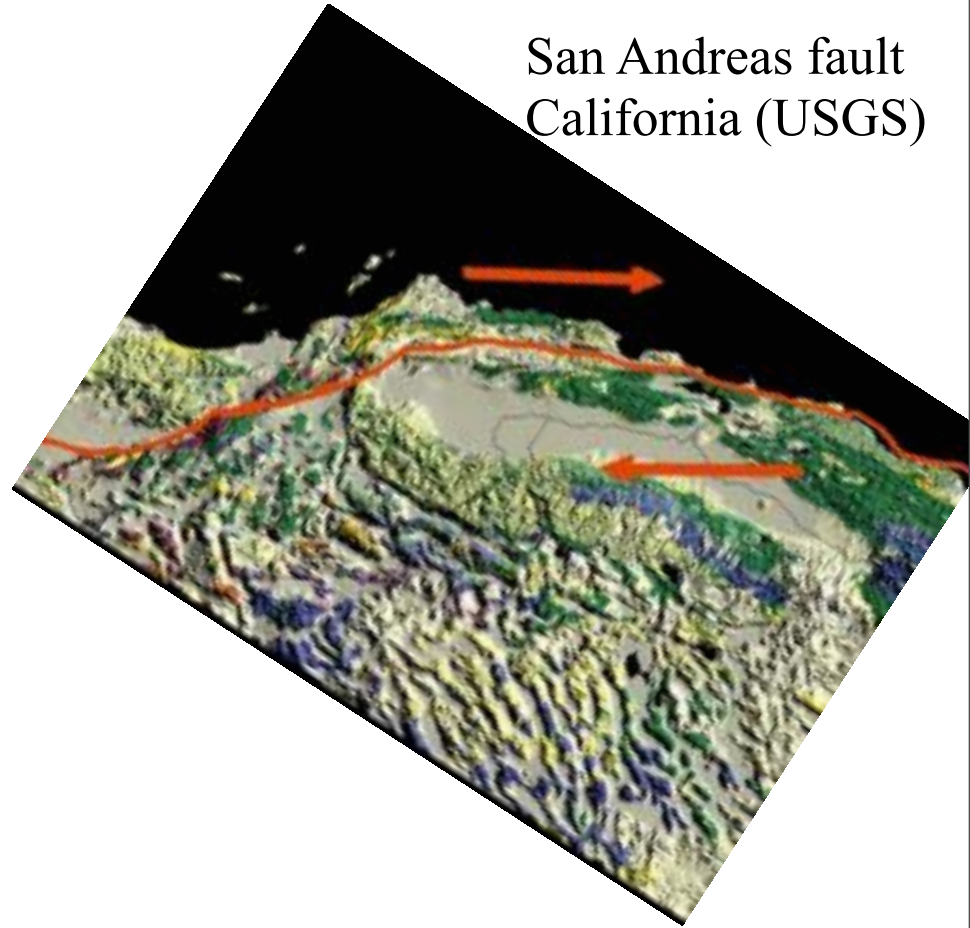
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S. M. Rubinstein, G. Cohen, and J. F., Phys. Rev. Lett. 98, 226103 (2007)

Ben-David, Rubinstein and Fineberg, *Nature* 463, 76 (2010)

Earthquakes *are* Friction

San Andreas fault
California (USGS)



Earthquakes *are* Friction

but: Earthquakes are mediated by (*rapid*) **fracture fronts**

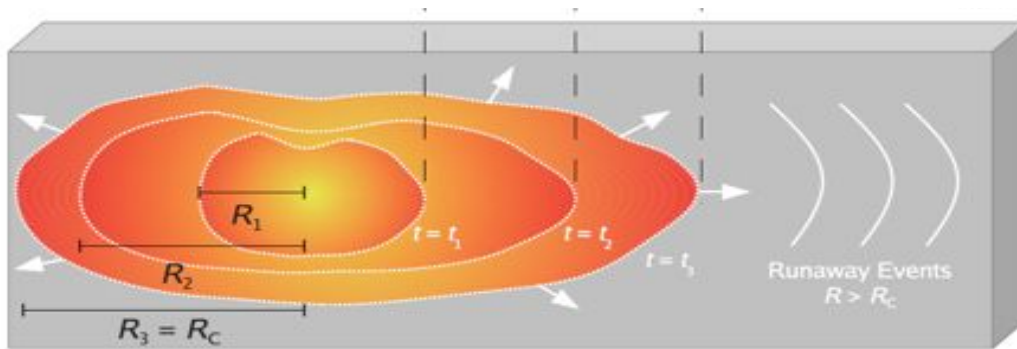
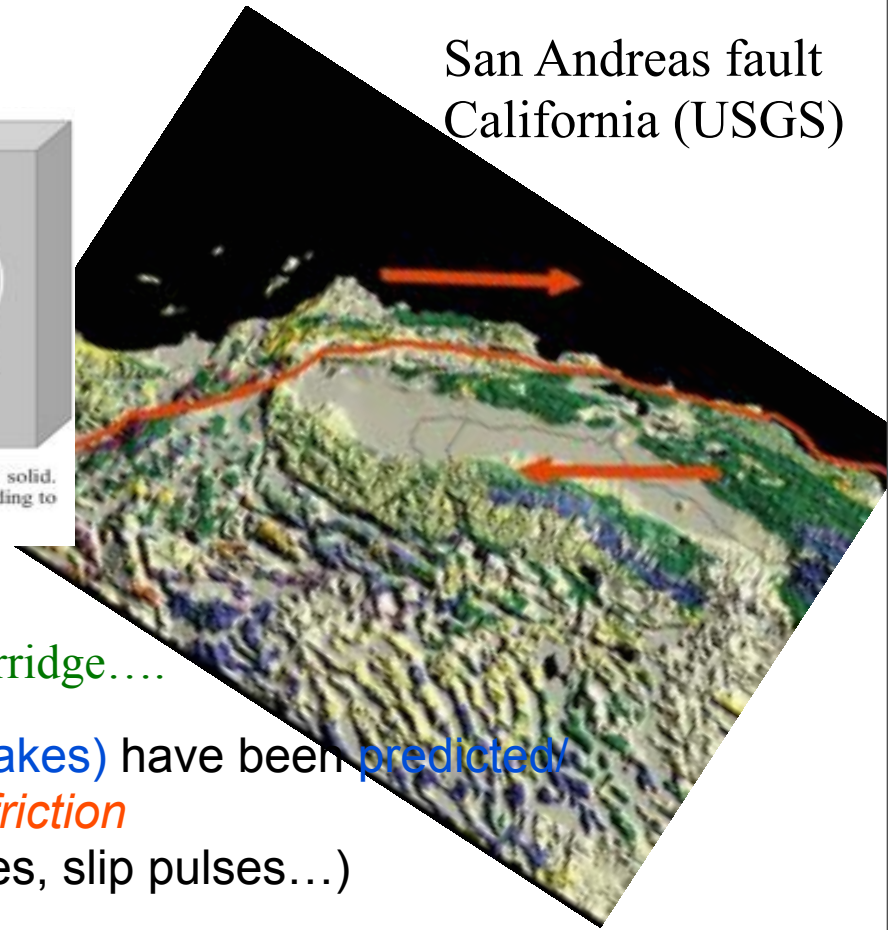


Figure 13. (top) Stress versus distance from the edge of (bottom) ruptures growing in elastic solid. Ruptures with a critical size R_c produce dynamically stress comparable to the static friction τ_s , leading to runaway events.

Y. Benzon (2008)

San Andreas fault
California (USGS)



Kostrov, Eshelby, Freund, Rice, Aki, Andrews, Burridge....

A variety of **different rupture modes** (\Leftrightarrow earthquakes) have been **predicted/observed/deduced...** that **mediate the onset of friction** (e.g slow, sub-Rayleigh, Supershear earthquakes, slip pulses...)

- How can we make “sense” of these **different rupture modes**?
- Can these different rupture modes conspire to produce a

Earthquakes *are* Friction

but: Earthquakes are mediated by (*rapid*) **fracture fronts**

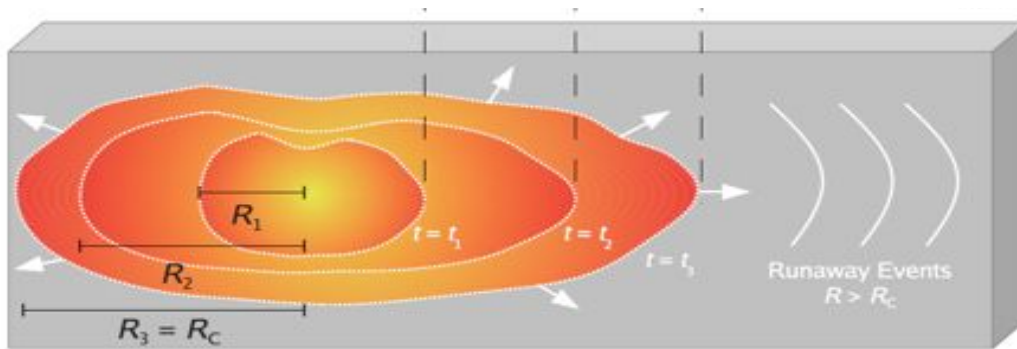
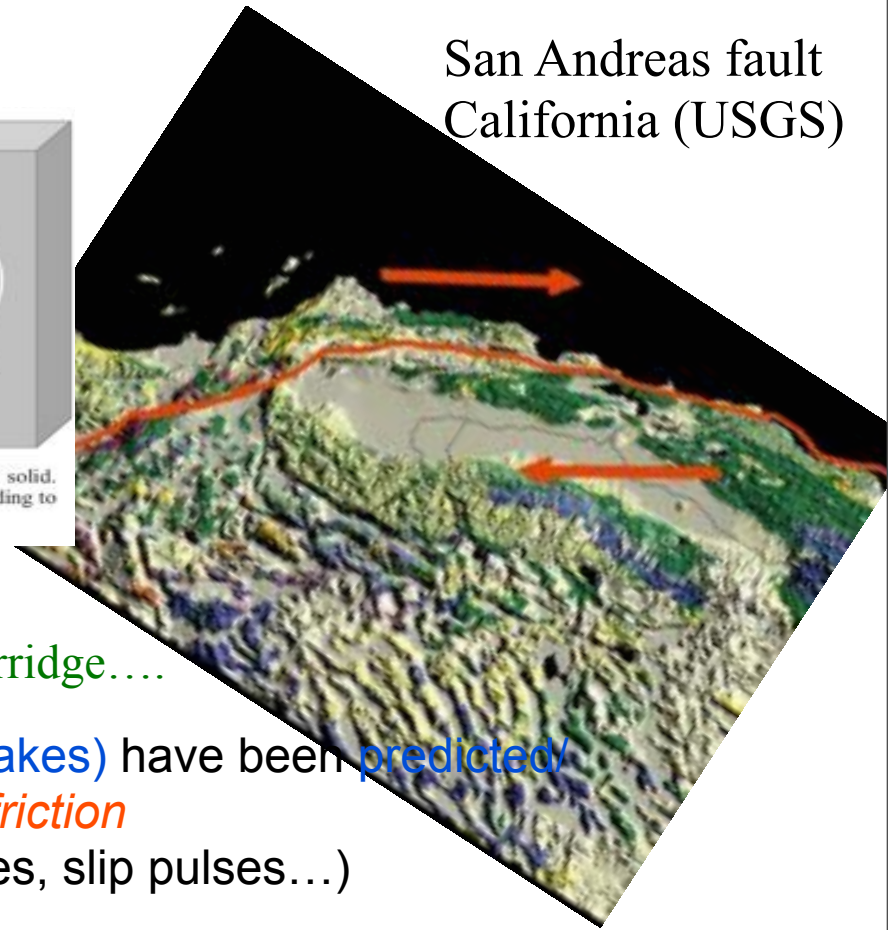


Figure 13. (top) Stress versus distance from the edge of (bottom) ruptures growing in elastic solid. Ruptures with a critical size R_c produce dynamically stress comparable to the static friction τ_s , leading to runaway events.

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- How can we make “sense” of these **different rupture modes**?
- Can these different rupture modes conspire to produce a **single “friction coefficient”???**
- ***Do they??***

A fracture primer:

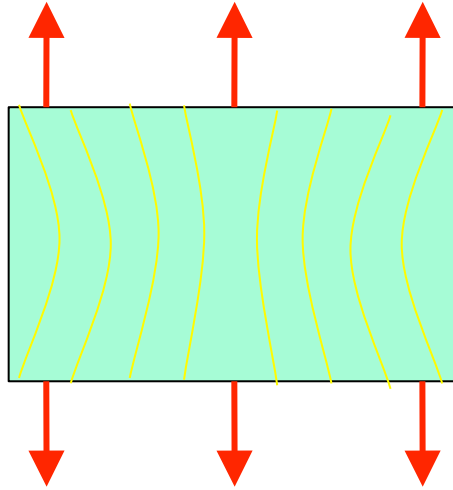
Griffith threshold for Fracture initiation

Released elastic energy $>$ Energy to create new surfaces (“Fracture Energy”)

A fracture primer:

Griffith threshold for Fracture initiation

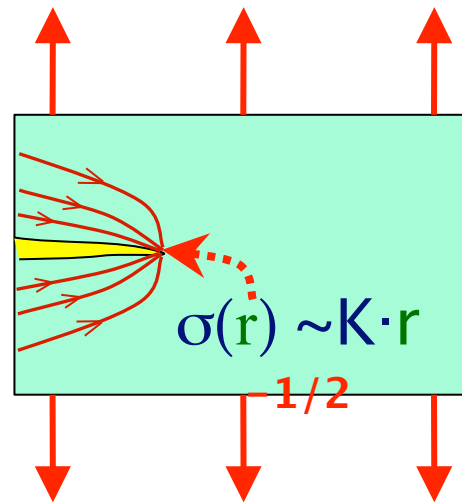
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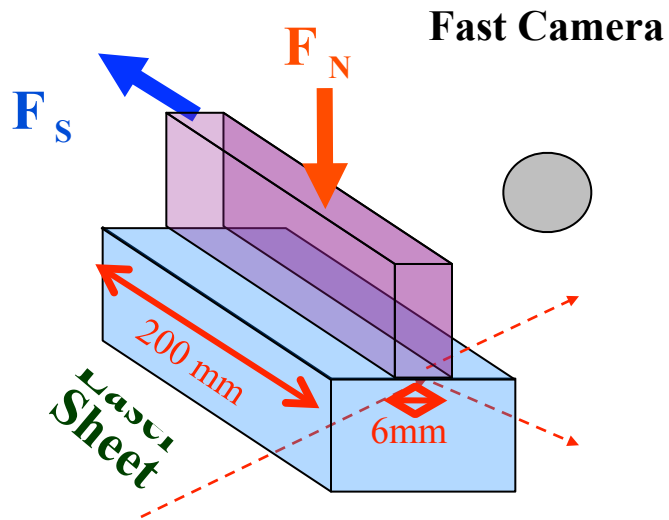
Released elastic energy $>$ Energy to create new surfaces (“Fracture Energy”)



A crack **focuses** elastic energy into a **stress field singularity** at its tip.

- Material is **preferentially ruptured** at the tip of a crack
- Failure: Loads \ll theoretical strength

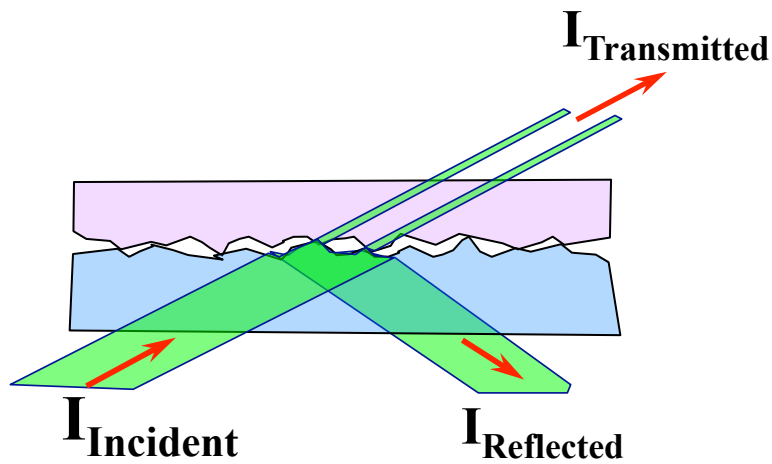
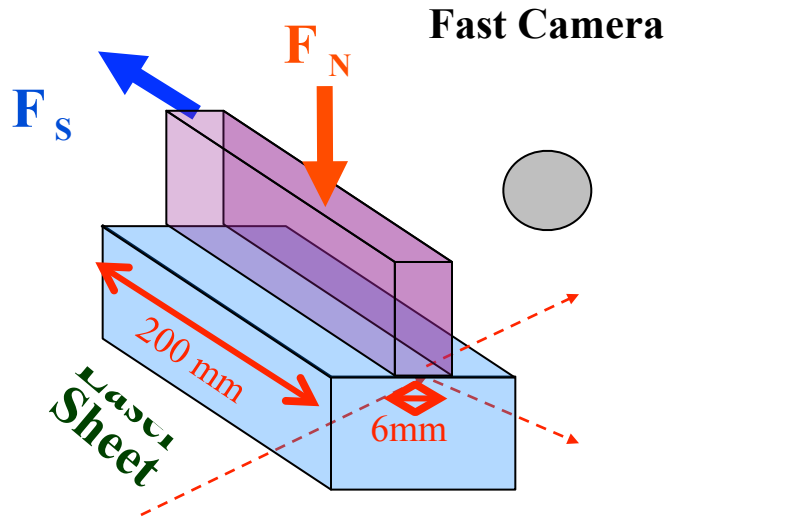
Real Contact area A measurements



S. M. Rubinstein, G. Cohen, and J. F., Nature 430, 1005-1009 (2004)

S. M. Rubinstein, G. Cohen, and J. F., Int. J. Fracture 140, 201-212 (2006)

Real Contact area A measurements



$$I_{\text{transmitted}} \propto A$$

Frame Rate \sim 250,000 Frames/sec

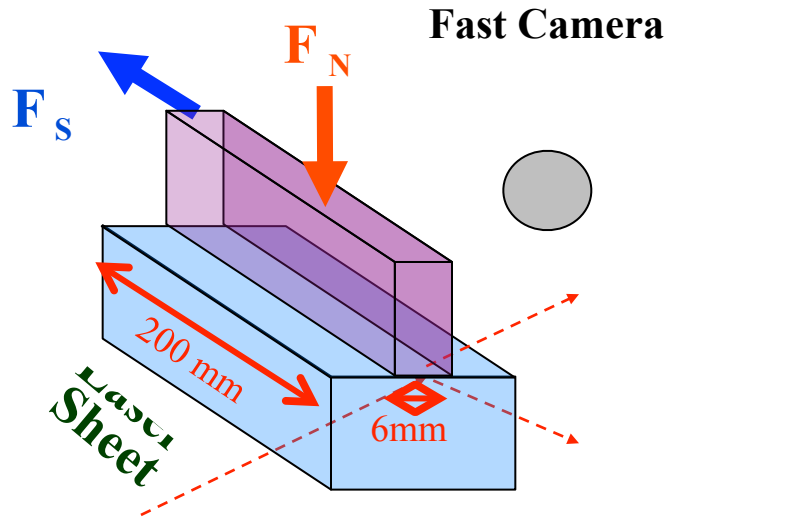
Resolution: 1280 Pixels / 200mm

$$A(x,t) = I(x,t) = \int I(x,y,t) dy$$

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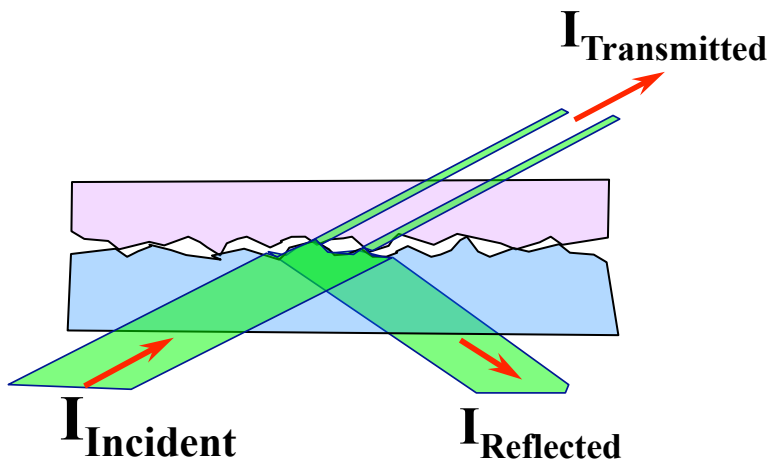
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Non-uniform stresses along the interface

Are introduced/controlled by:



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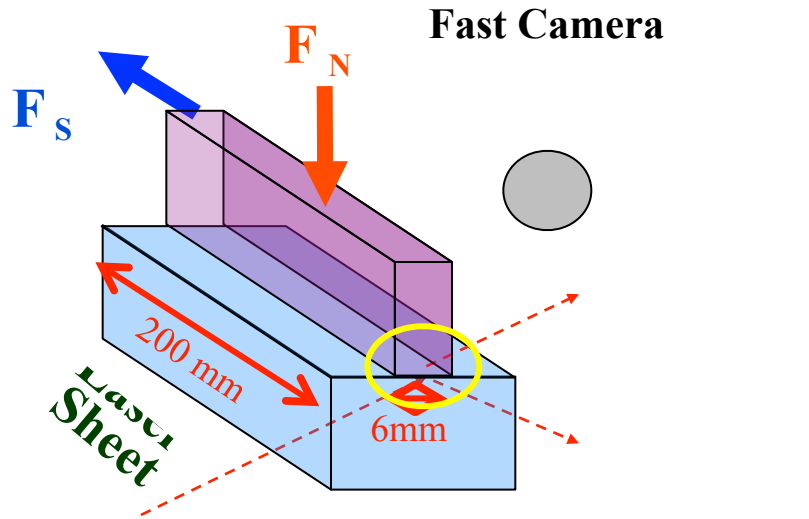
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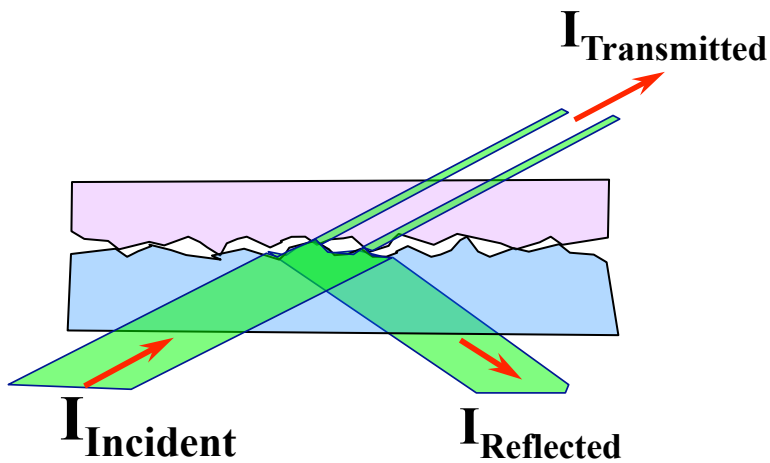
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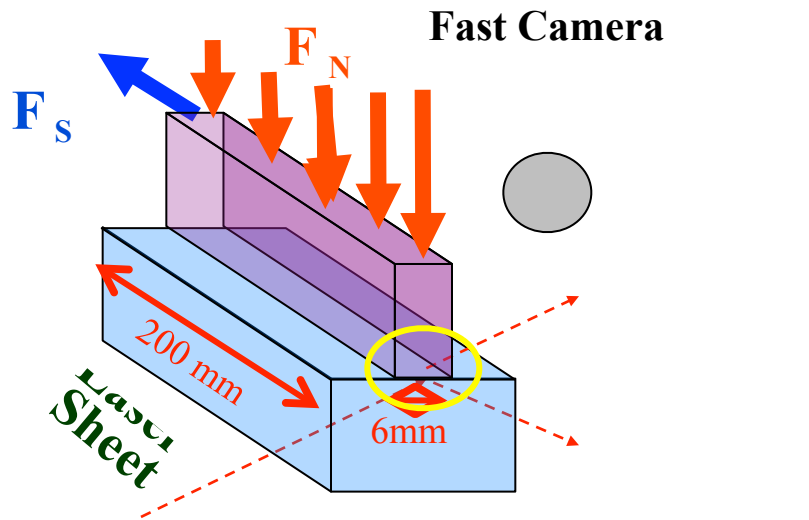
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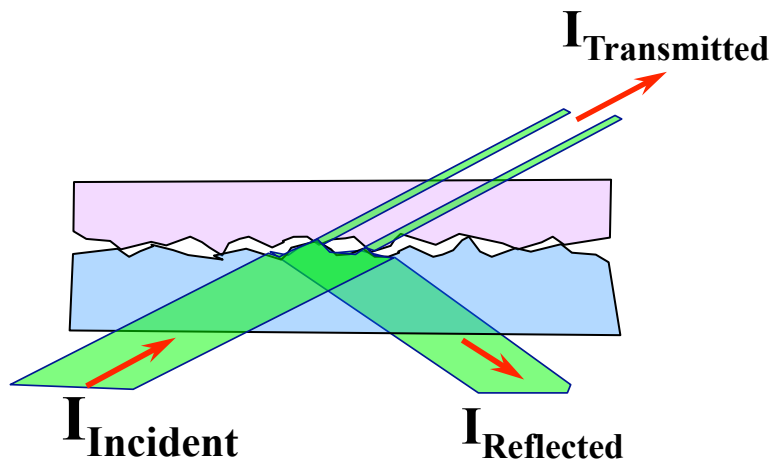
Real Contact area A measurements



Non-uniform stresses along the interface

Are introduced/controlled by:

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- Spatially inhomogeneous loads in F_N , F_S



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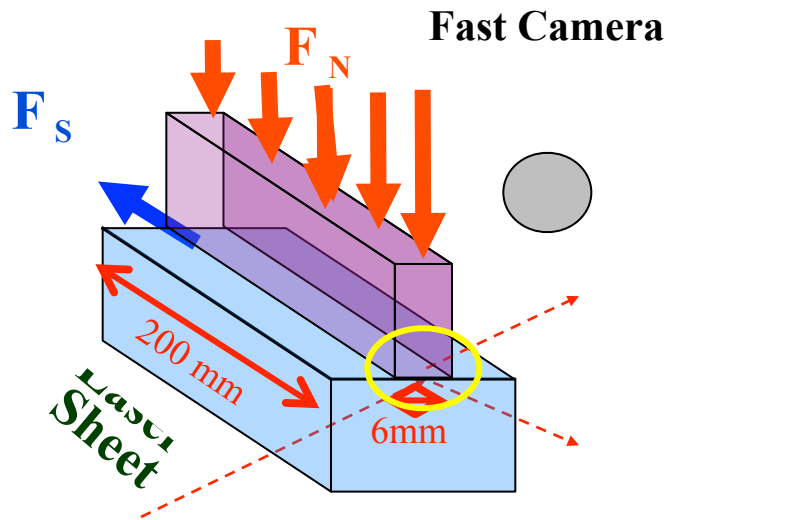
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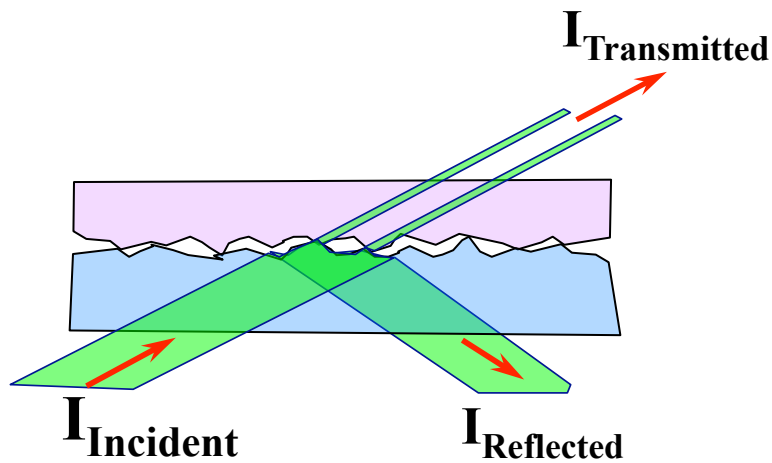
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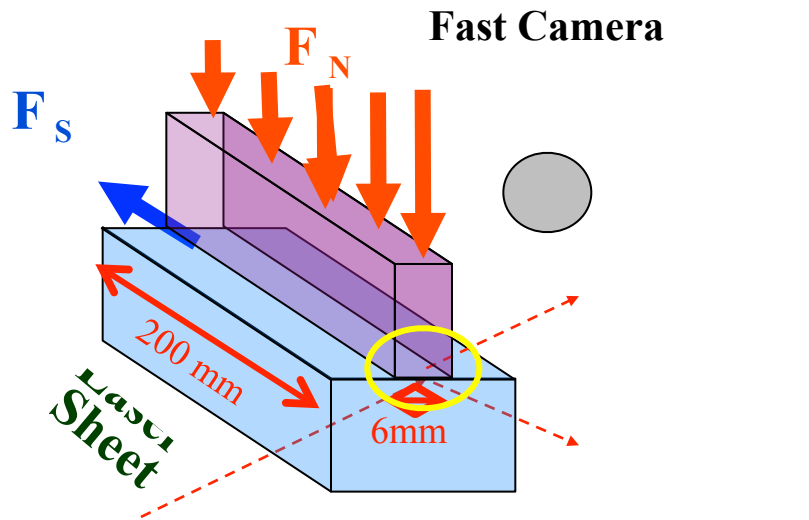
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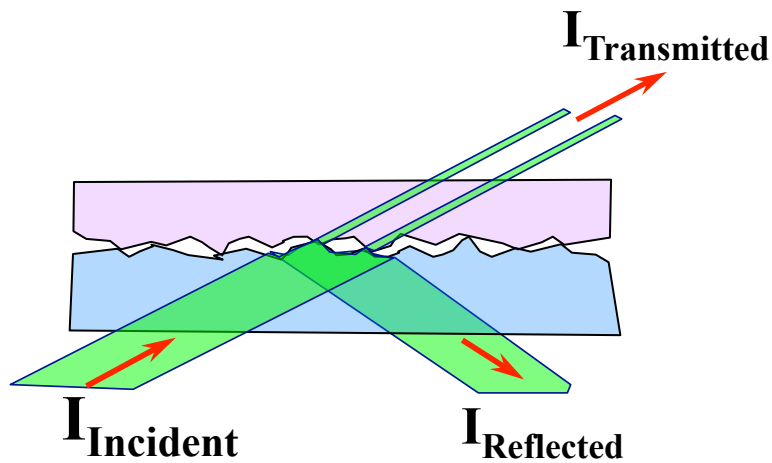
Real Contact area A measurements



Non-uniform stresses along the interface

Are introduced/controlled by:

- Block edges
- Spatially inhomogeneous loads in F_N , F_S
- **Dynamically**, by prior slip events



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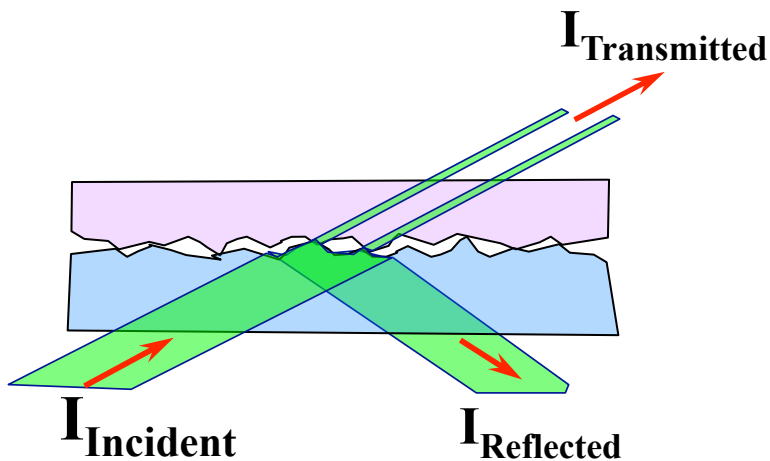
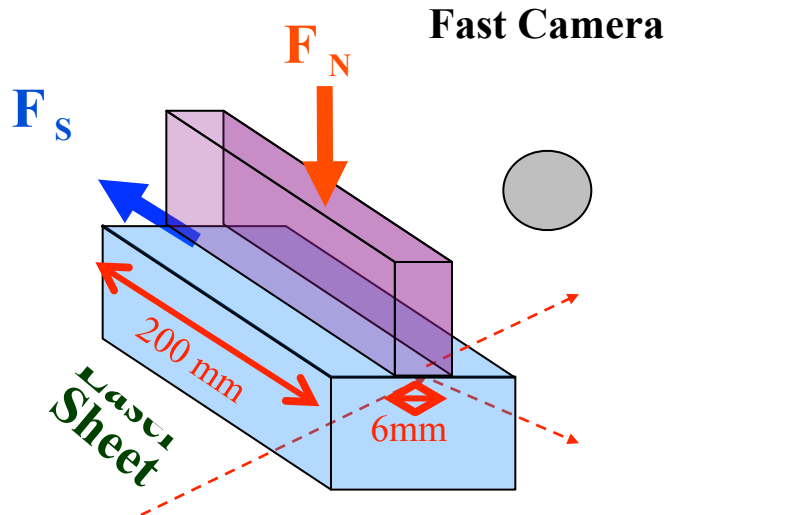
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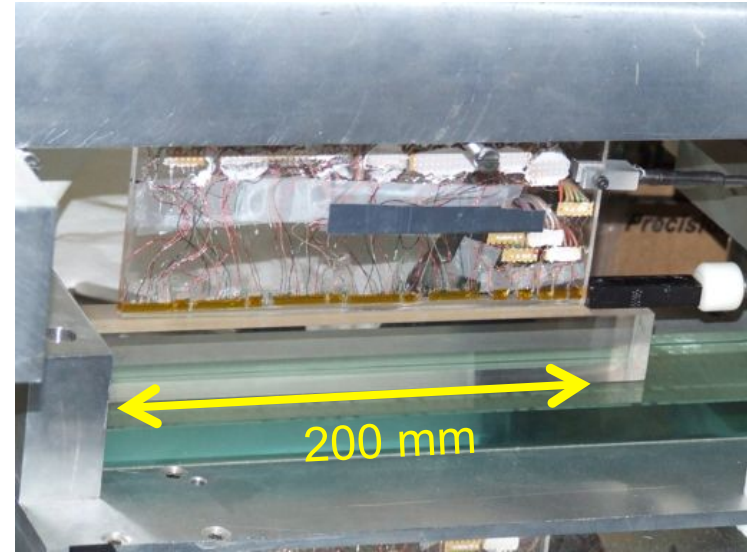


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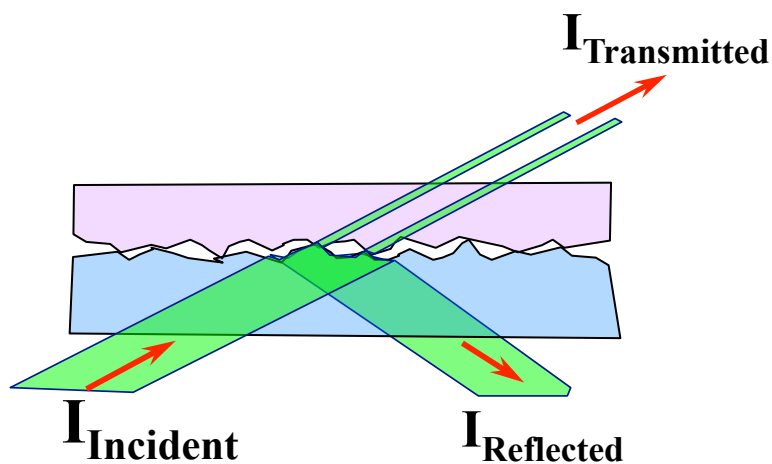
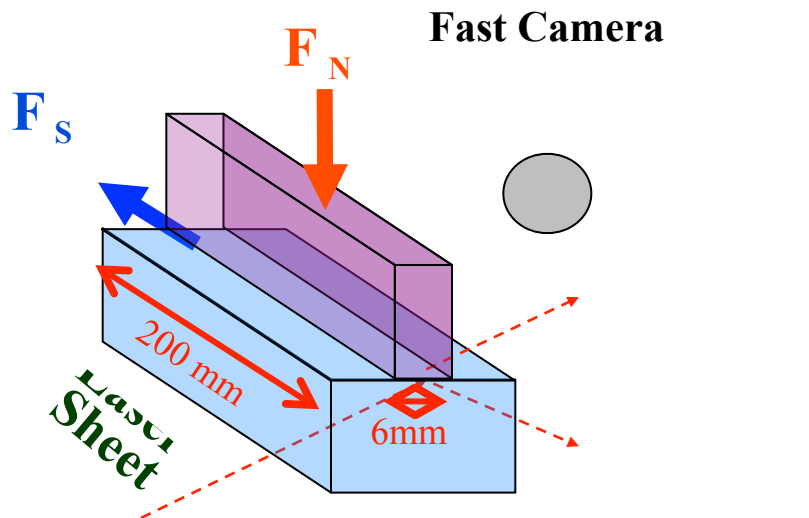
Stress measurements



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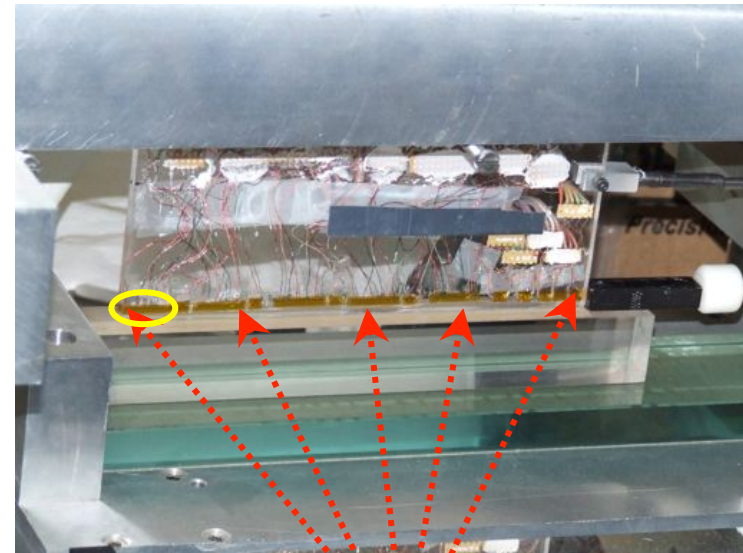


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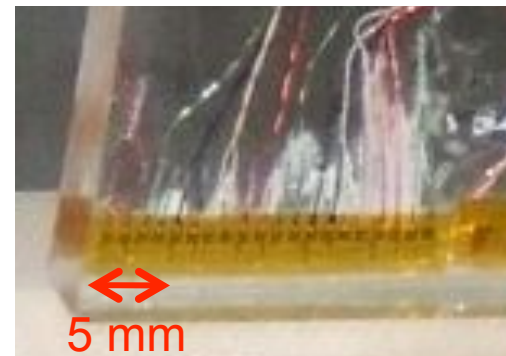
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Stress measurements



74 miniature strain gages

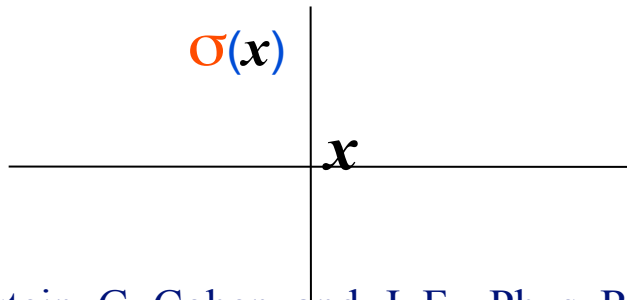
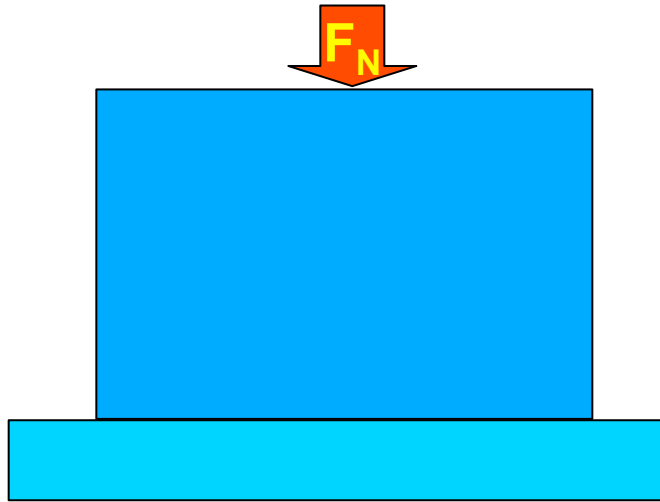


All strain gages monitored continuously at \sim 2Hz

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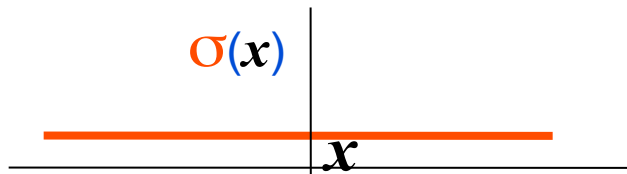
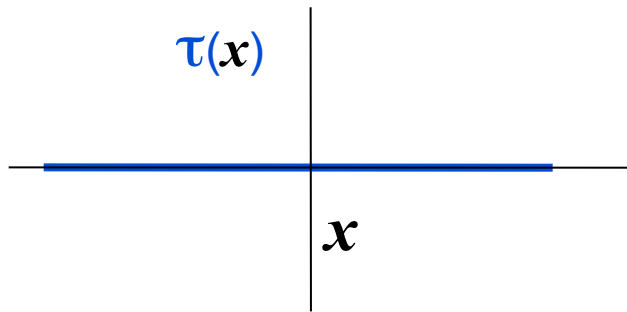
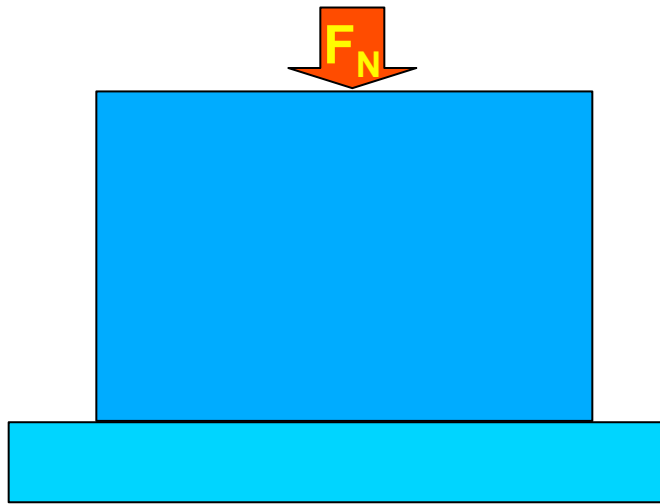
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Non-uniform stress profiles are formed naturally - *prior to motion*



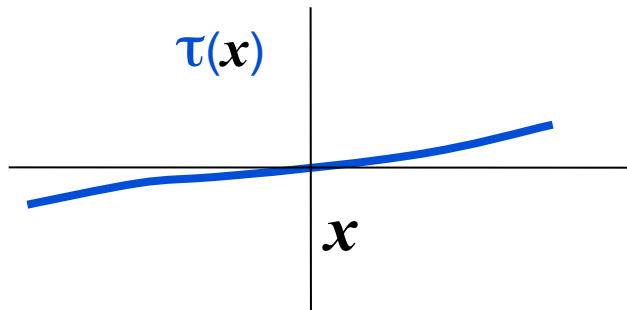
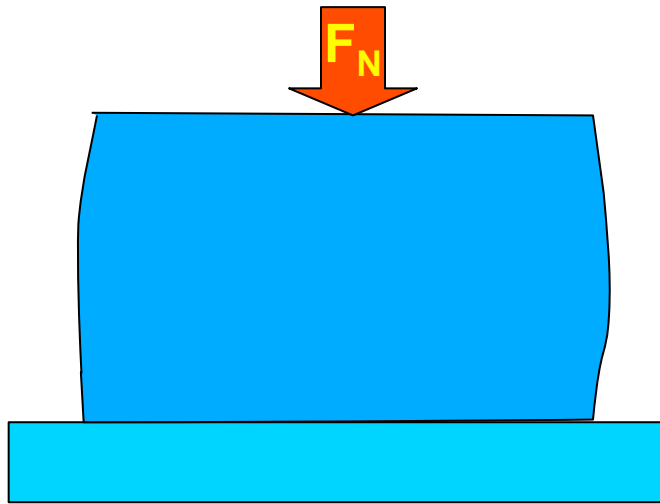
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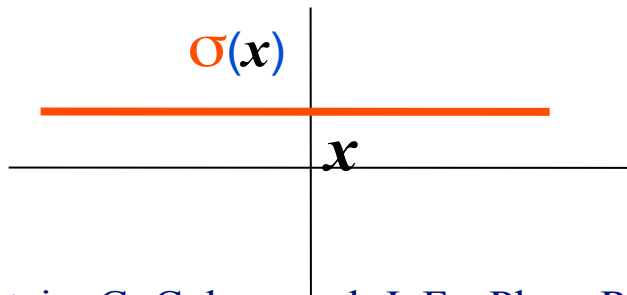


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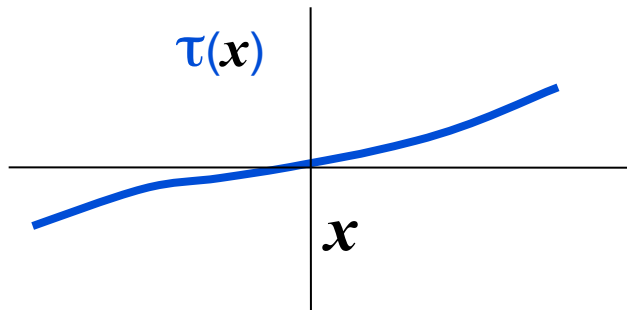
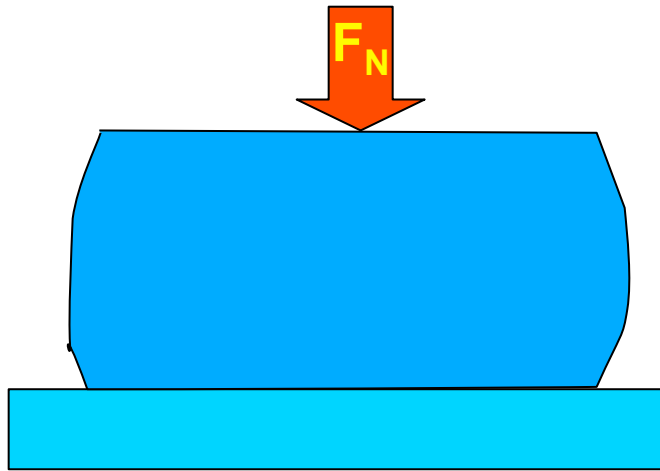


Uniform loading + friction
Frustrated Poisson expansion:
→ *Non-uniform* shear stress, $\tau(x)$
+ uniform normal stress, $\sigma(x)$

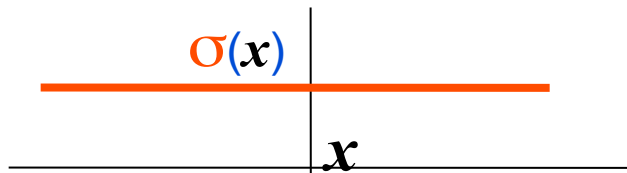


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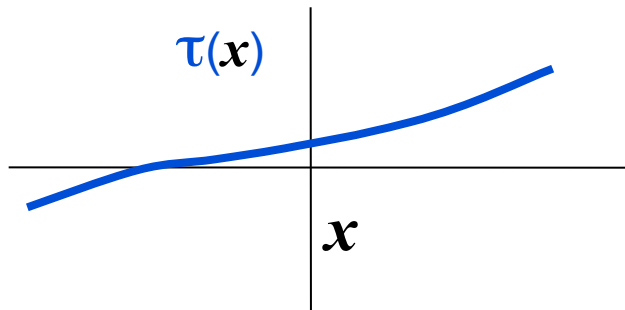
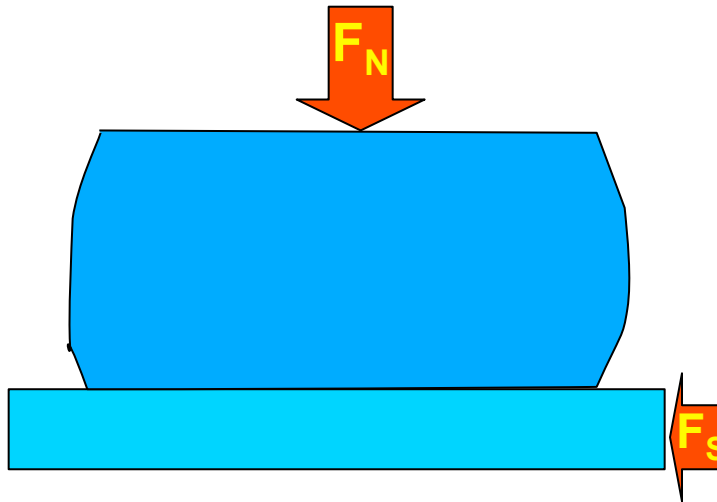


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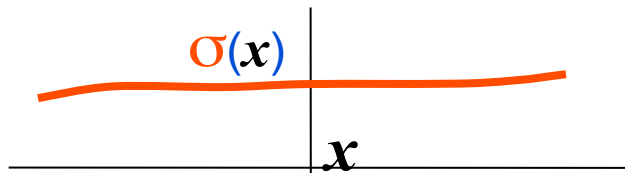


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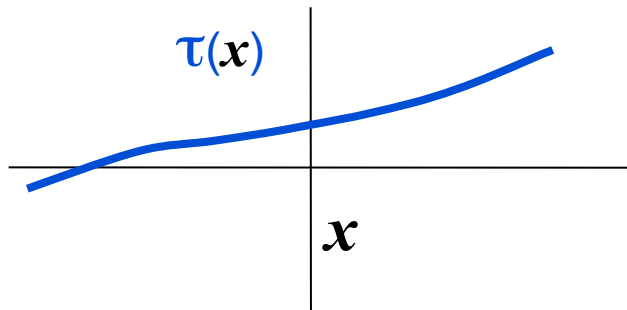
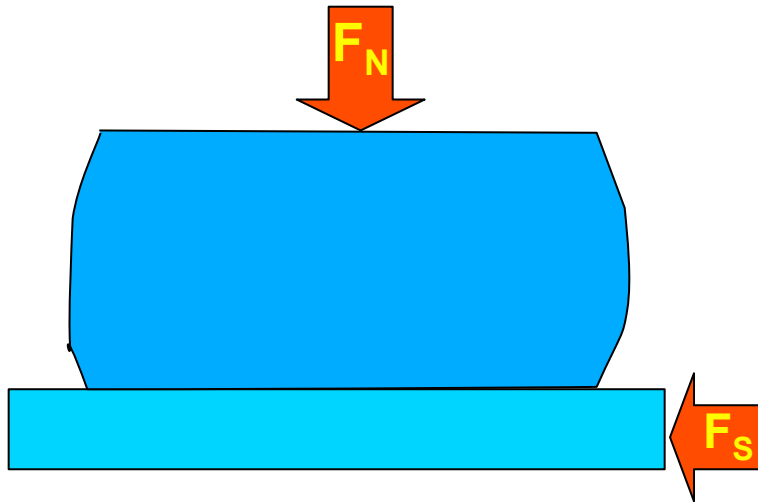
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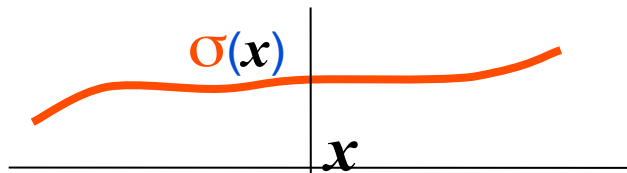
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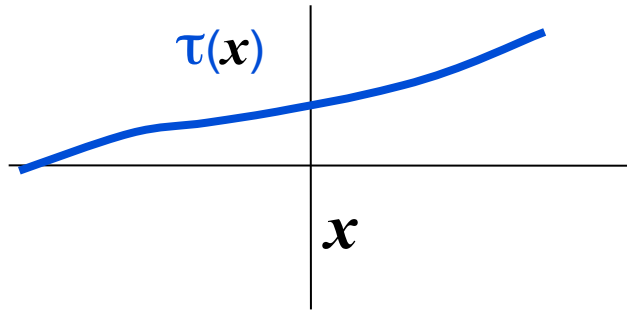
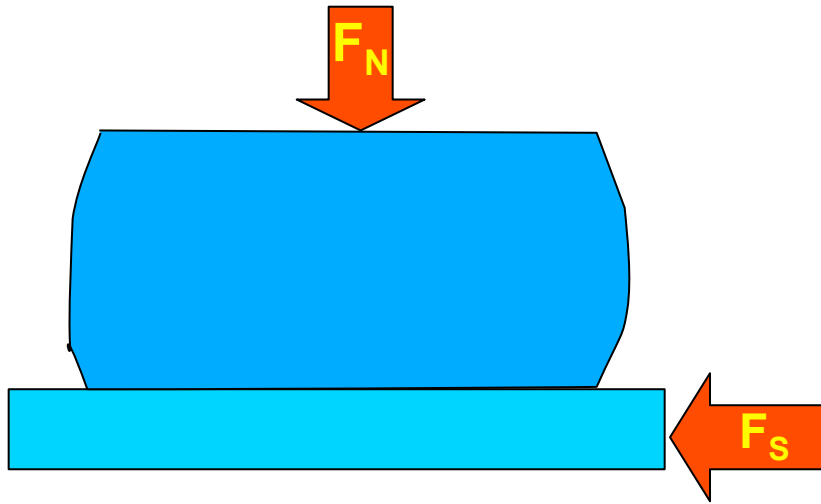
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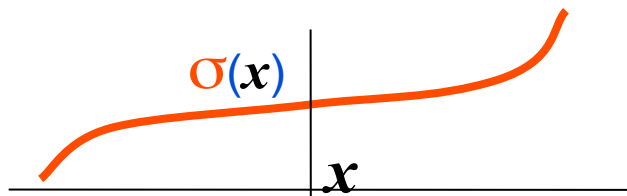
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S. M. Rubinstein, G. Cohen, and J. F., Phys. Rev. Lett. 96, 256103 (2006)

Non-uniform stress profiles are formed naturally - *prior to motion*



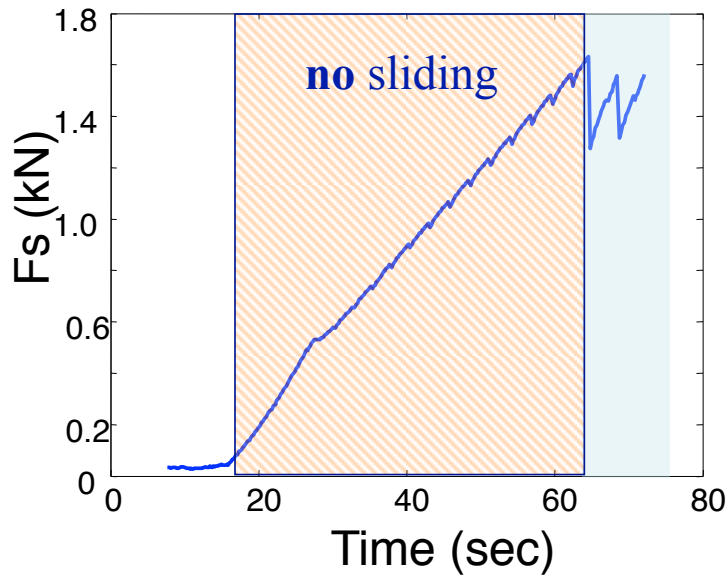
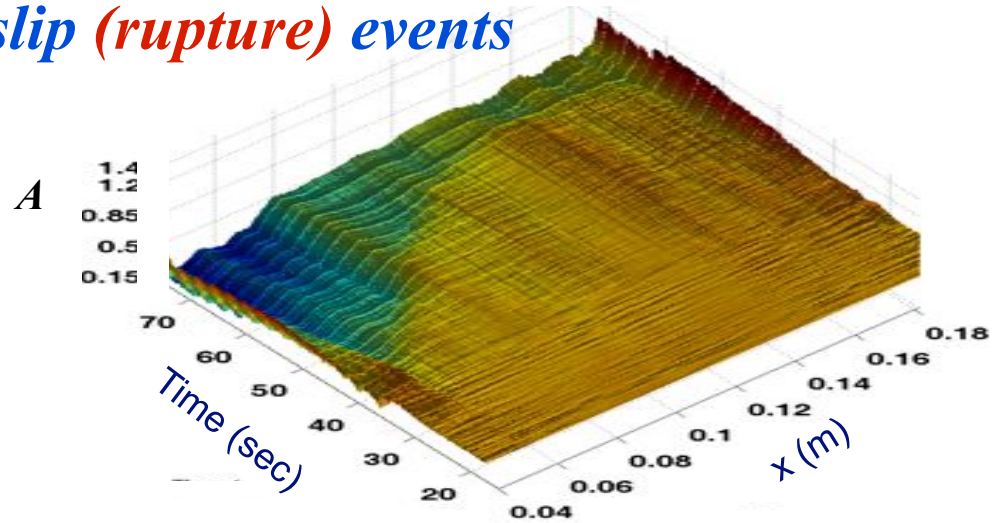
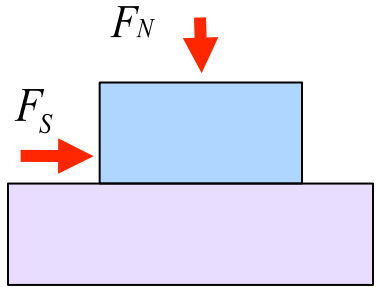
Uniform loading + friction
Frustrated Poisson expansion:
→ *Non-uniform* shear stress, $\tau(x)$
+ uniform normal stress, $\sigma(x)$



Torque due to applied shear, F_S :
→ *Uniformly* increased $\tau(x)$
+ *non-uniform* $\sigma(x)$

S. M. Rubinstein, G. Cohen, and J. F., Phys. Rev. Lett. 96, 256103 (2006)

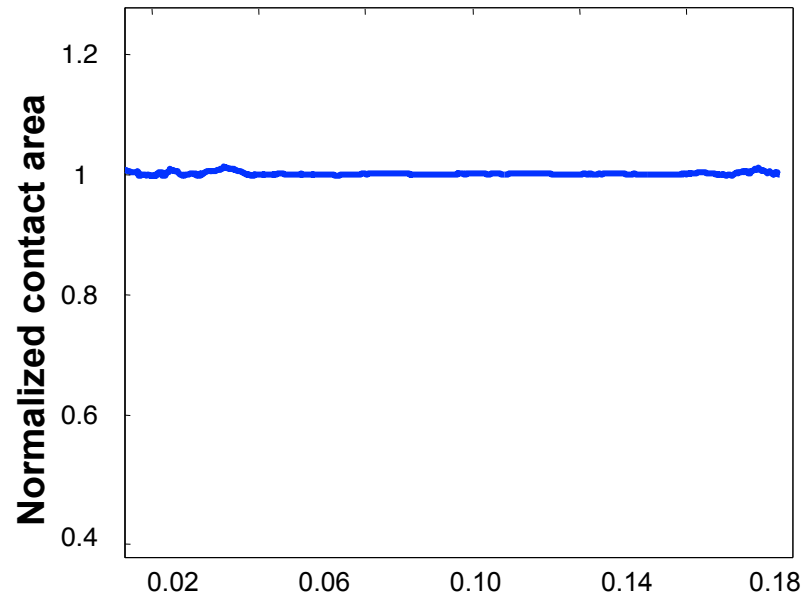
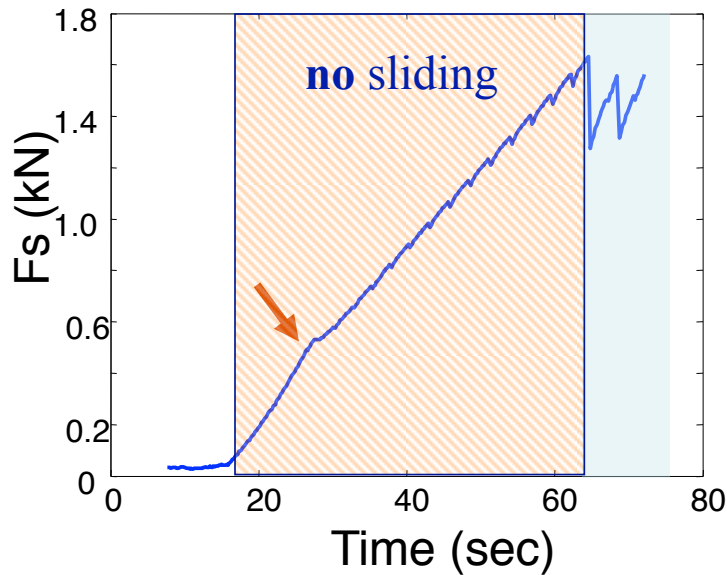
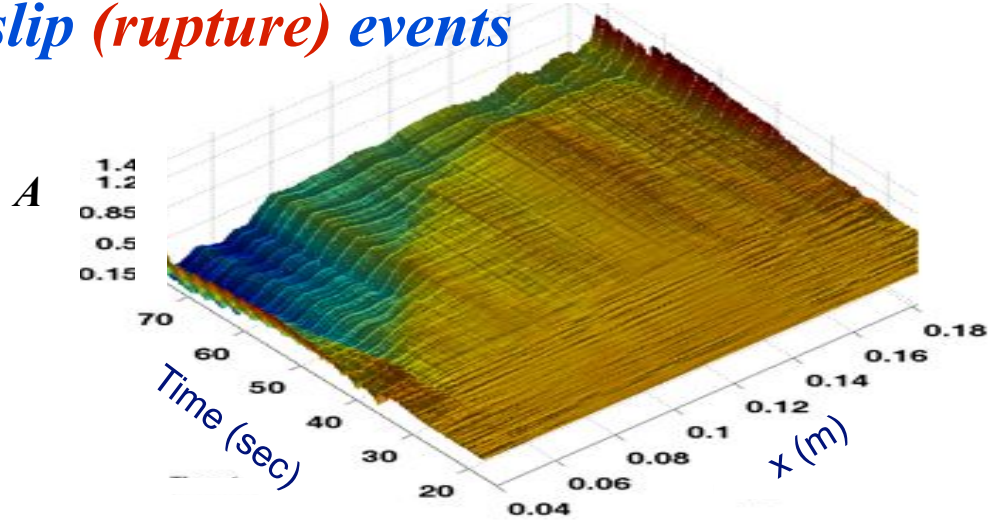
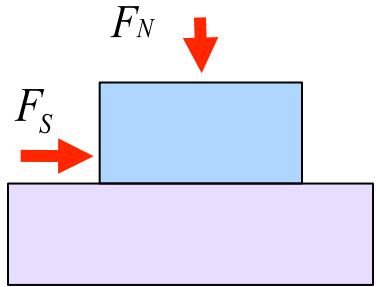
The **contact-area/stress distribution** can also change *dynamically* via *arrested precursory slip (rupture) events*



S. M. Rubinstein, G. Cohen, and J. F., Phys. Rev. Lett. 98, 226103 (2007)

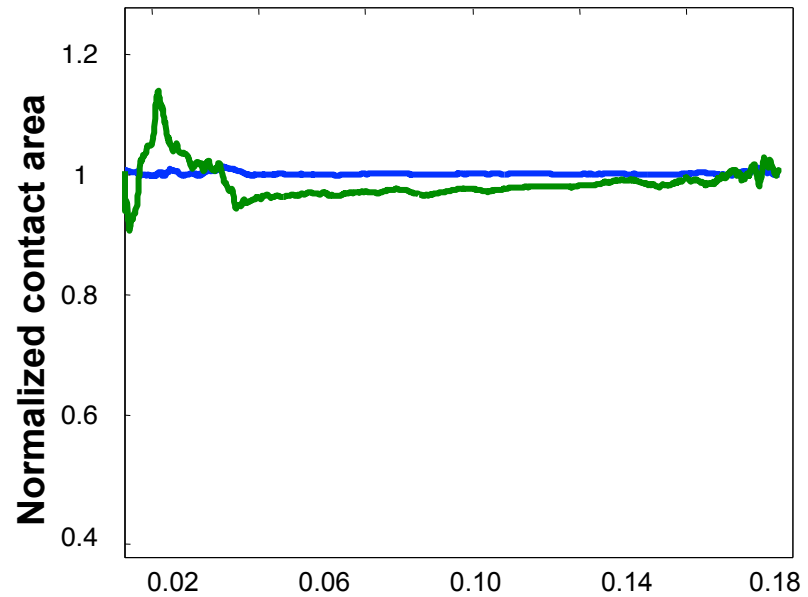
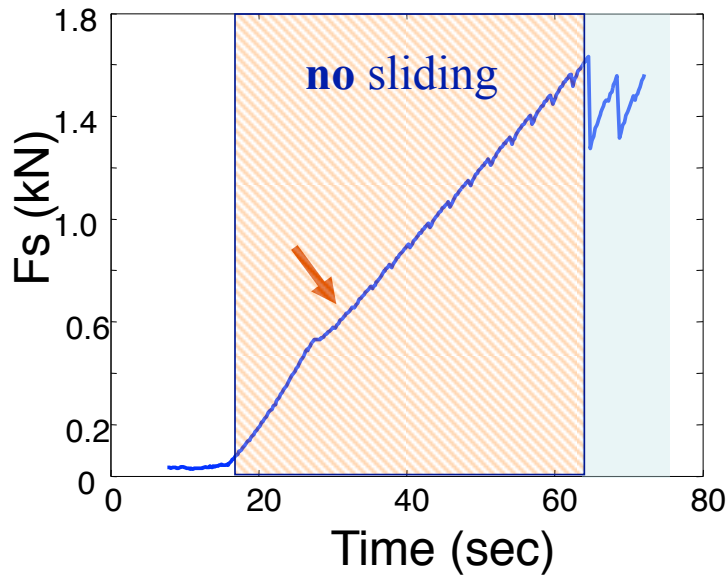
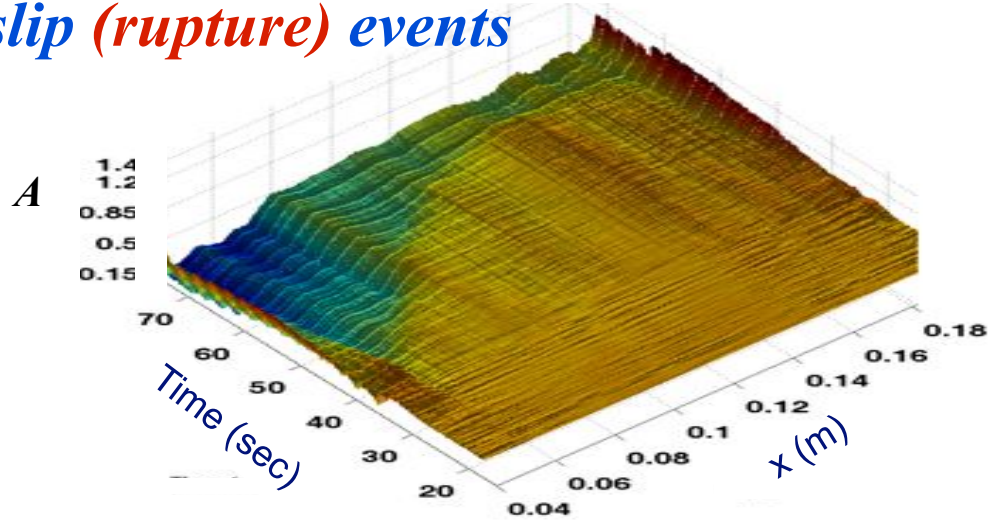
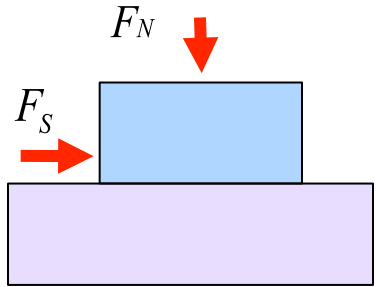
Monday, November 1, 2010

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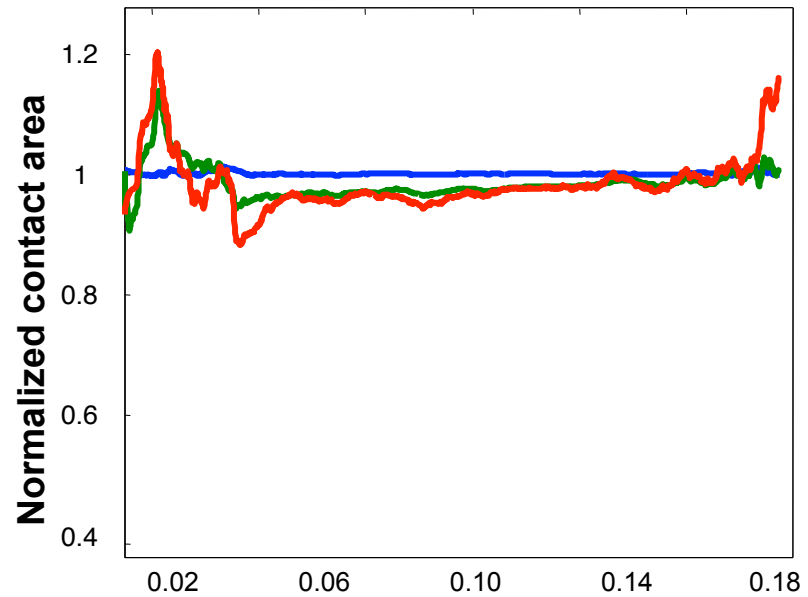
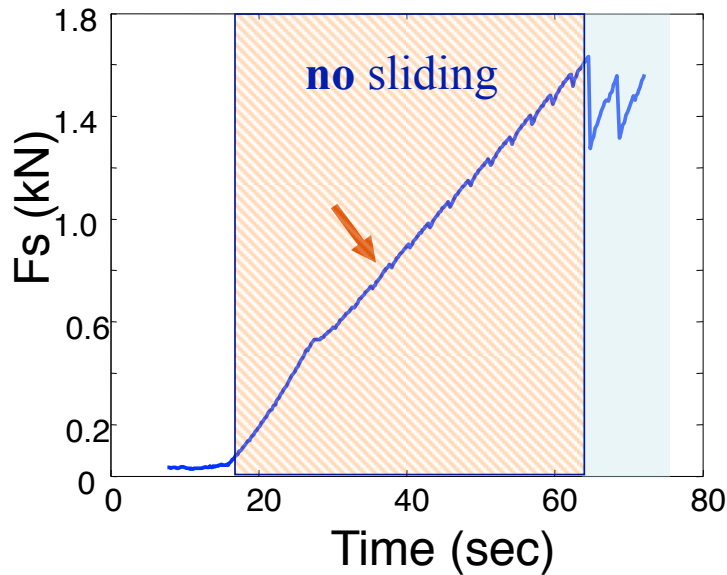
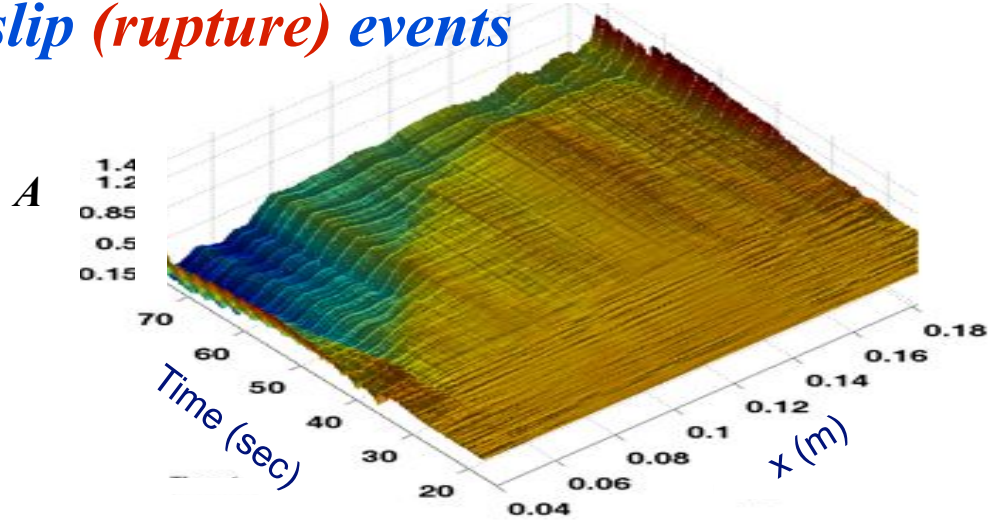
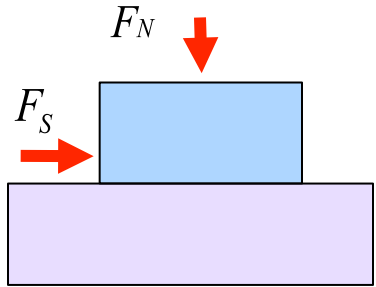
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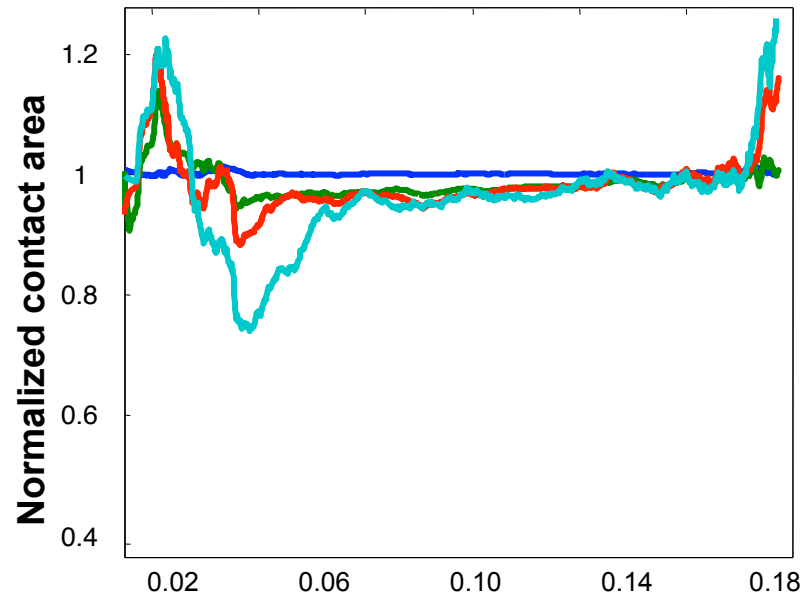
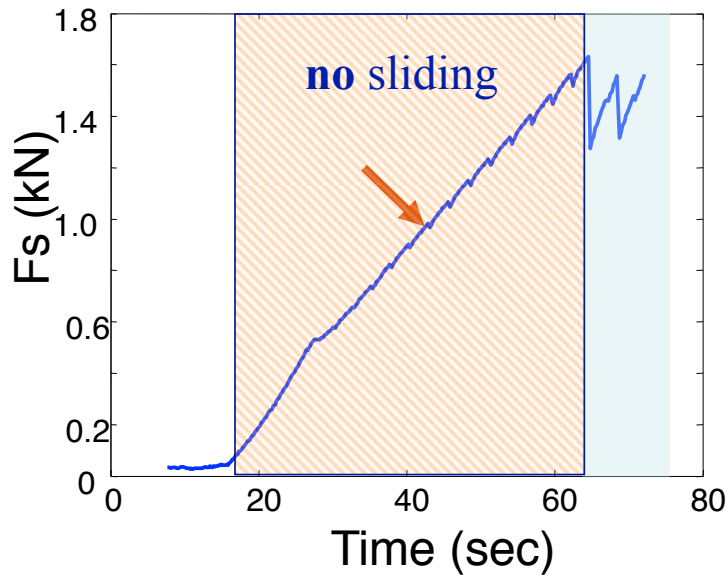
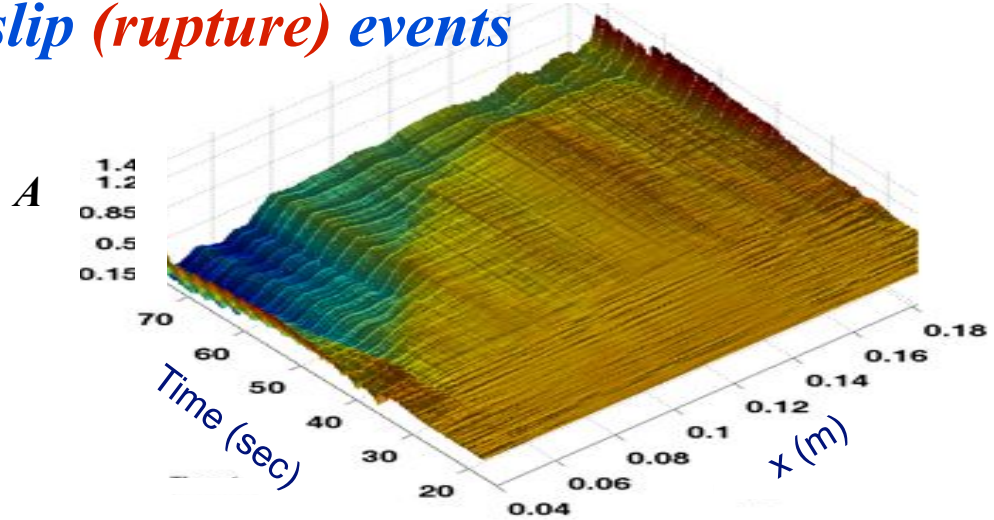
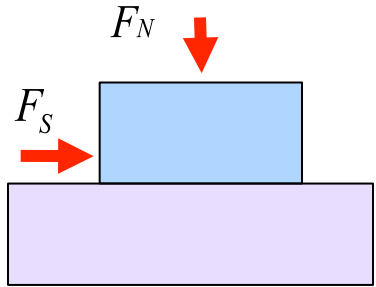
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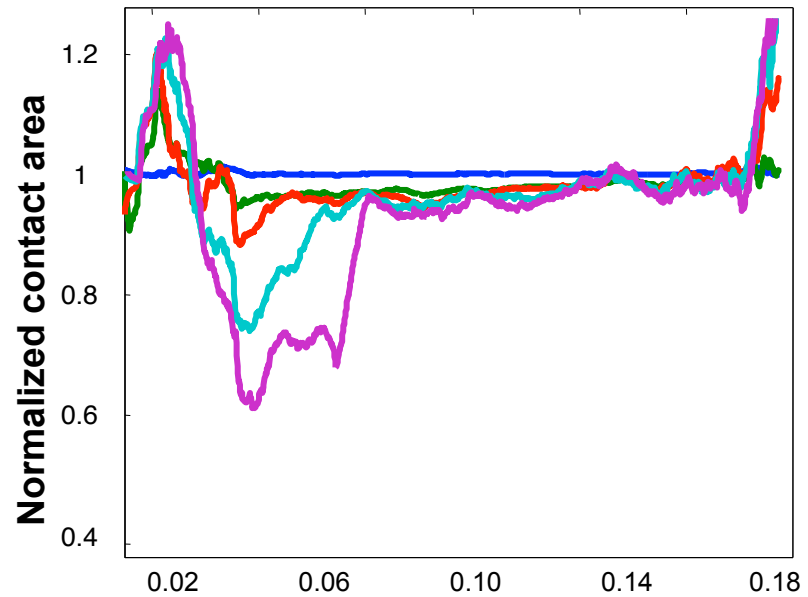
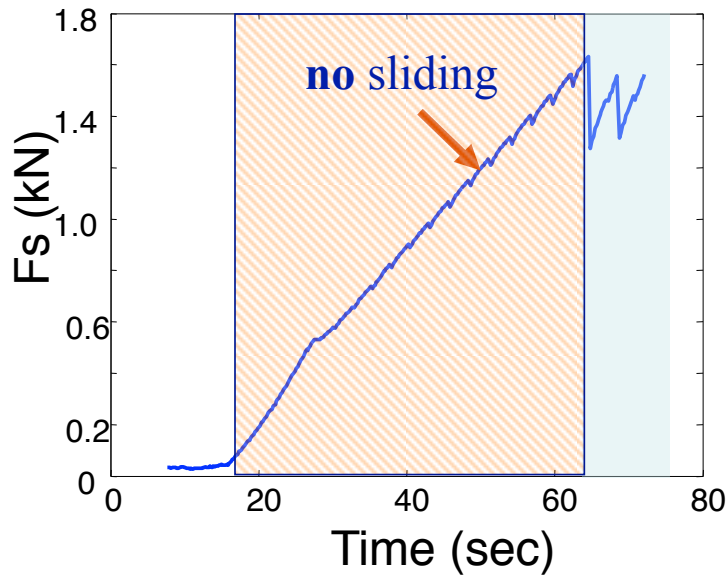
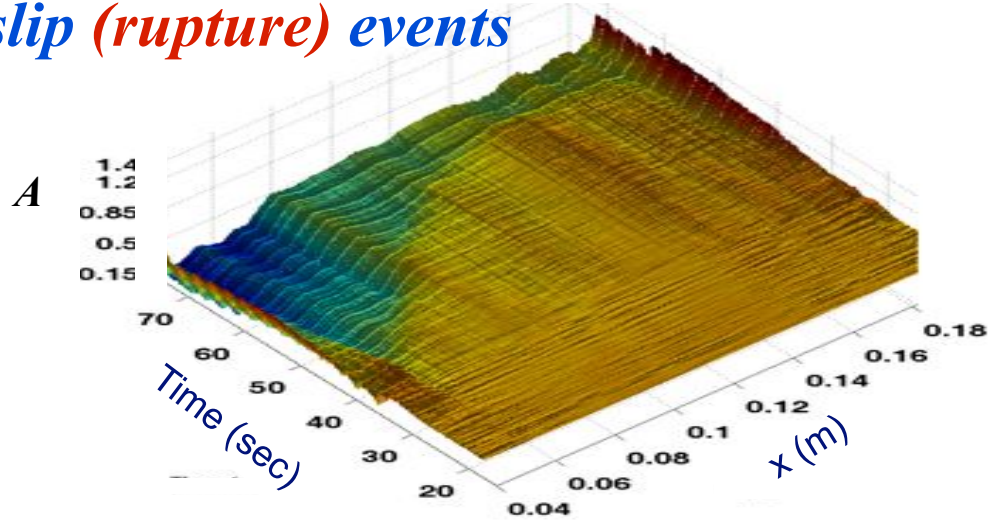
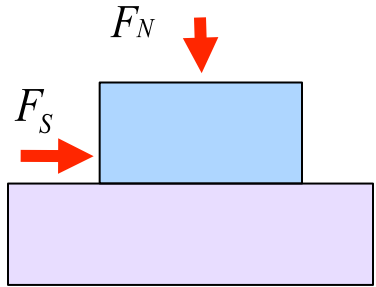
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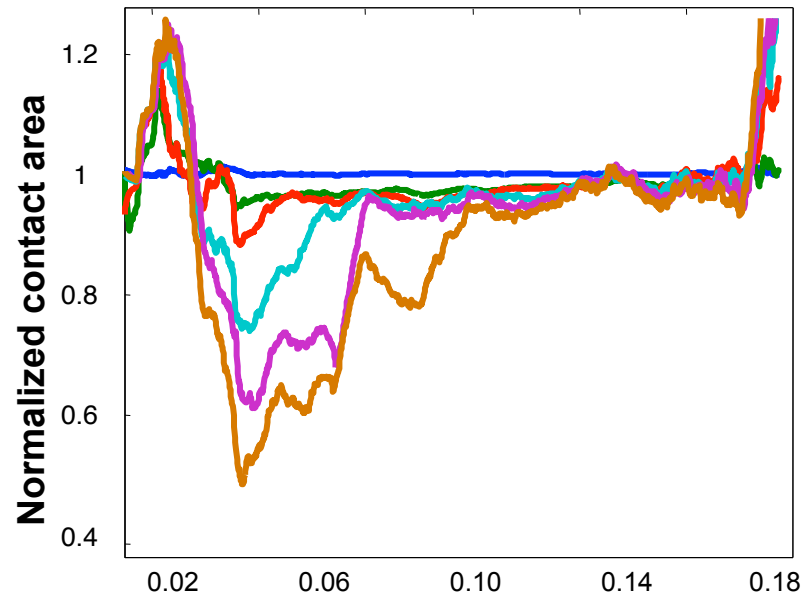
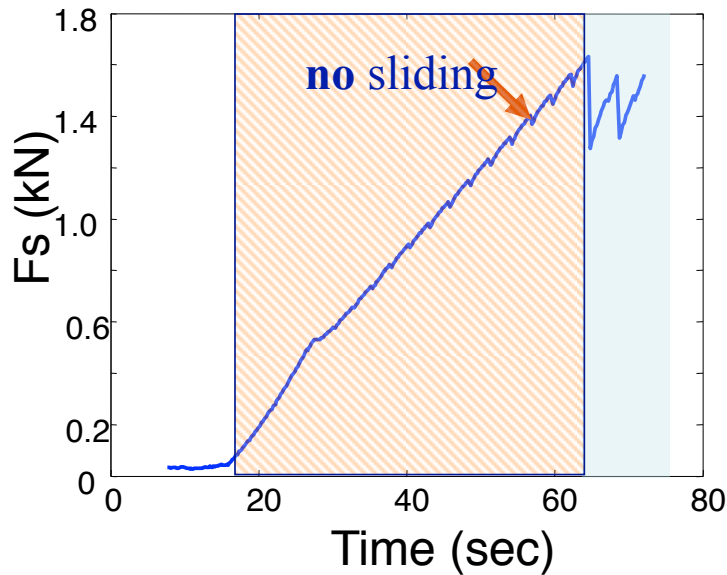
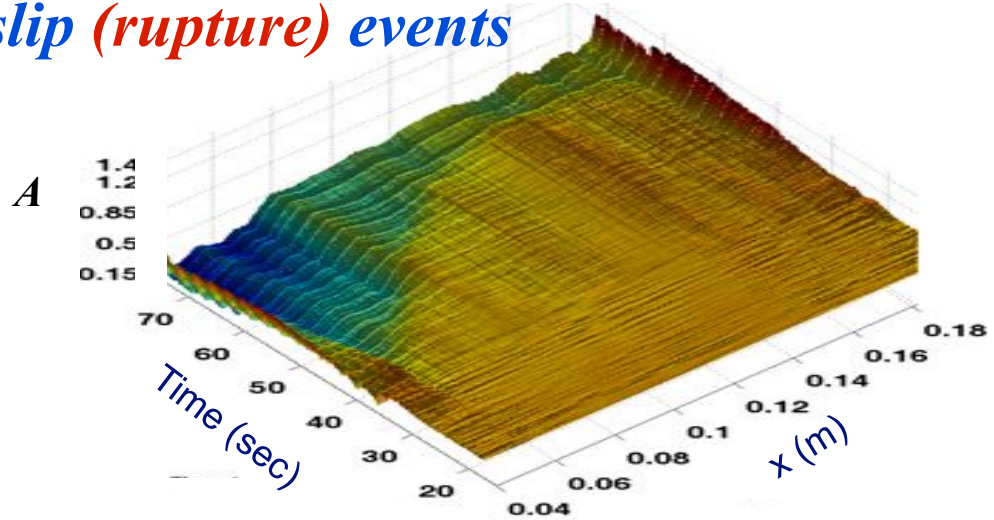
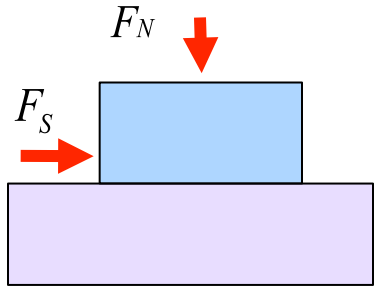
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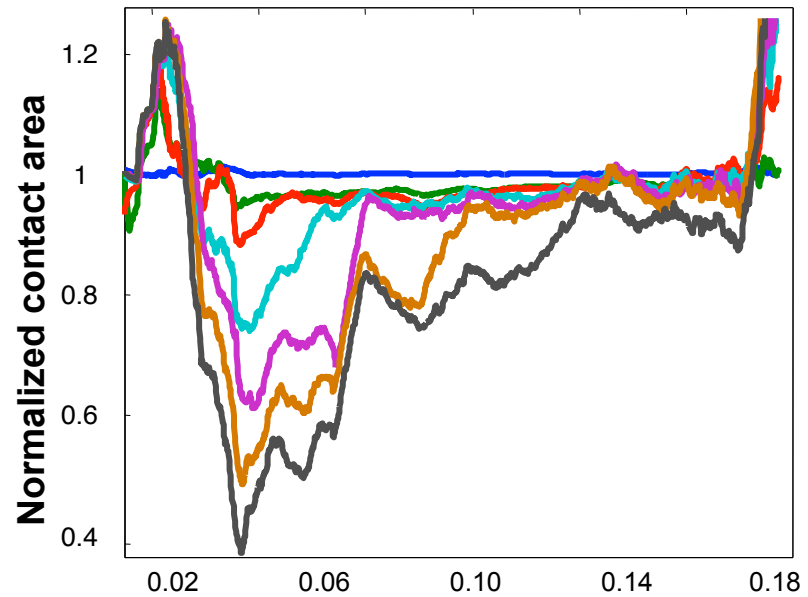
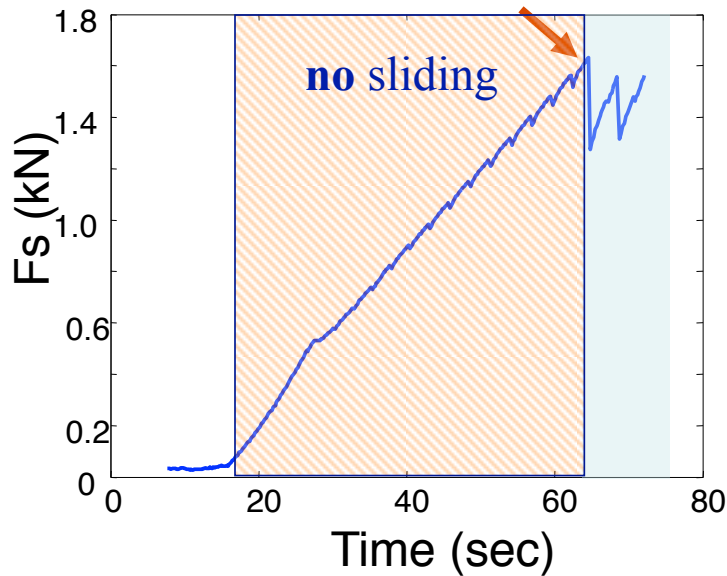
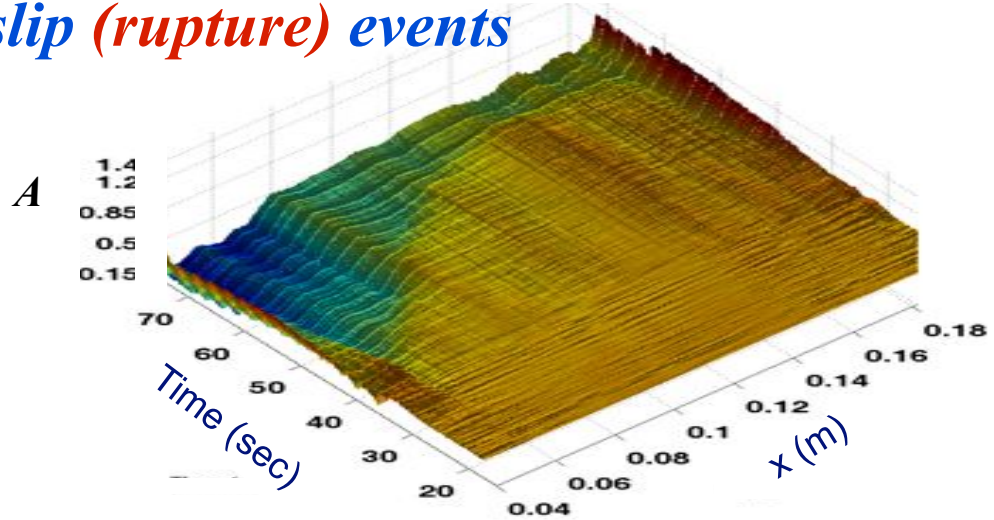
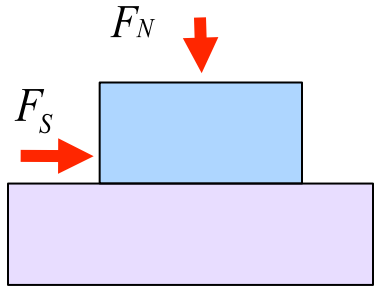
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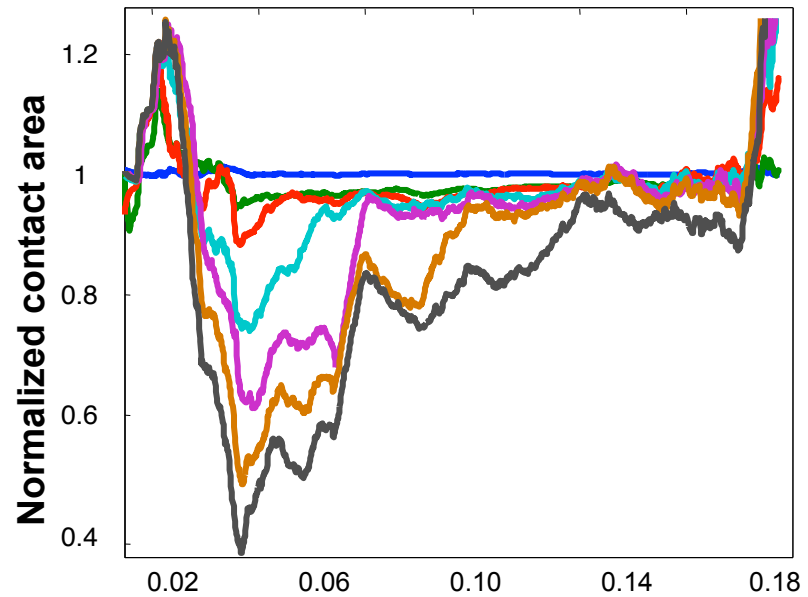
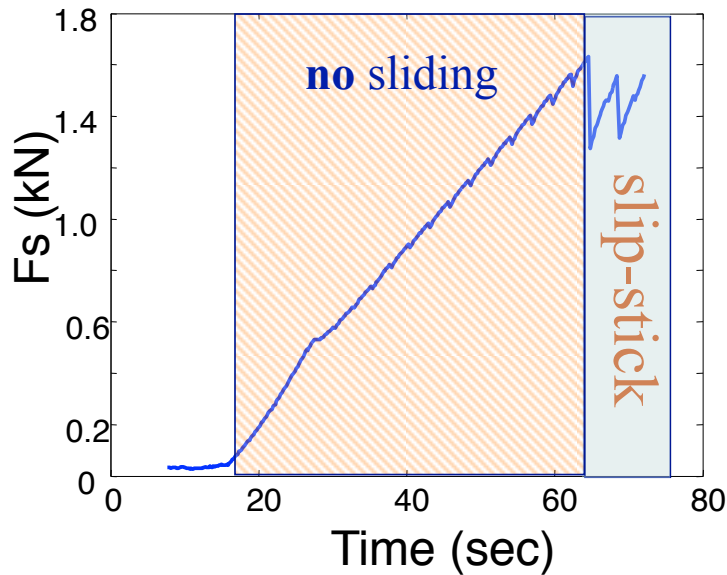
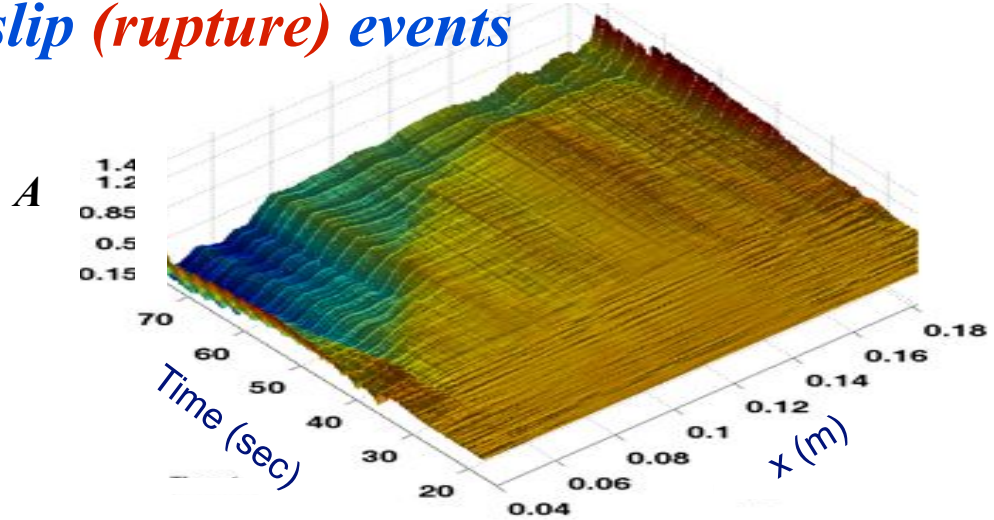
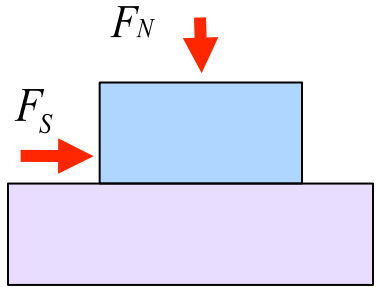
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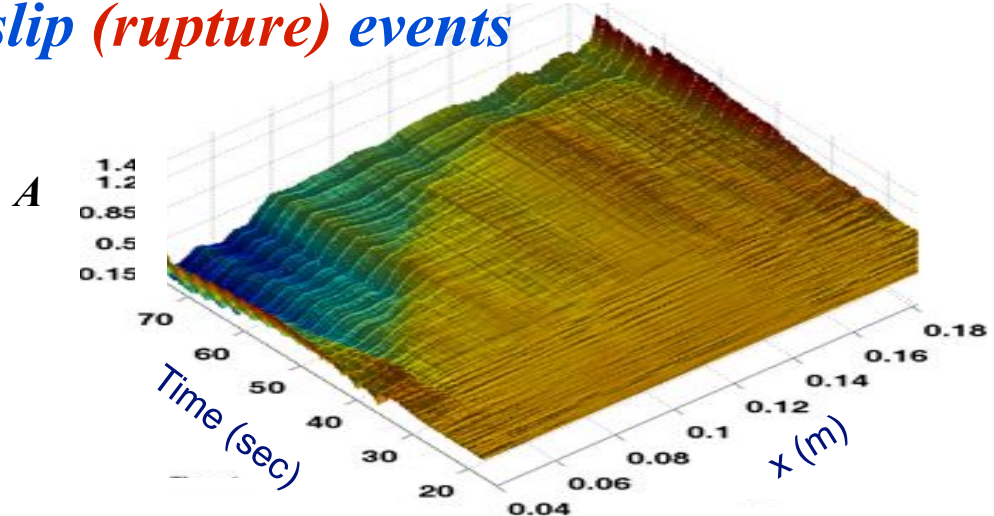
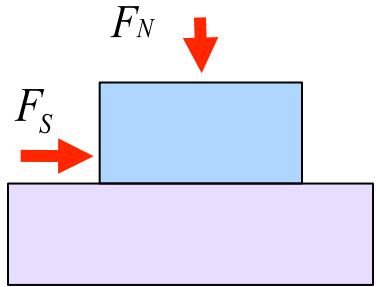
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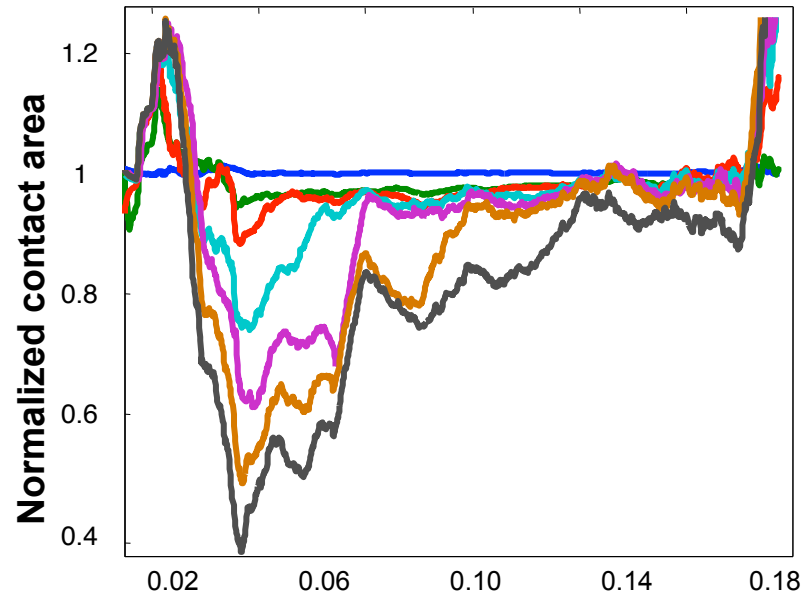
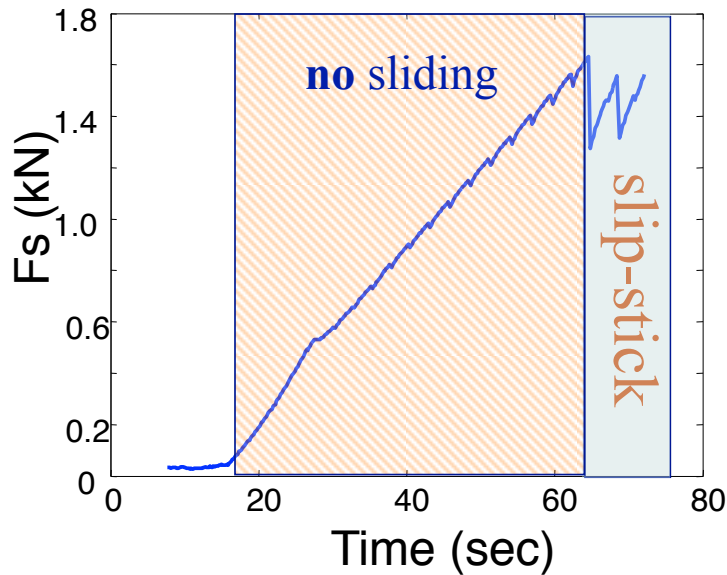


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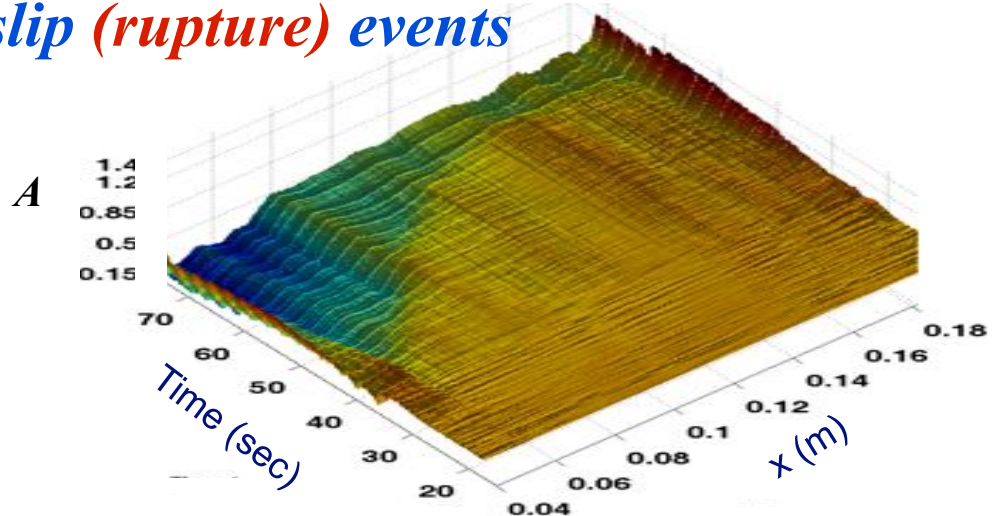
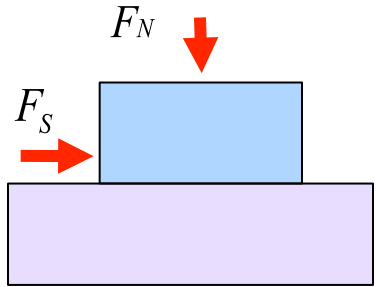


- Precursors create **highly non-uniform $A(x)$**

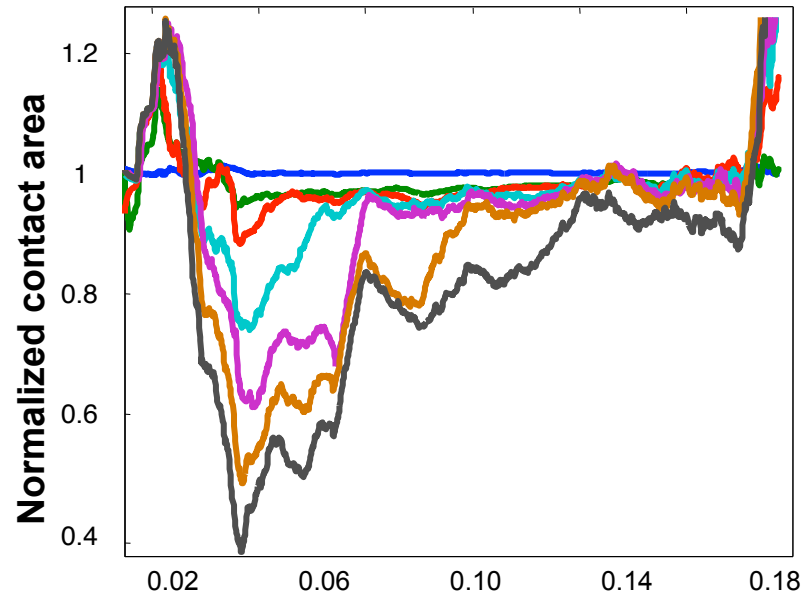
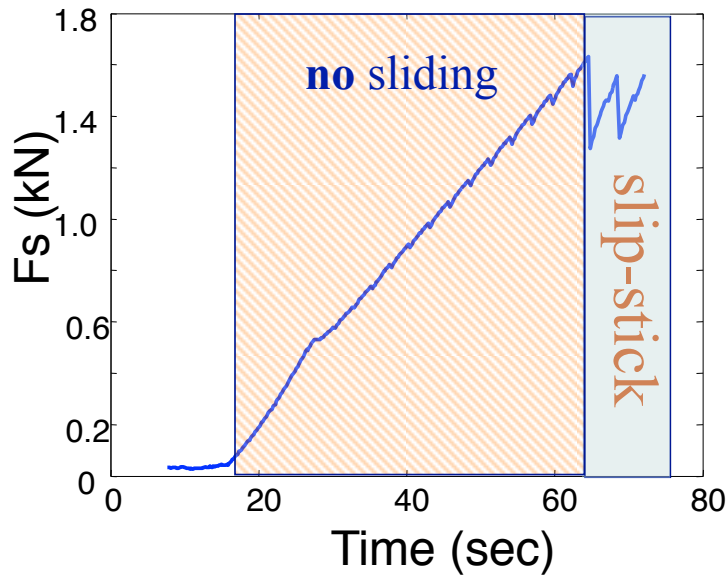


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The **contact-area/stress distribution** can also change *dynamically* via *arrested precursory slip (rupture) events*



- Precursors create **highly non-uniform** $A(x)$
- $A(x)$ profile $\propto \sigma(x)$ (normal stress)

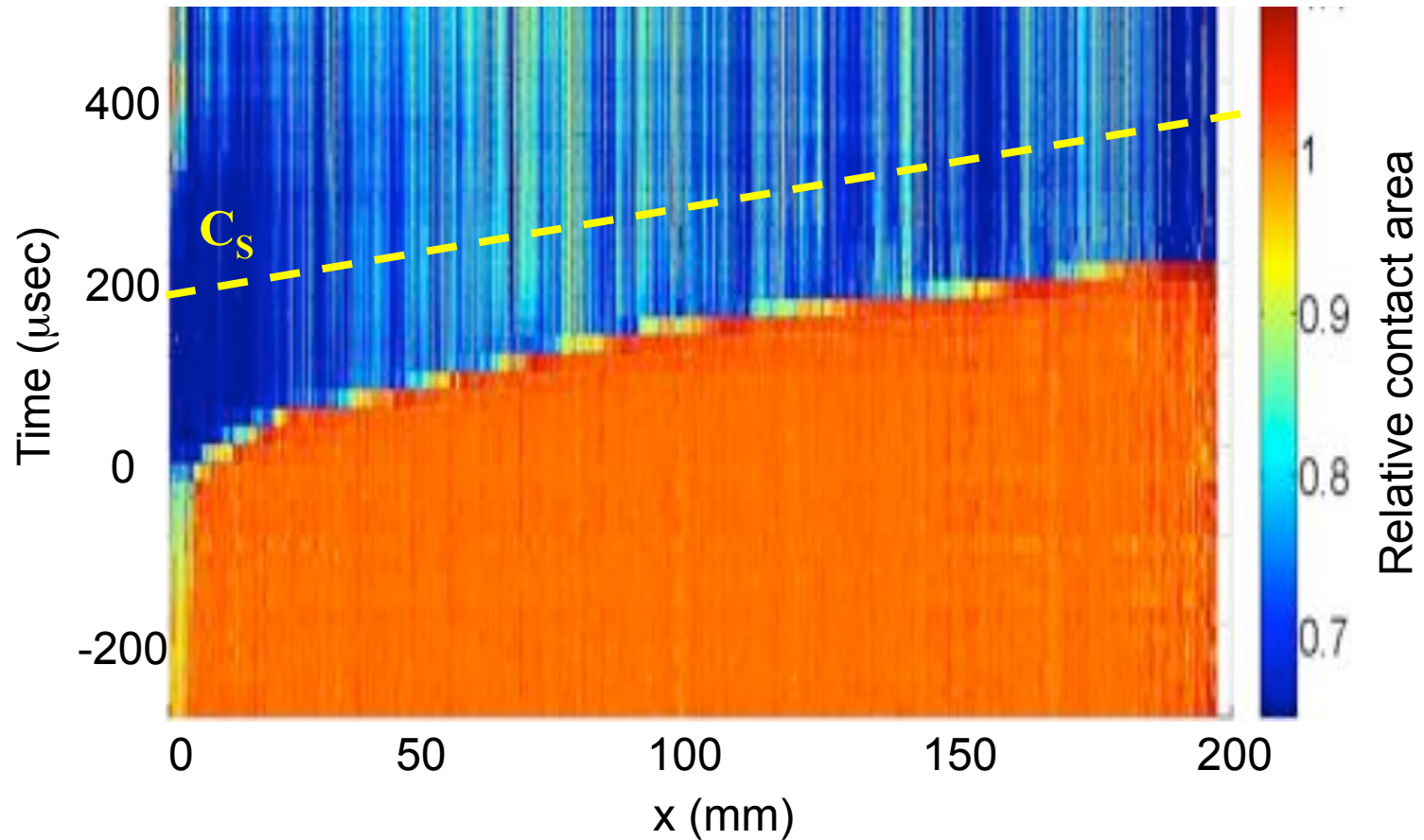


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What types of rupture events occur upon slip initiation?

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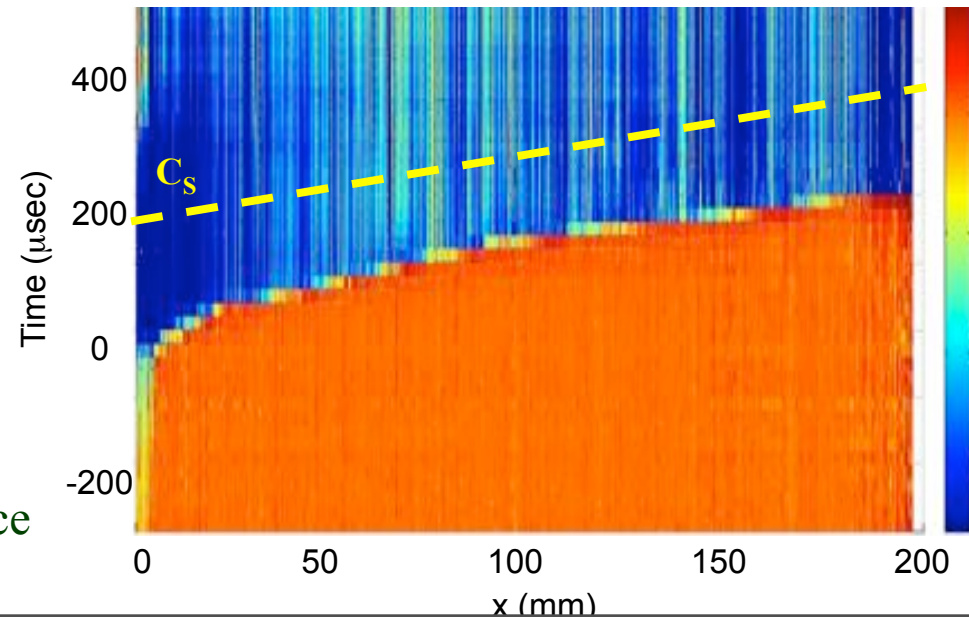
“Garden variety” rupture ($v < C_s$)



Horizontal lines are $A(x)$ over the entire interface
separated in time by $2\text{-}20\mu\text{s}$

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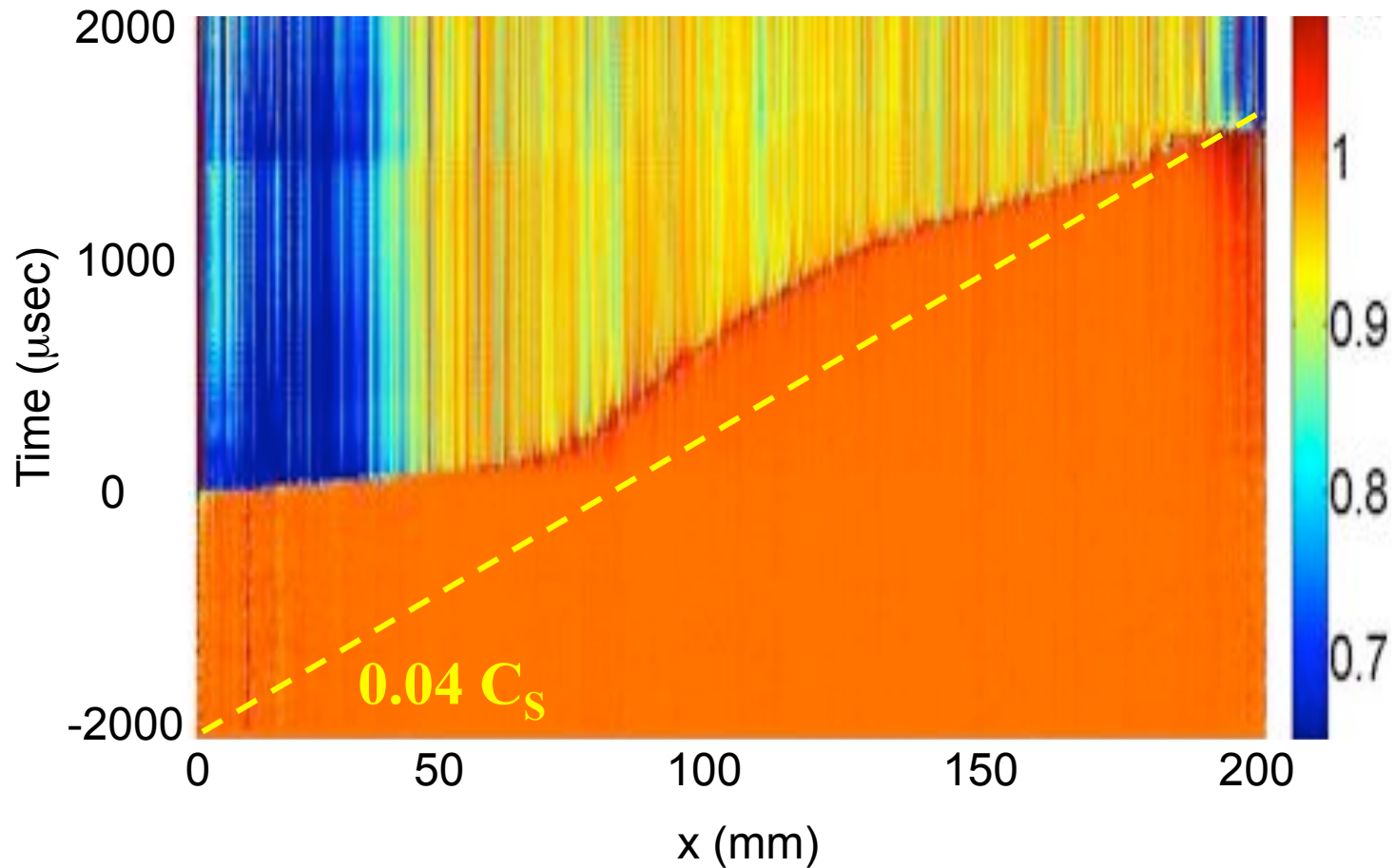
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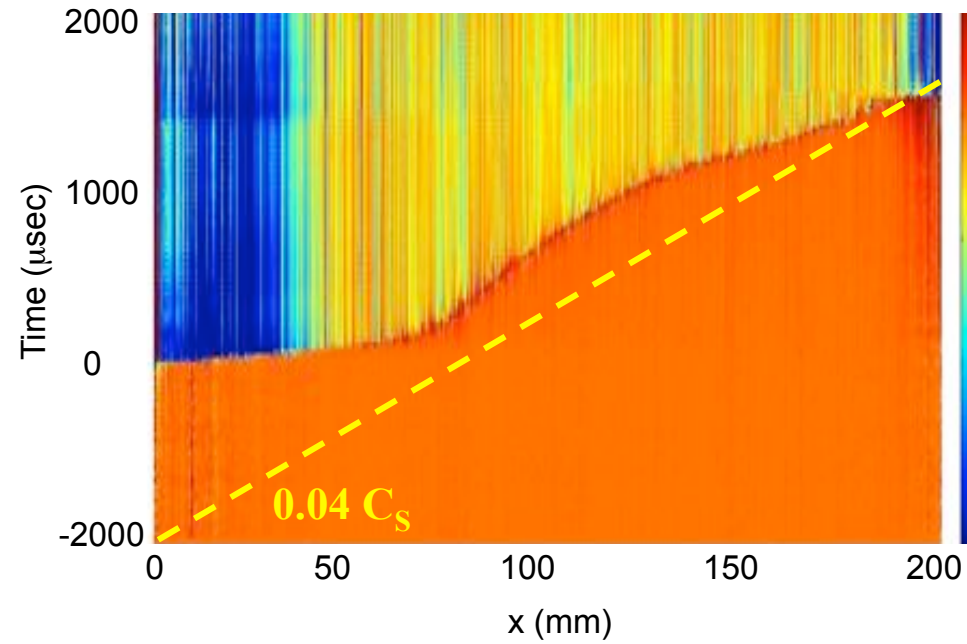
“Slow” rupture ($v \ll C_S$)



Horizontal lines are $A(x)$ over the entire interface
separated in time by $2\text{-}20\mu\text{s}$

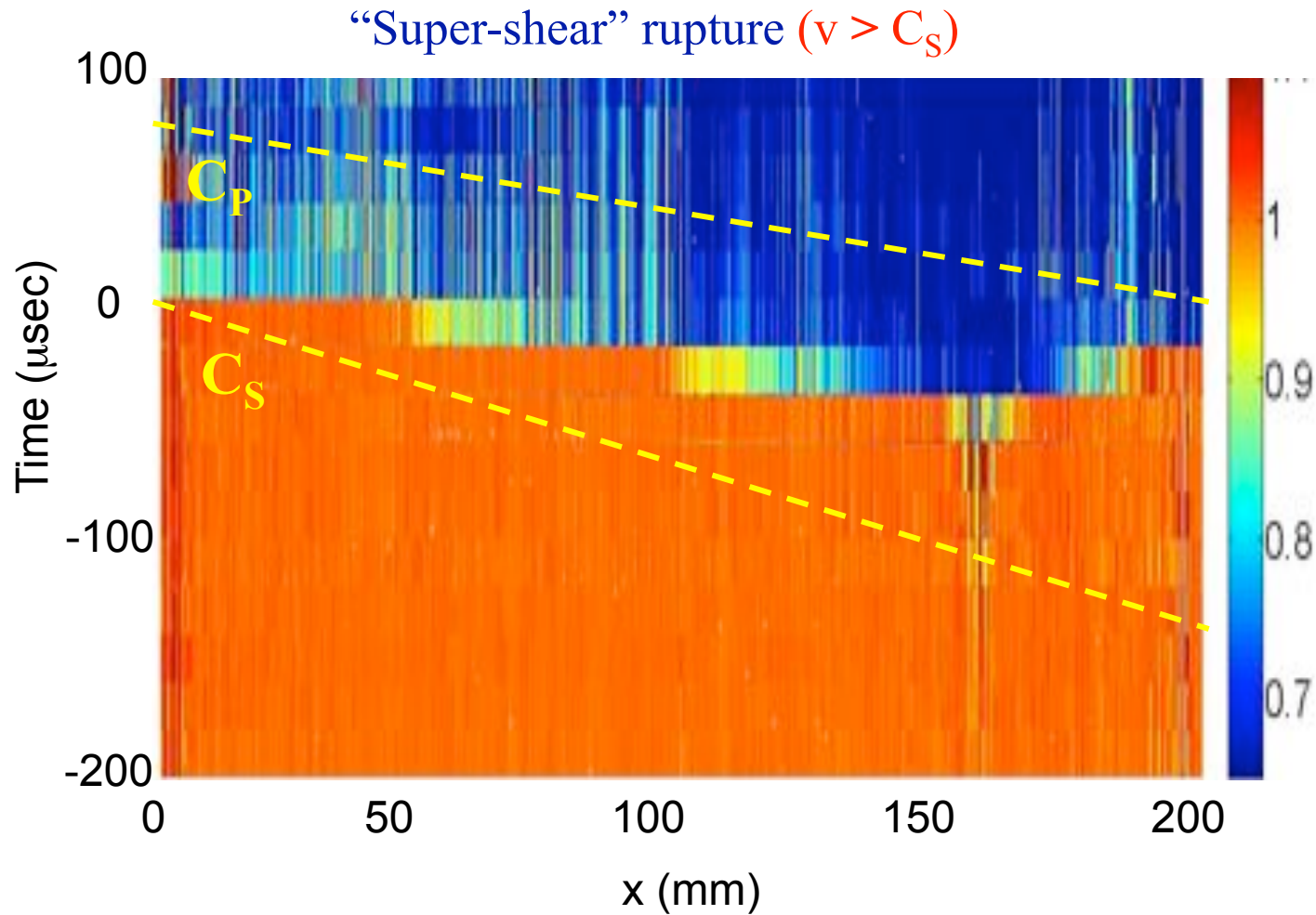
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“Slow” rupture ($v \ll C_s$)



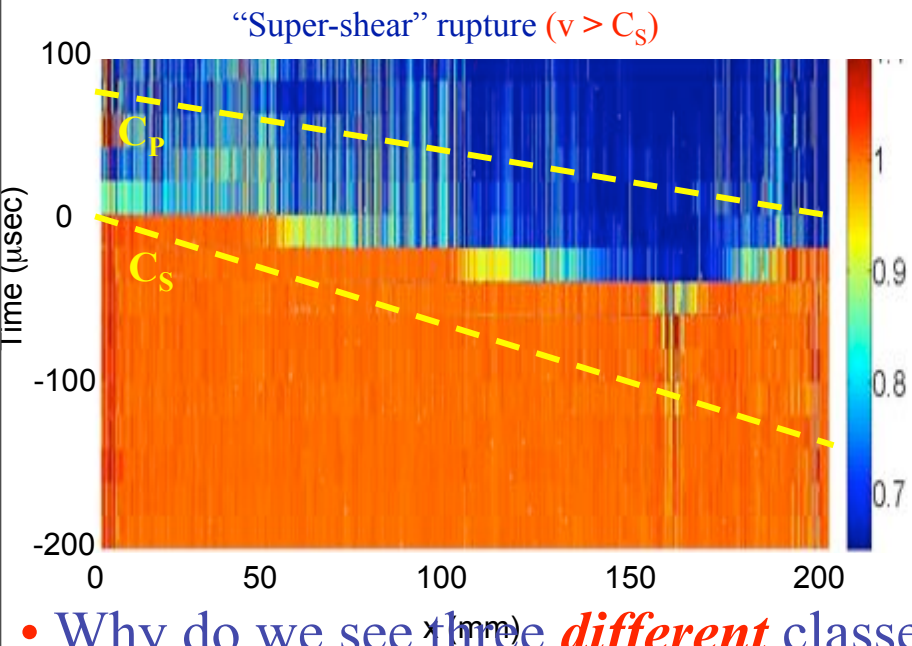
Horizontal lines are $A(x)$ over the entire interface
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What types of rupture events occur upon slip initiation?

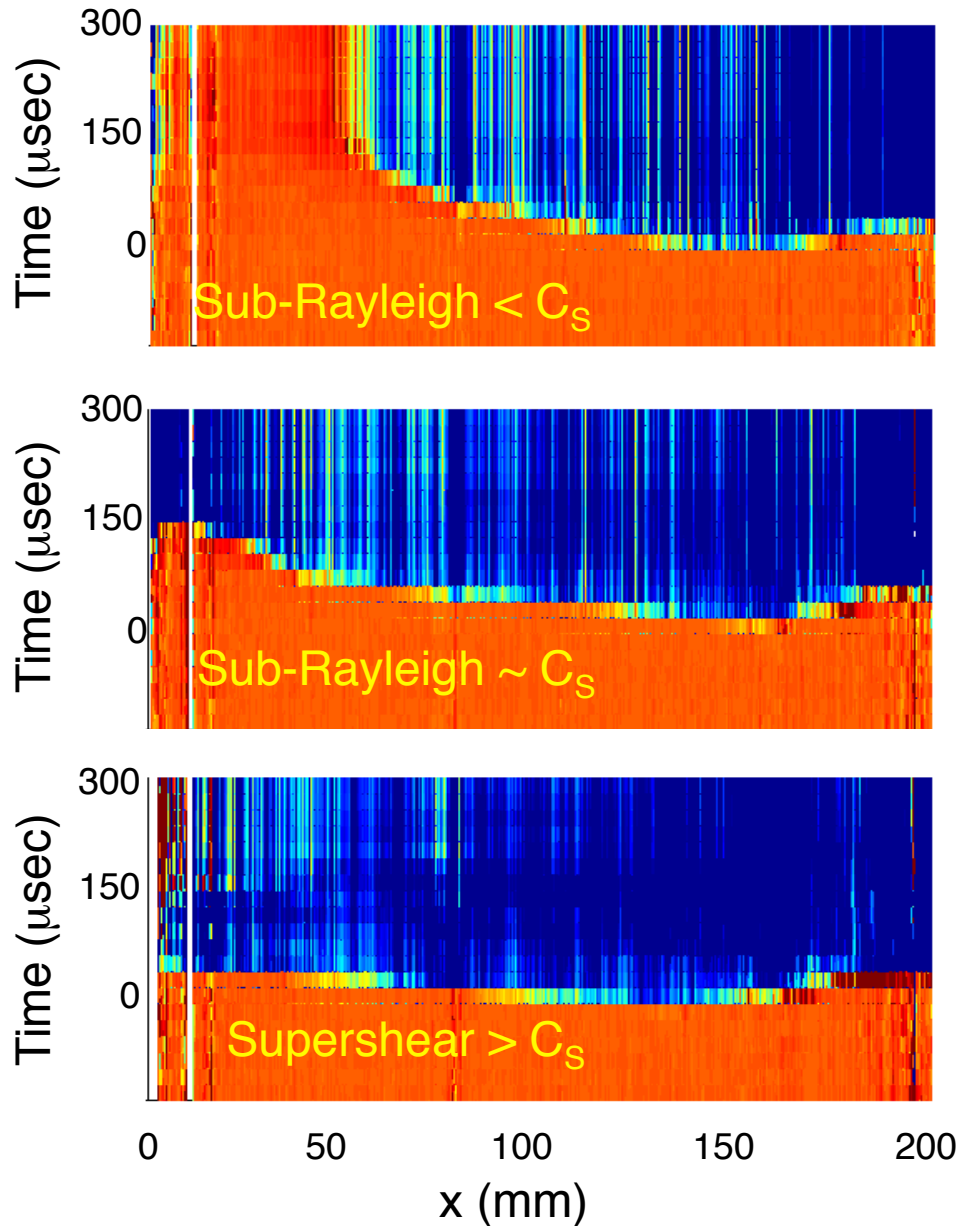


Horizontal lines are $A(x)$ over the entire interface
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What types of rupture events occur upon slip initiation?



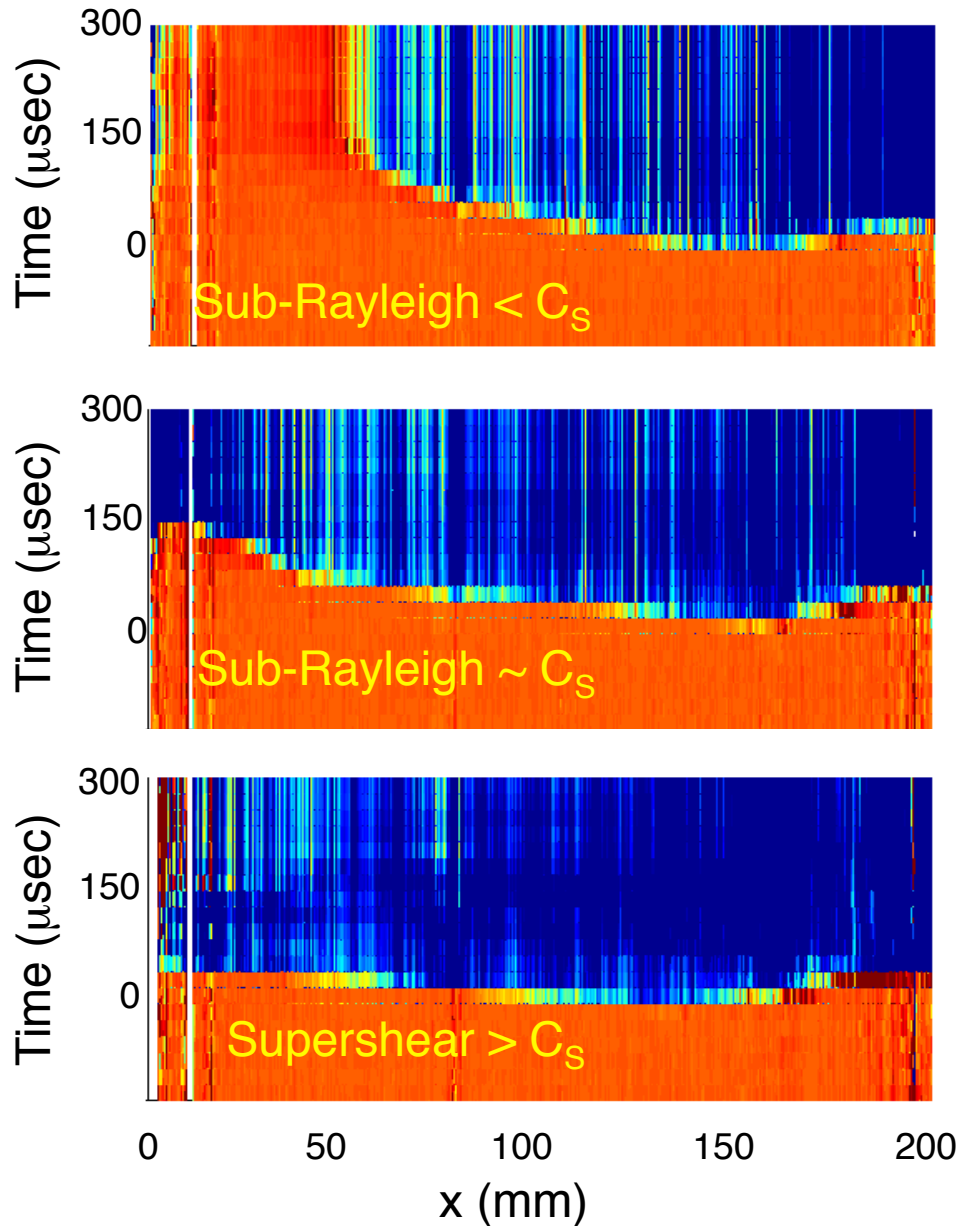
- Why do we see three *different* classes of “crack-like” behaviors?
- *When* do we see them?
- Can we *predict* which of the different types of ruptures will occur?



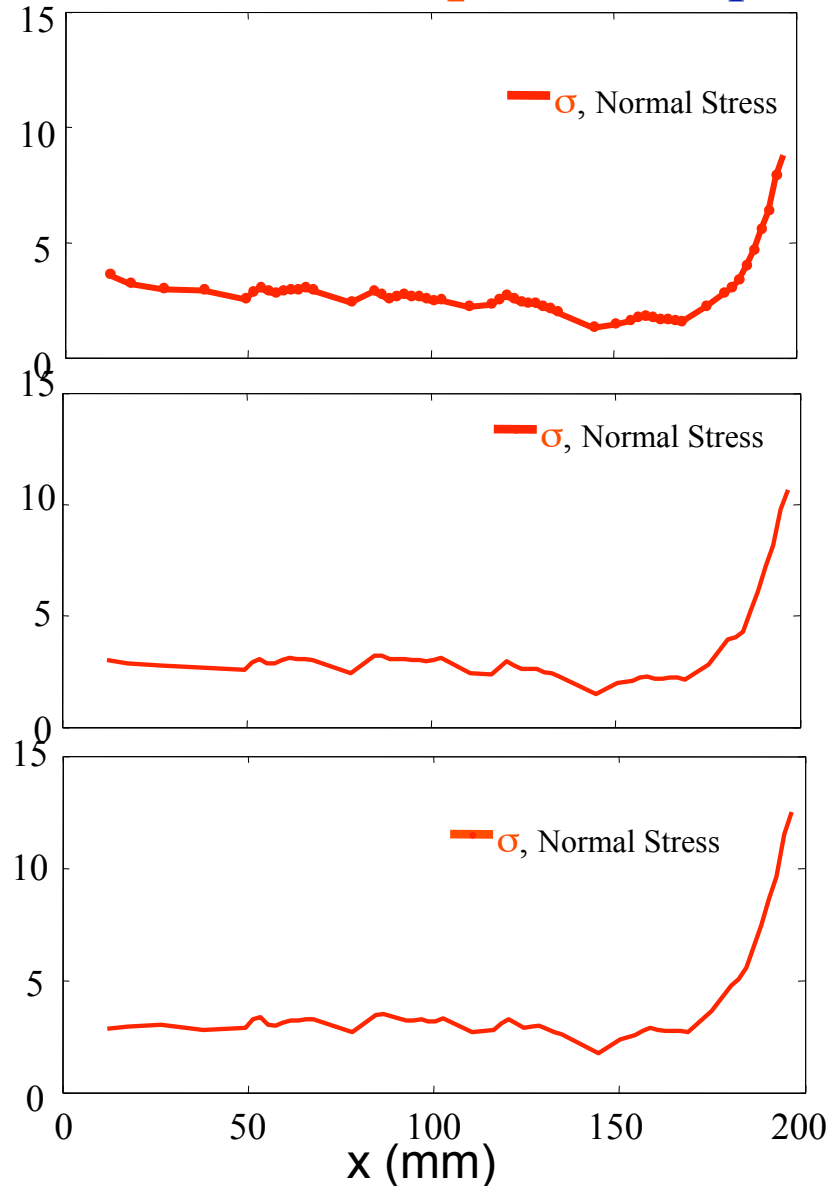
Three successive slip events driven under *ostensibly* the *same external* loading conditions:

Let's look at the *measured* stress distributions...

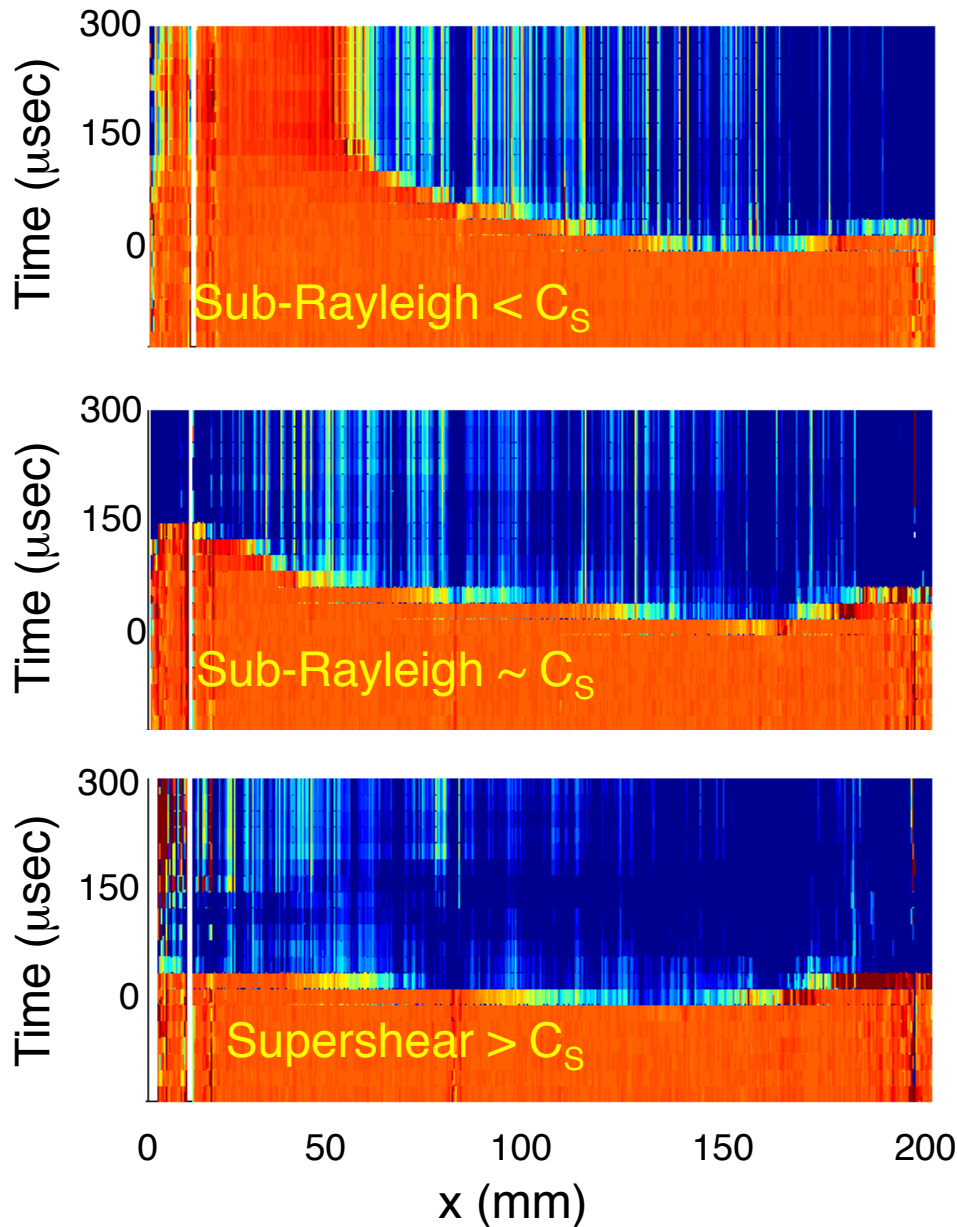
- Normal stress distributions are nearly identical!



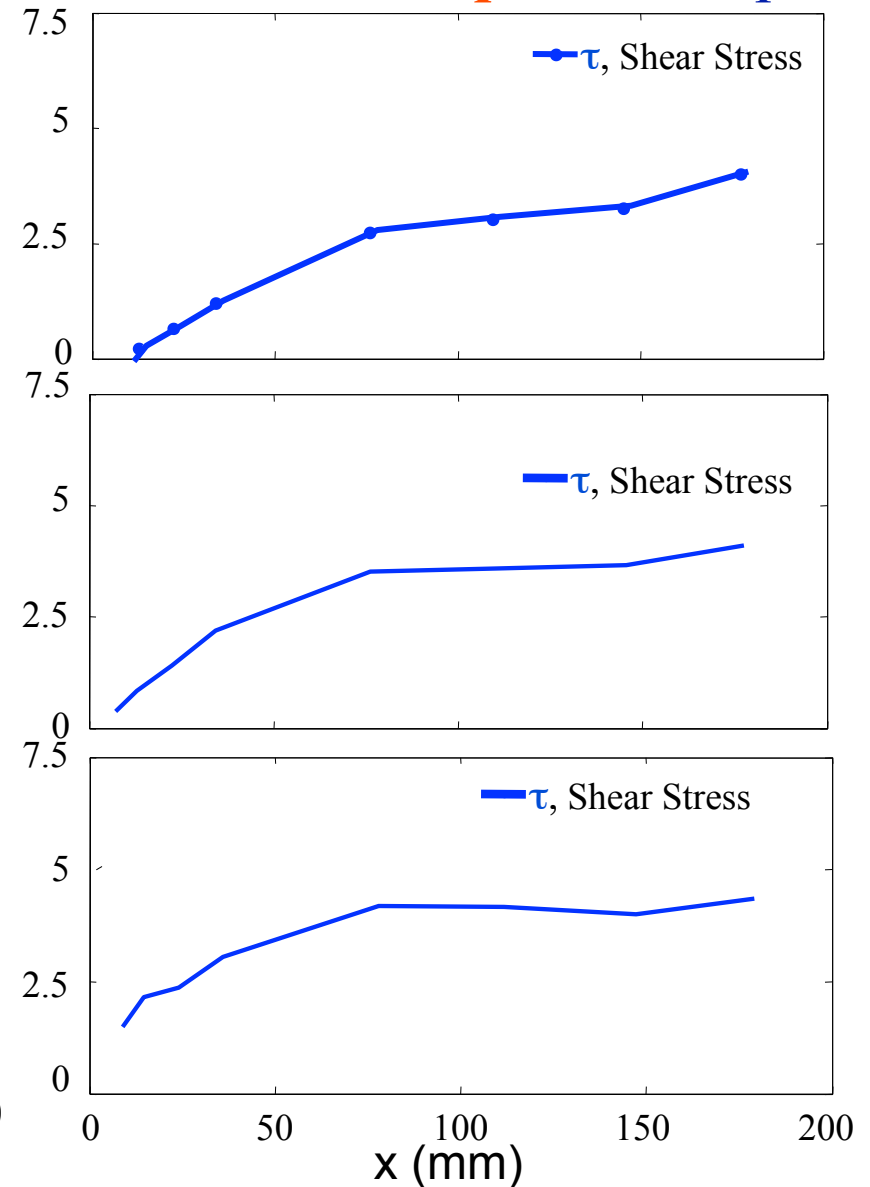
Stresses (MPa) *prior* to slip



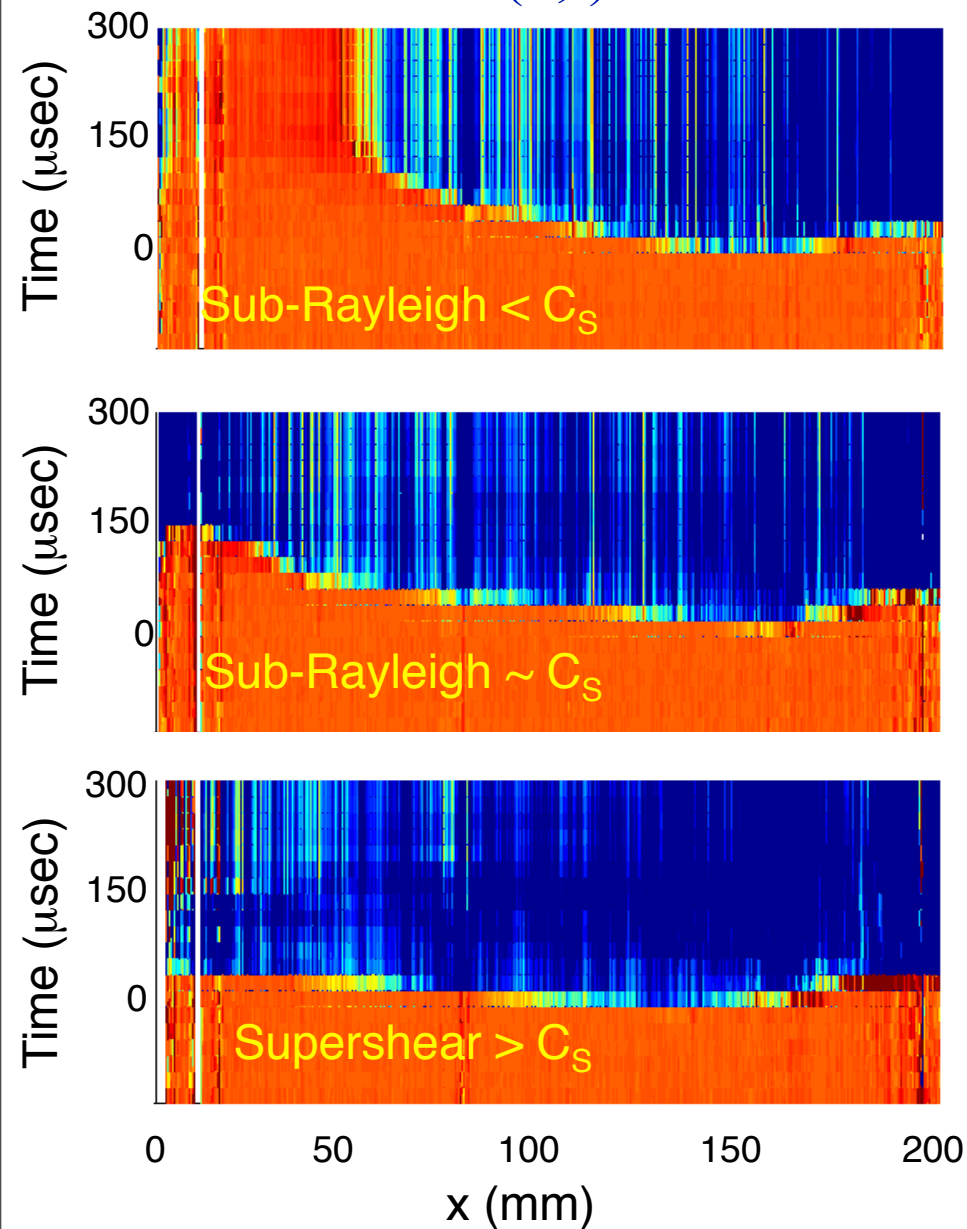
- **Shear** stress distributions are very similar! – What's going on?



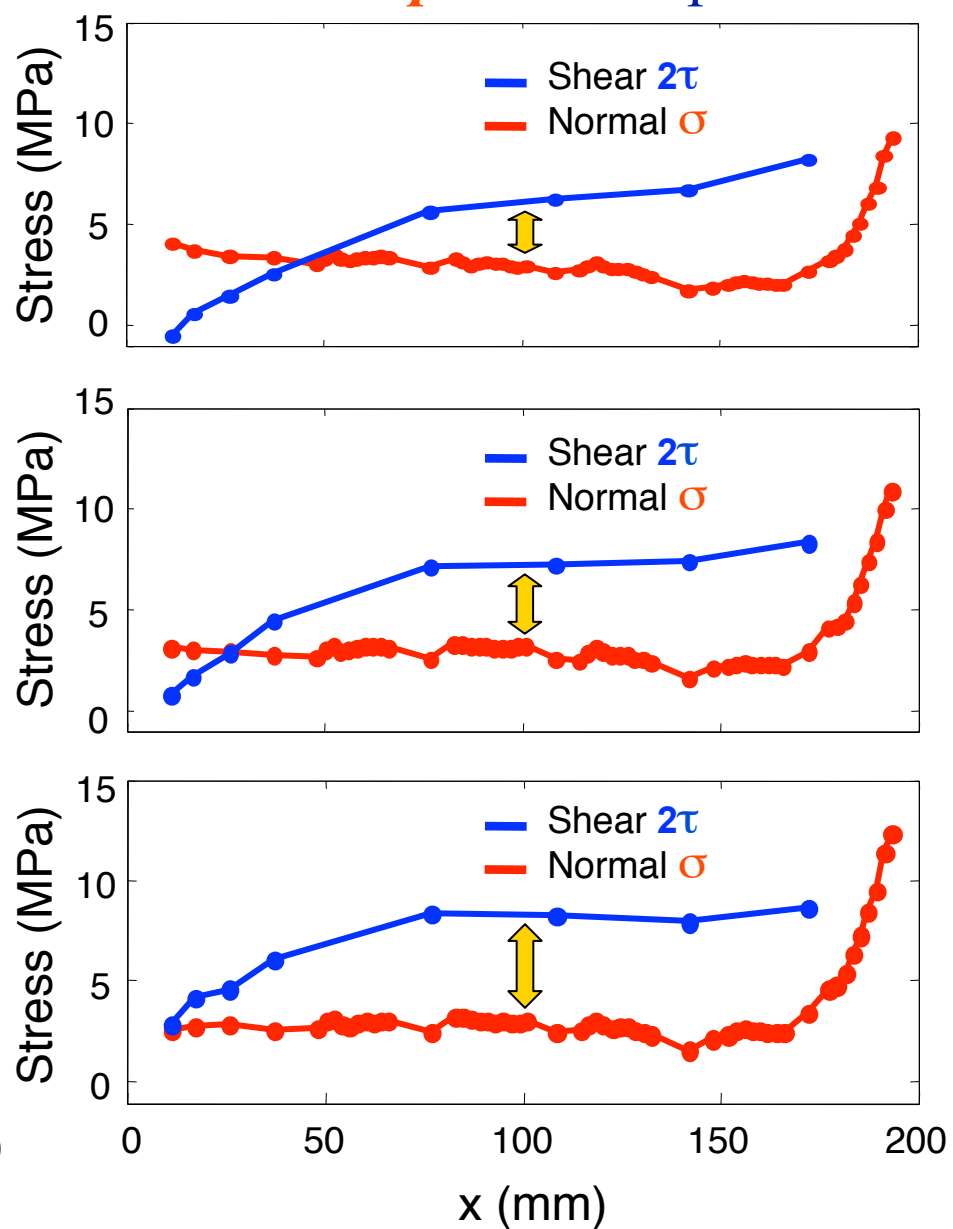
Stresses (MPa) *prior* to slip



$A(x,t)$

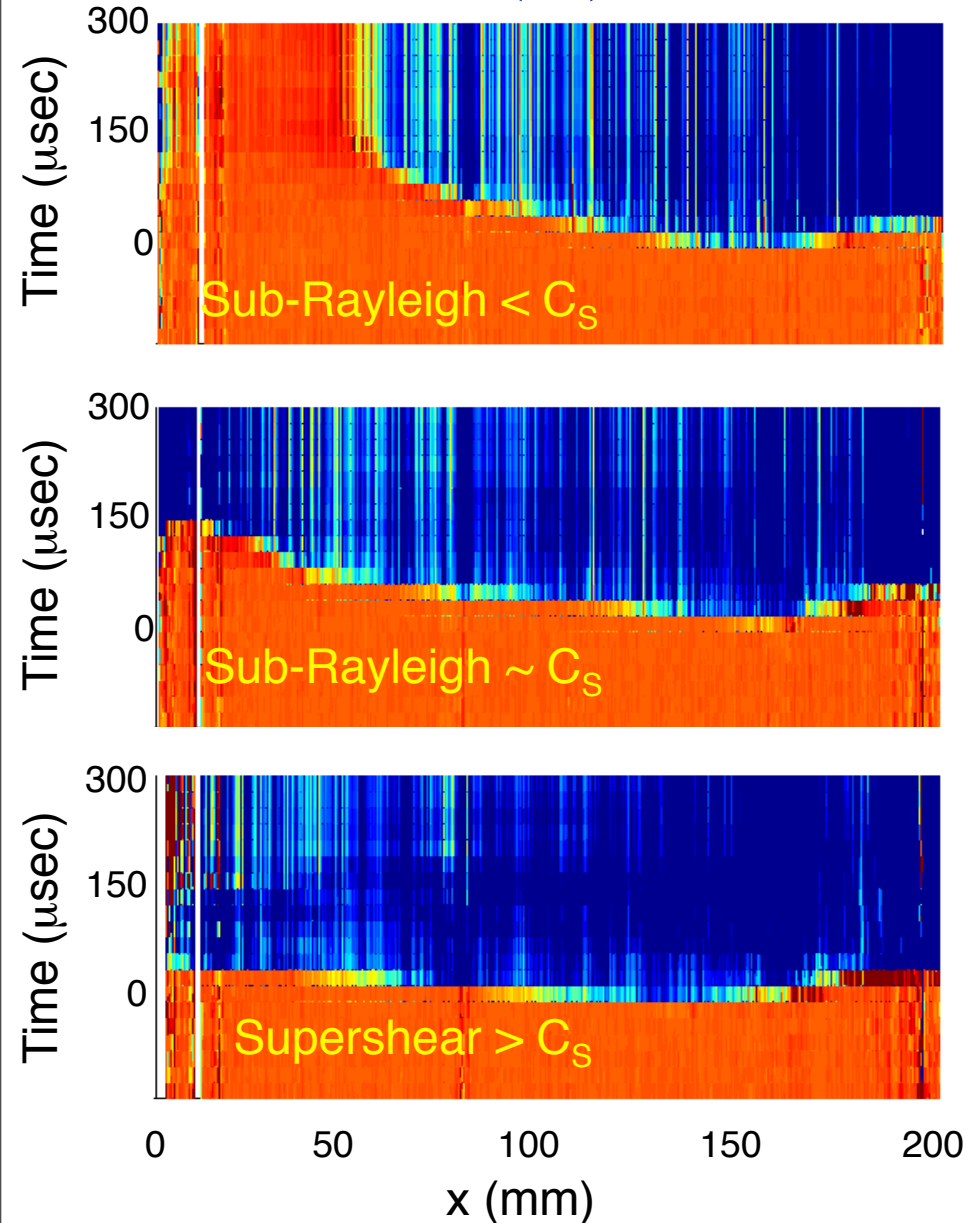


Stresses *prior* to slip

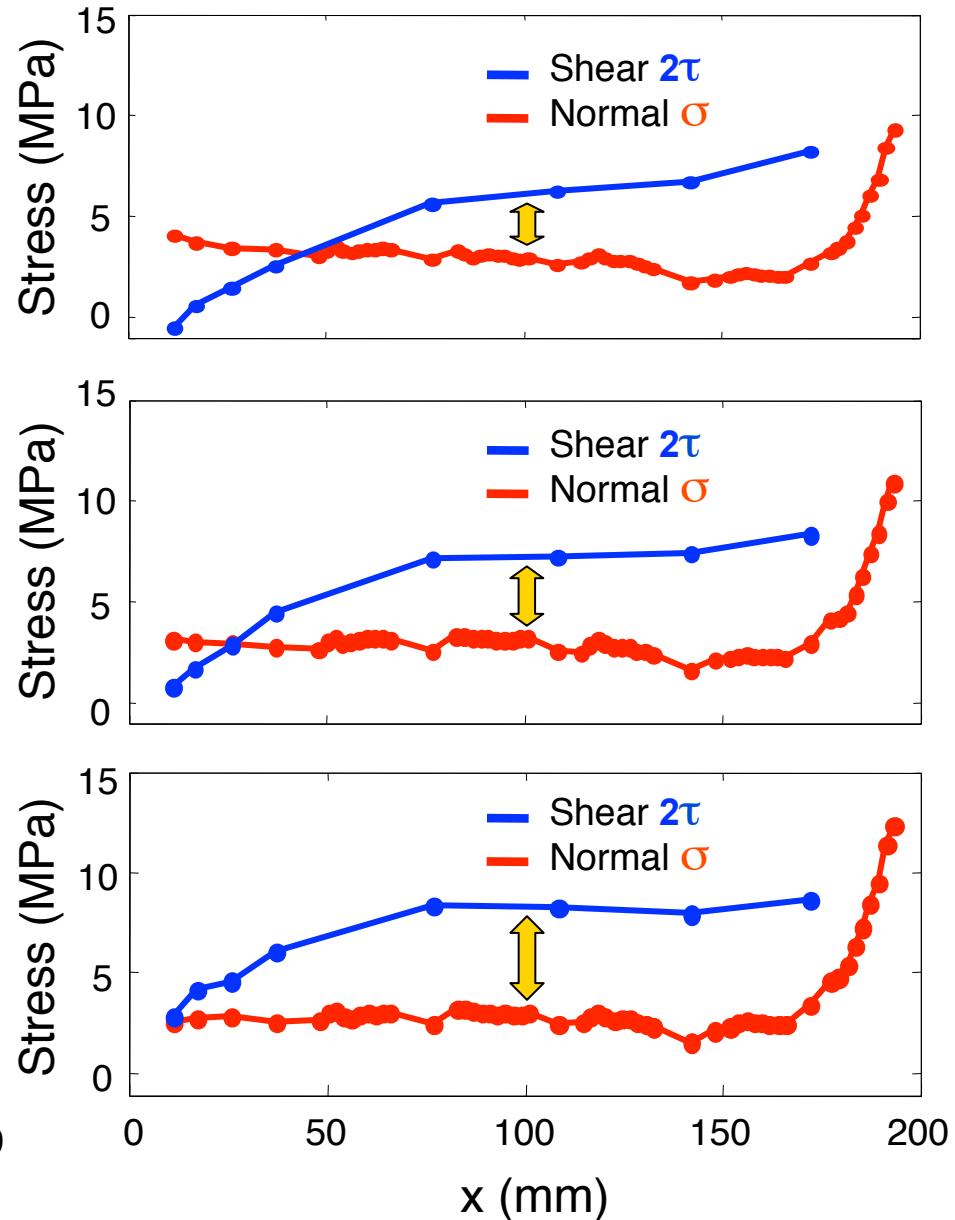


- A hint is given by looking at the *local* stress *differences*!

$A(x,t)$

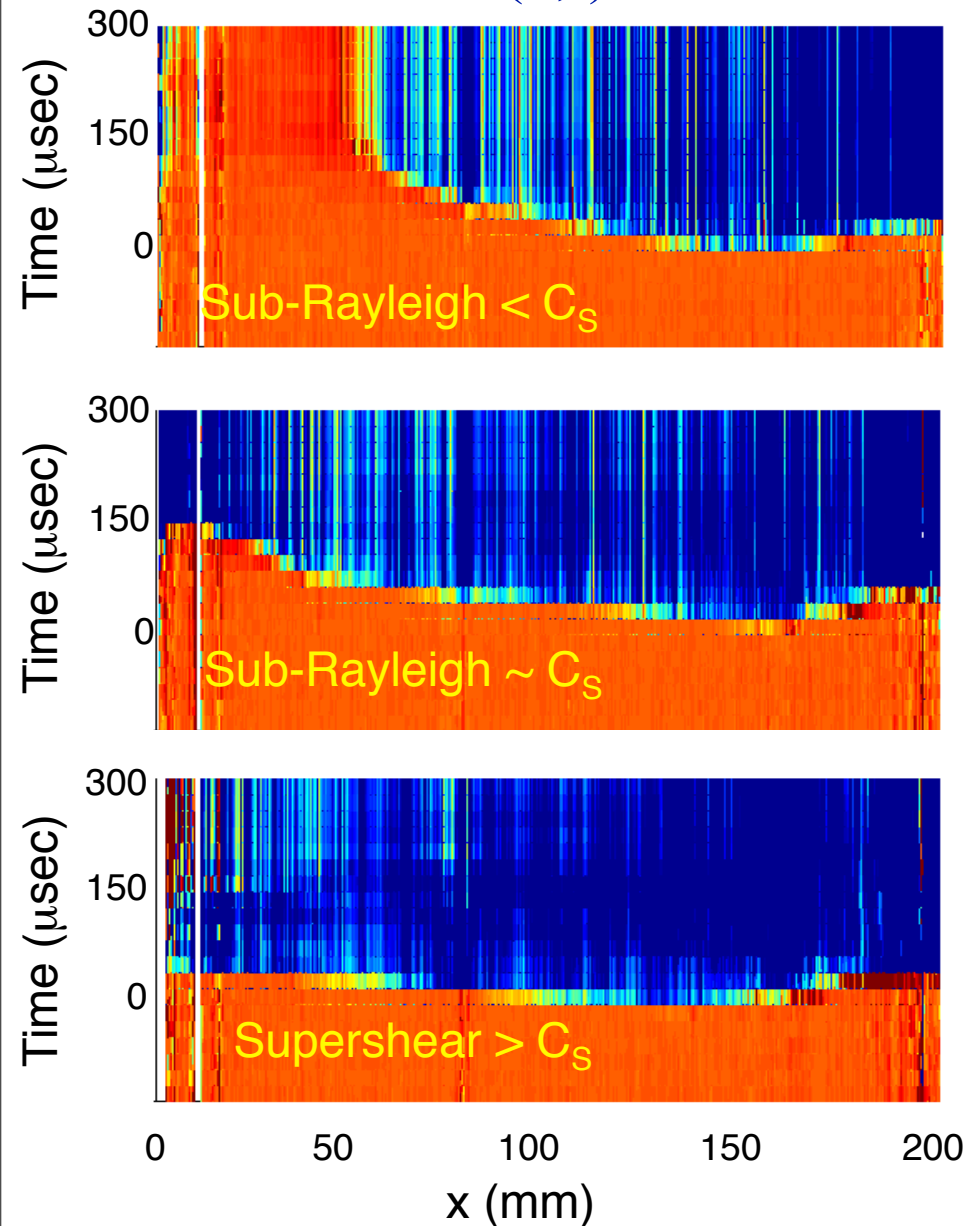


Stresses *prior* to slip

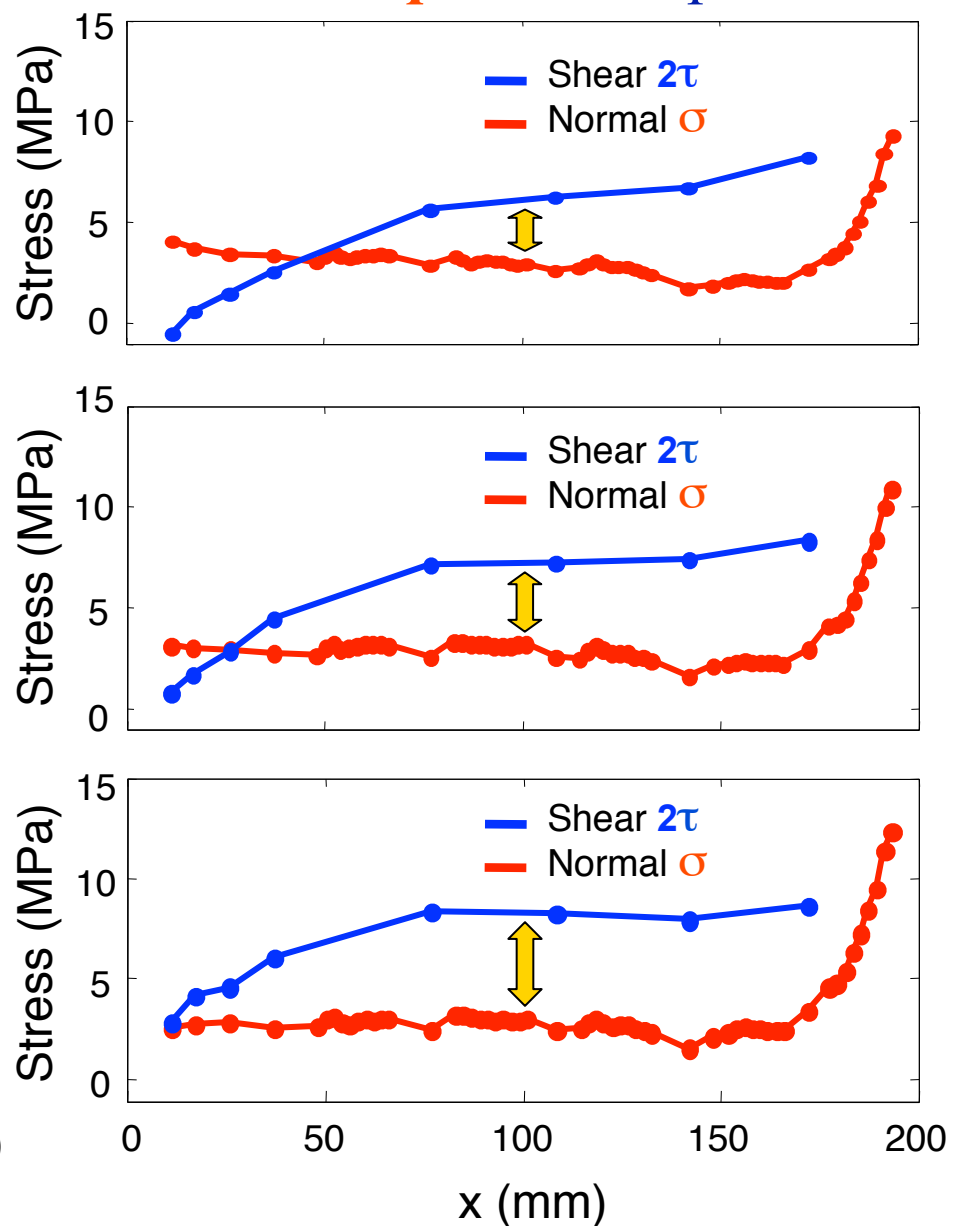


Local stress differences predict the *different* local dynamics

$A(x,t)$



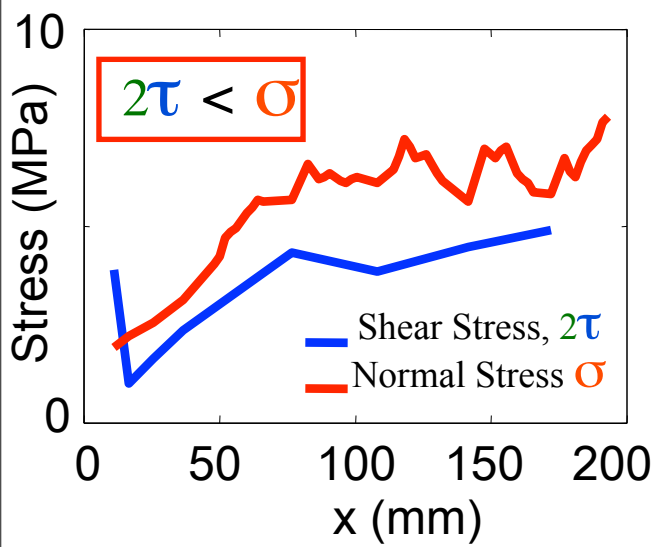
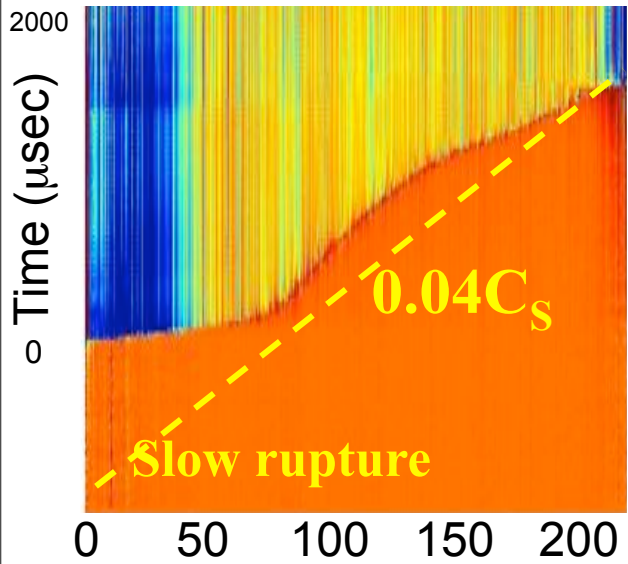
Stresses *prior* to slip



Does this hold for all types of rupture process?

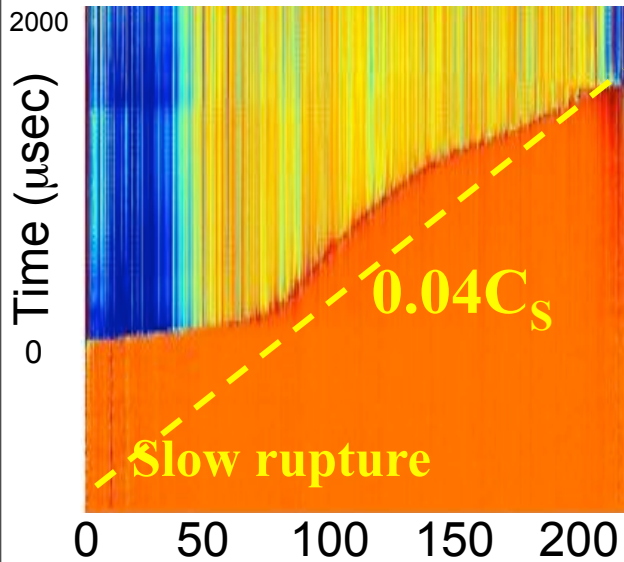
Does this hold for all types of rupture process?

$$v \ll C_s$$

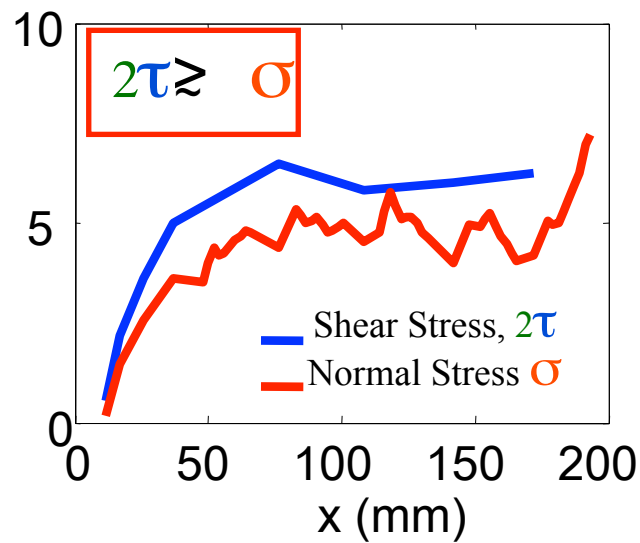
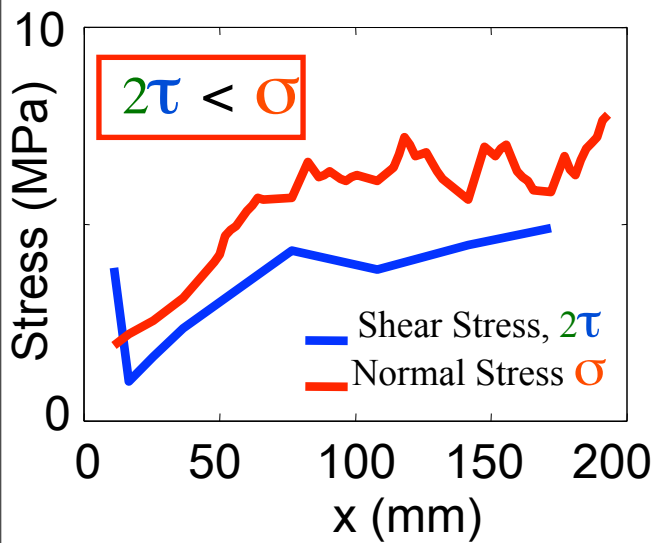
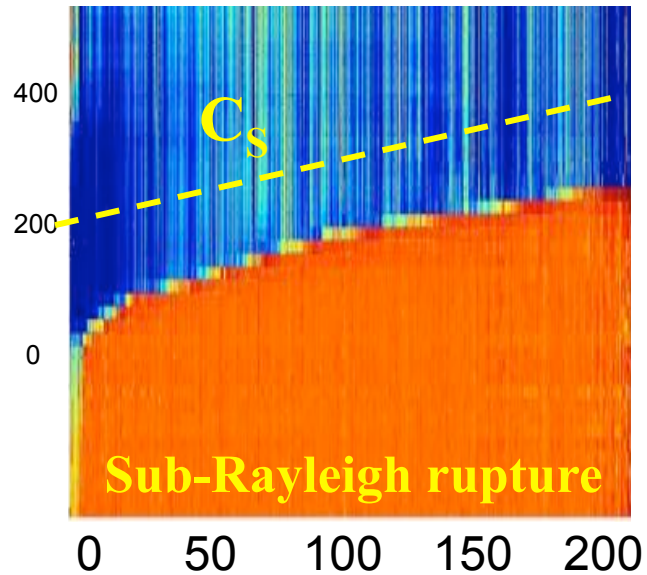


Does this hold for all types of rupture process?

$$v \ll C_s$$



$$v < C_s$$

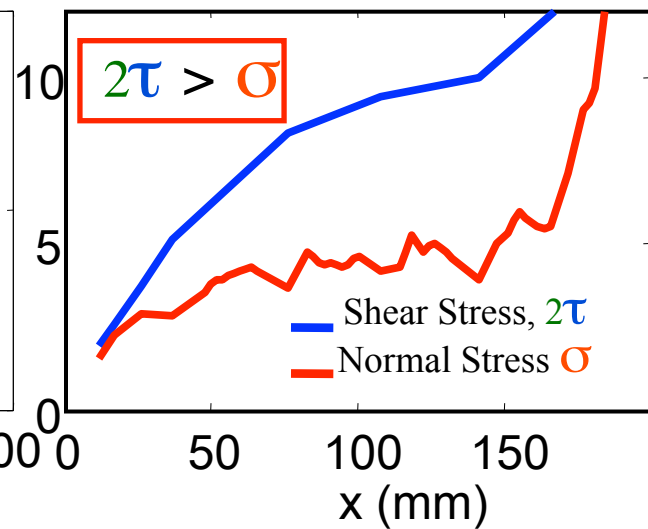
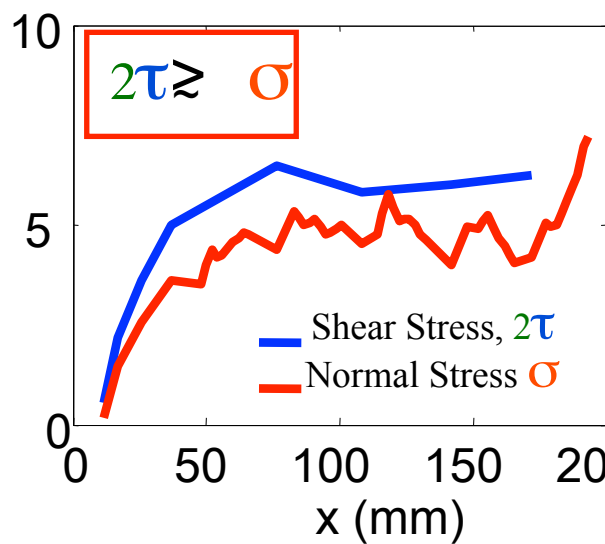
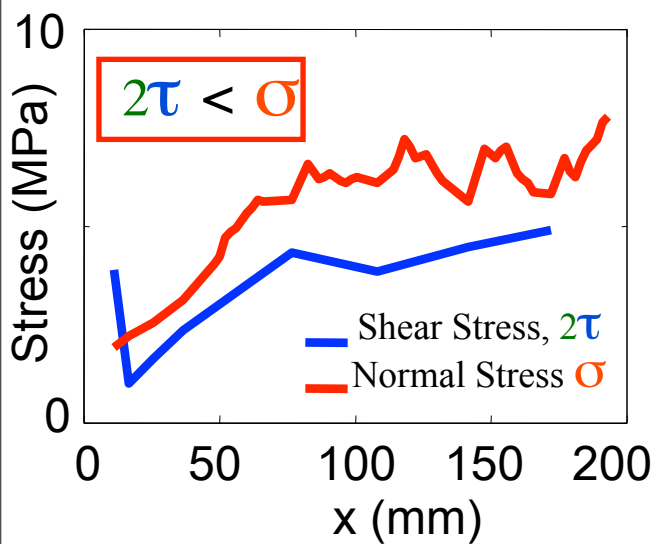
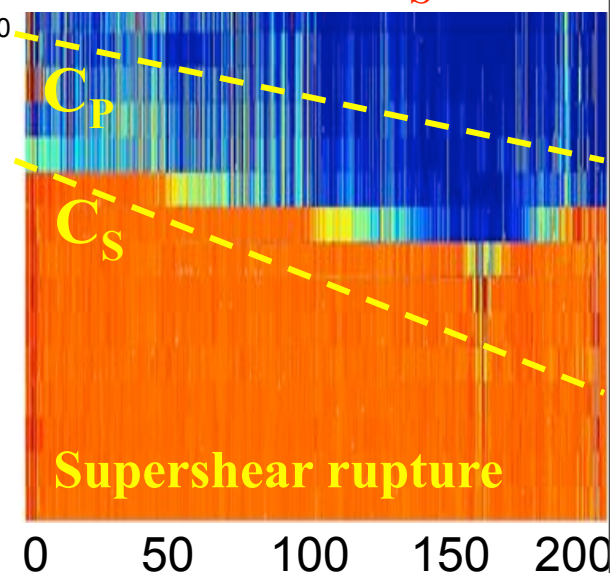
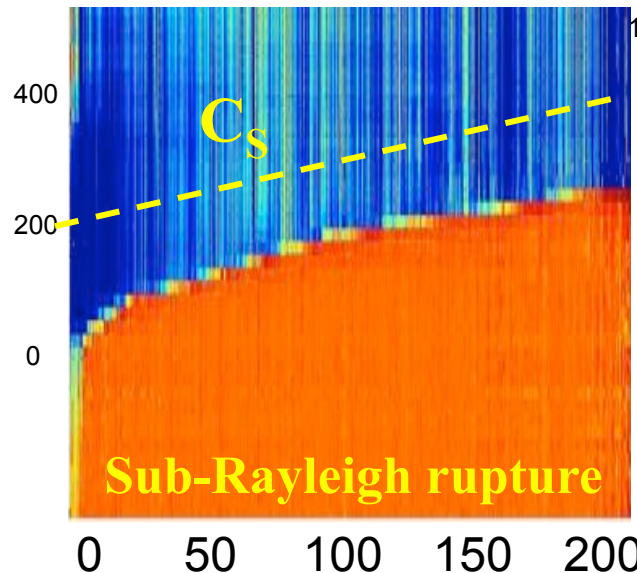
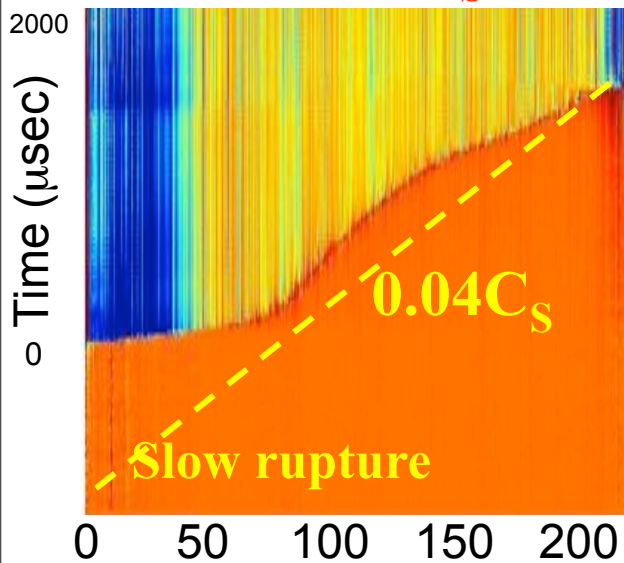


Does this hold for all types of rupture process?

$$v \ll C_s$$

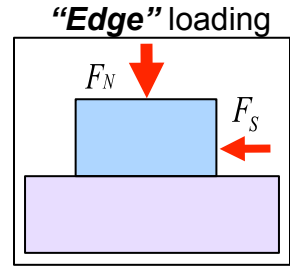
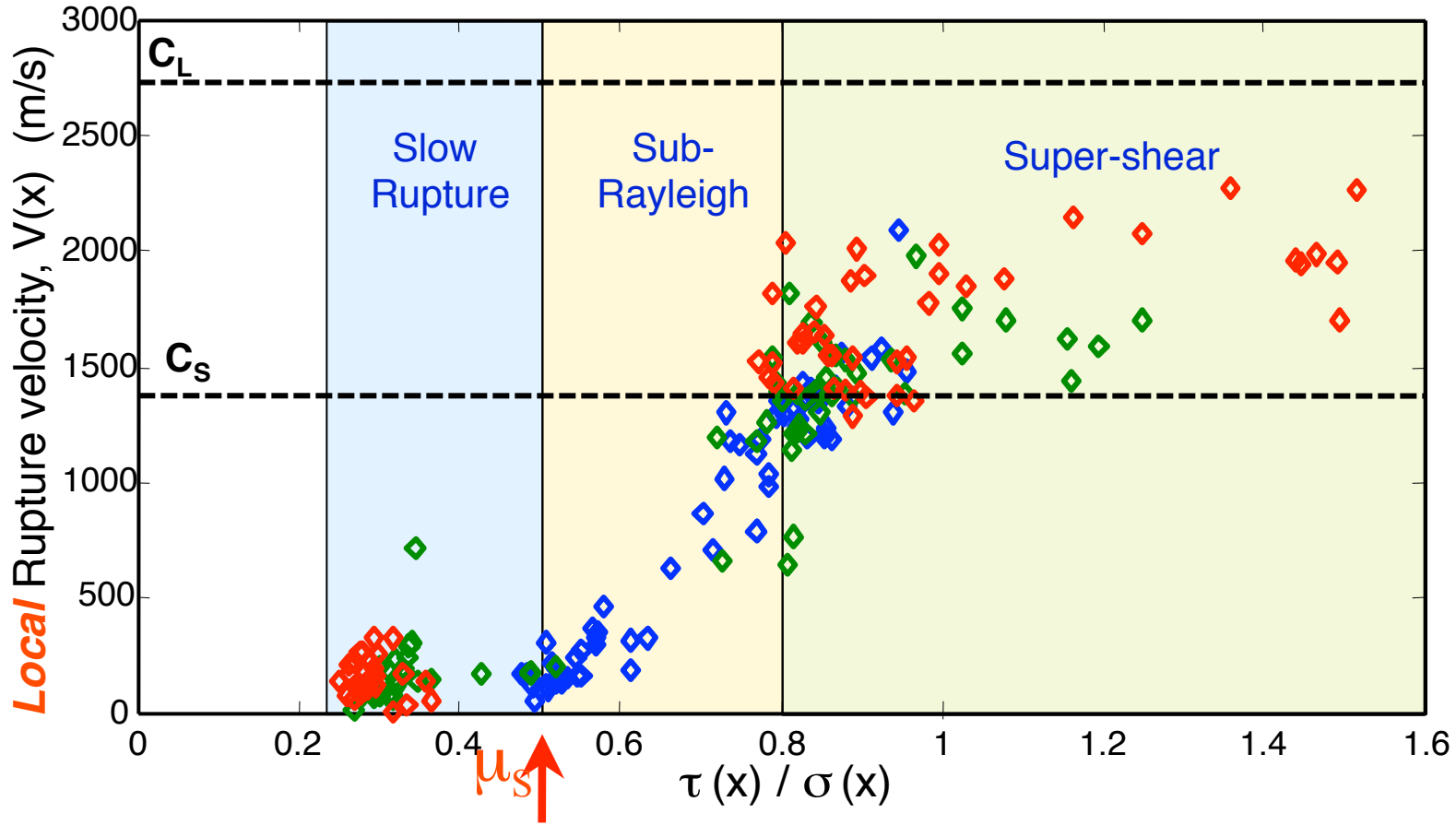
$$v < C_s$$

$$v > C_s$$

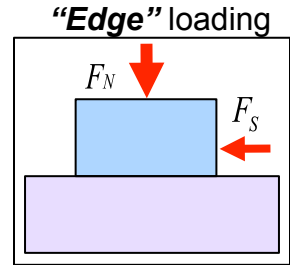
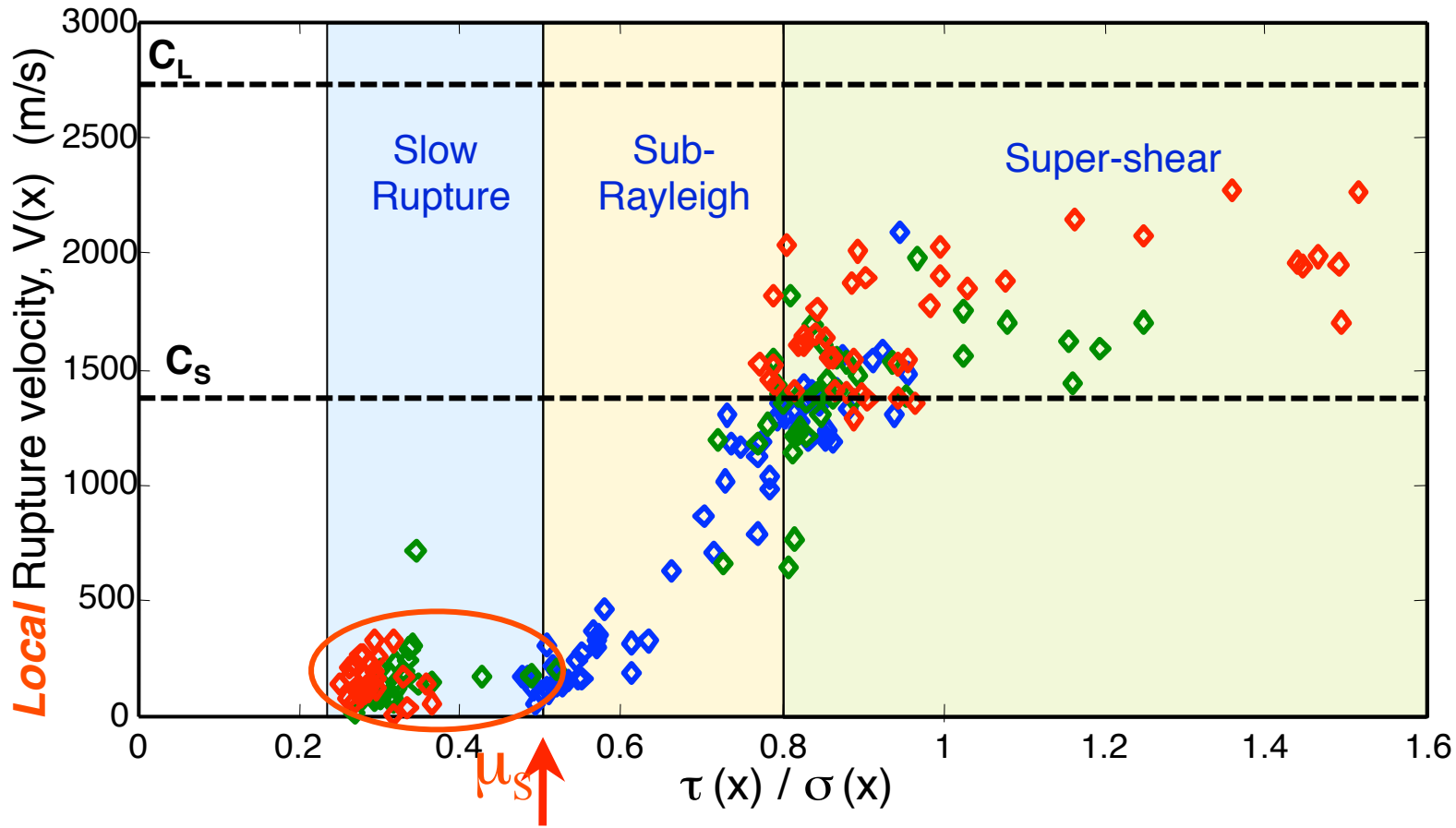


We can now understand the *local dynamics* in terms of $\tau(x)/\sigma(x)$!

> 100 different events/experiments under a broad range of local conditions:
(only regions *away* from pushing considered)



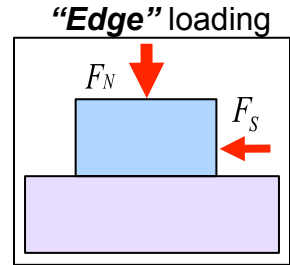
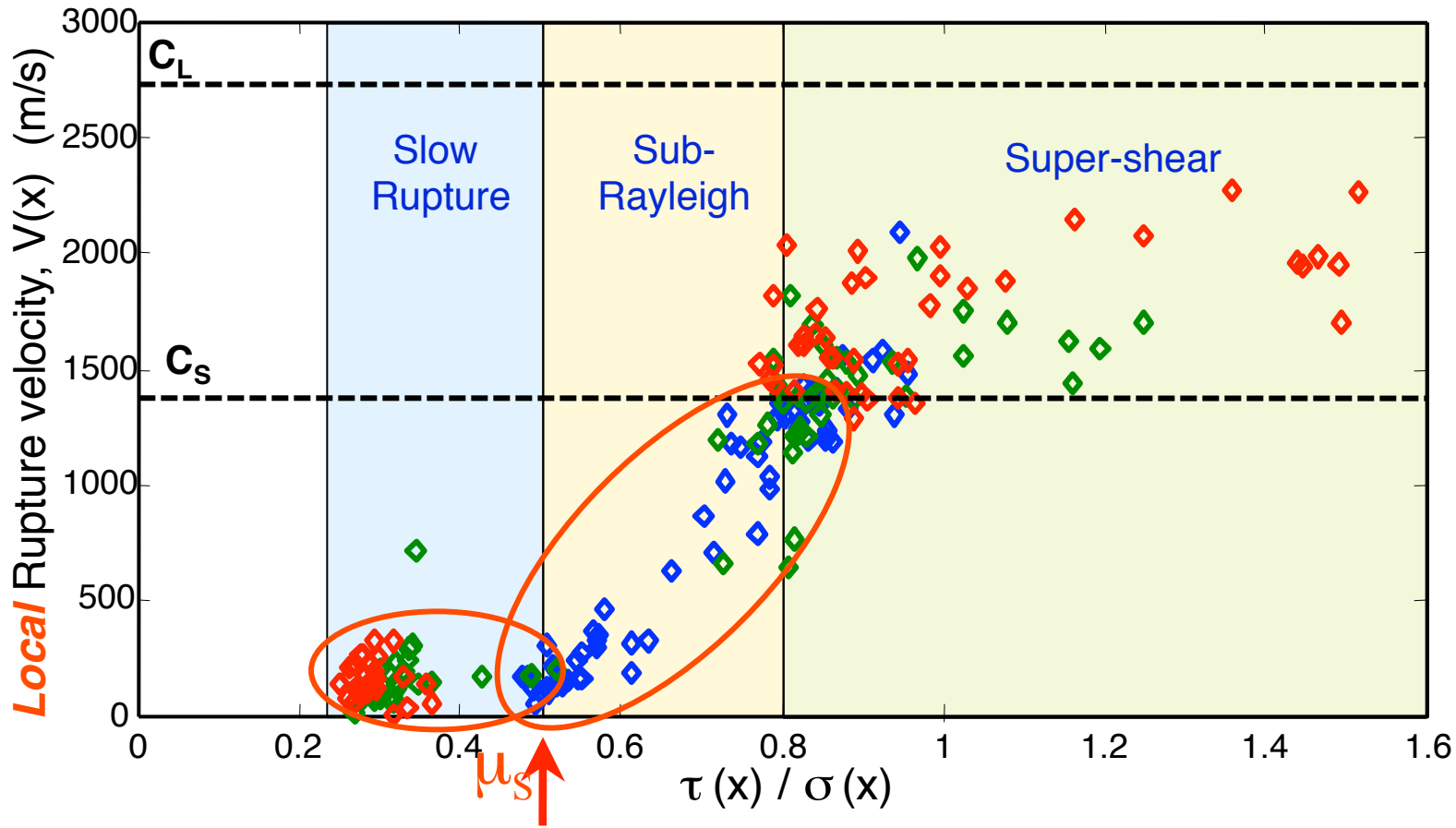
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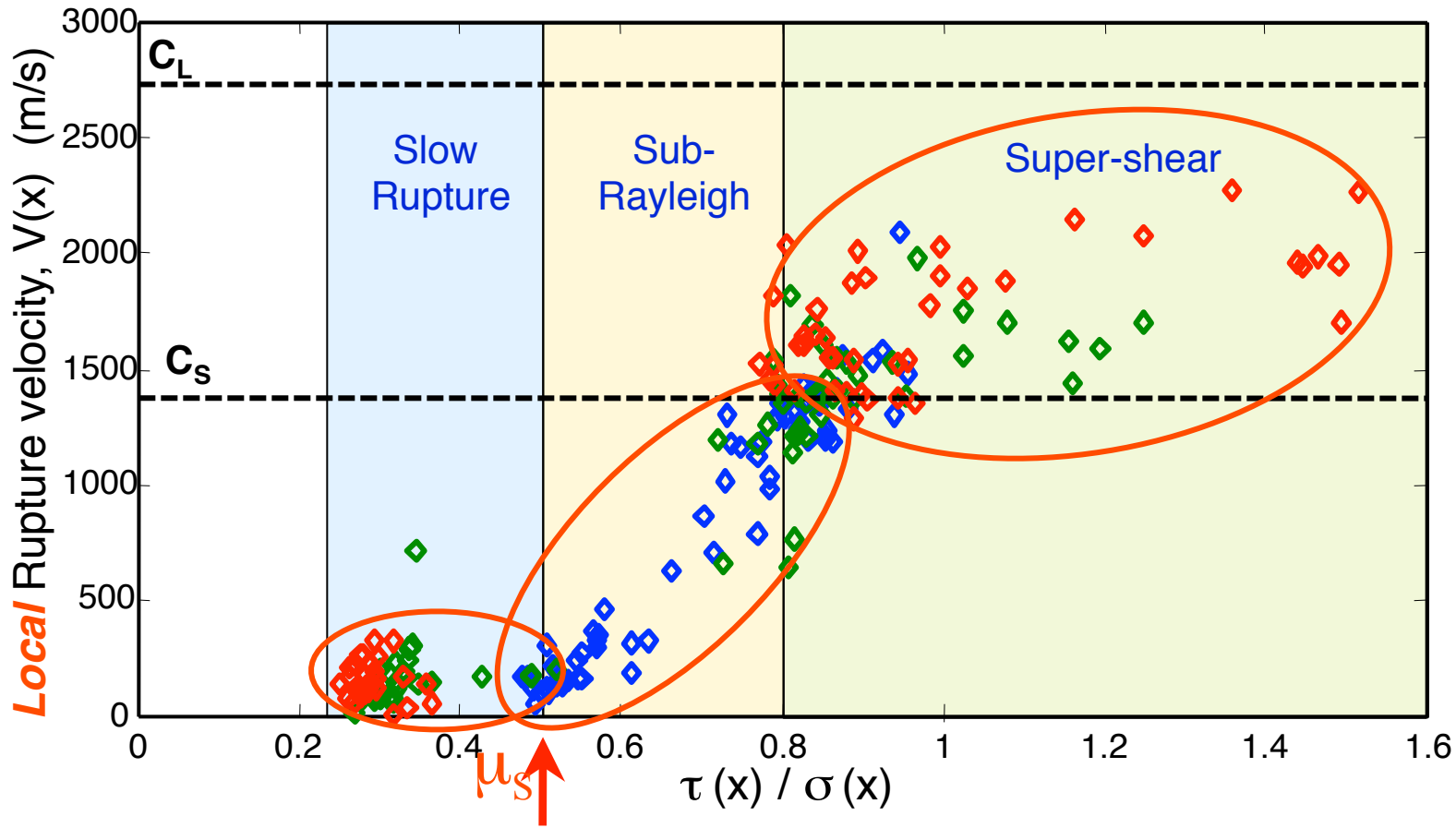
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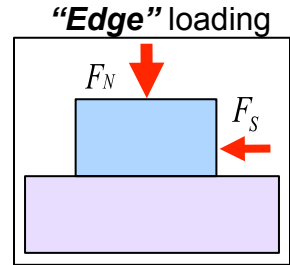
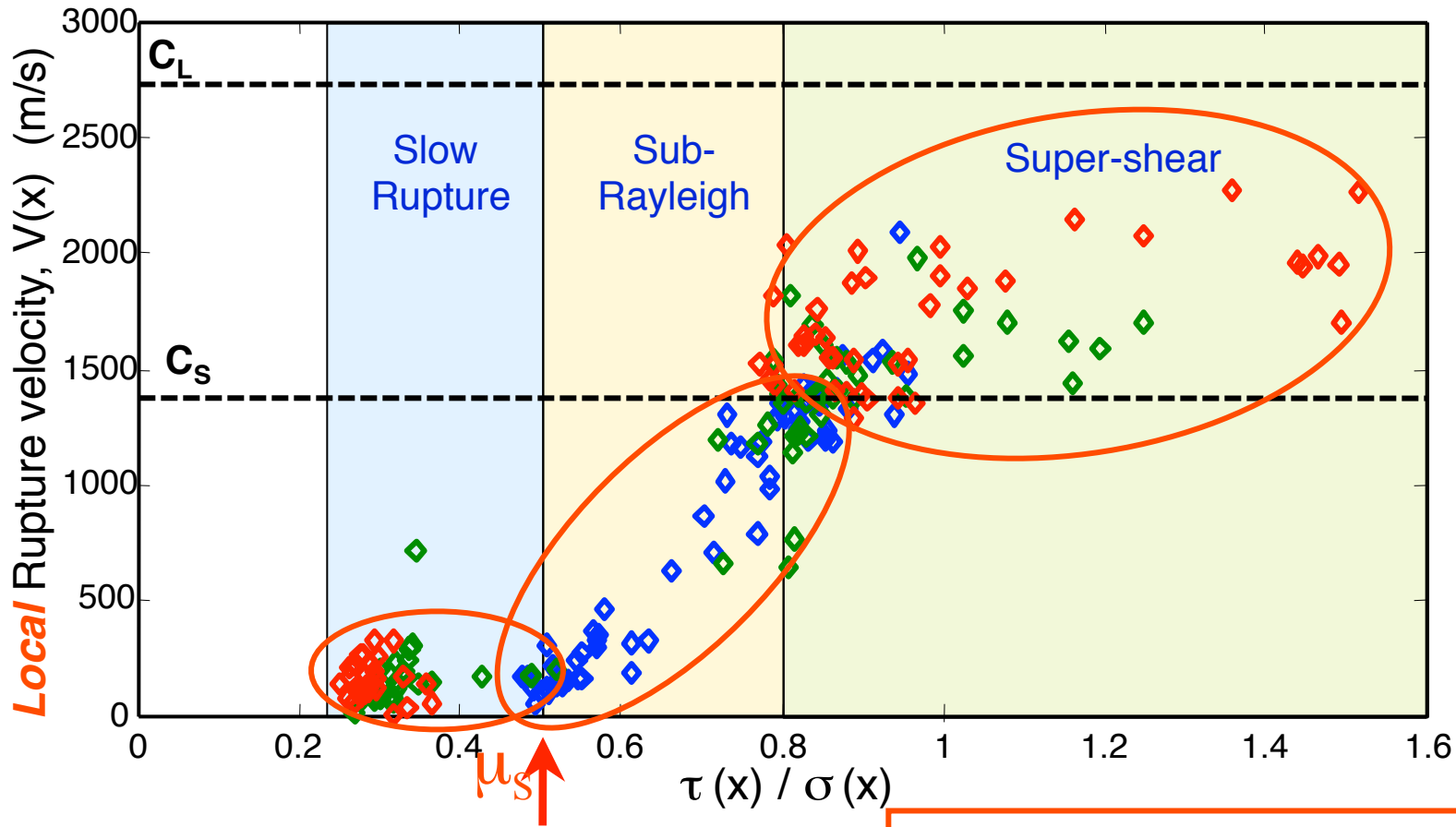
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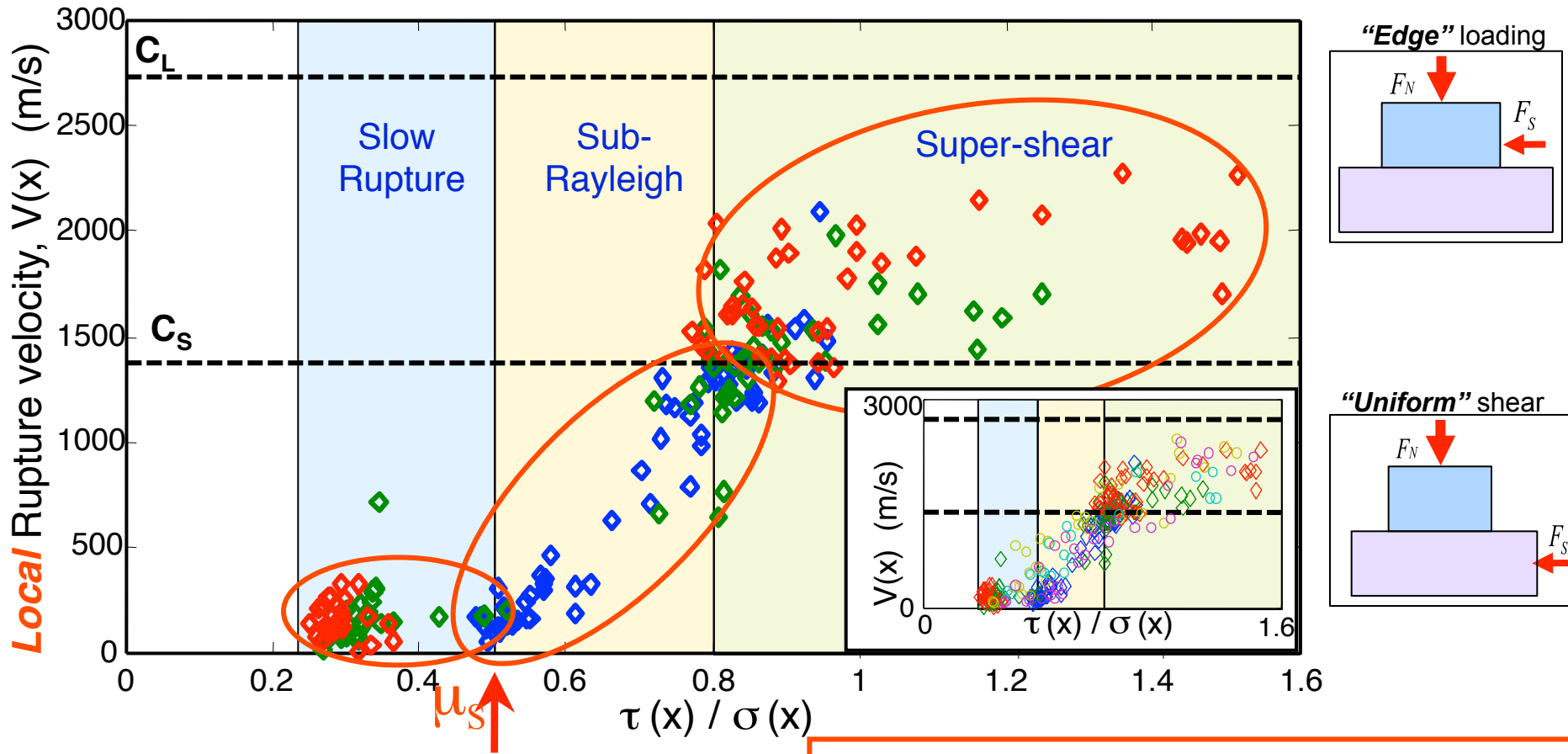


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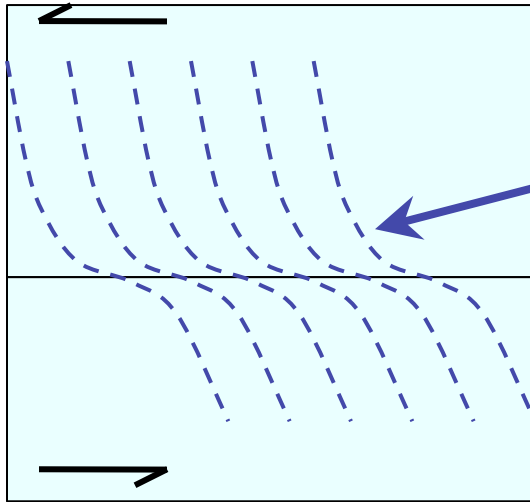
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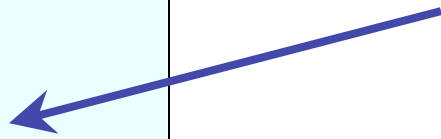
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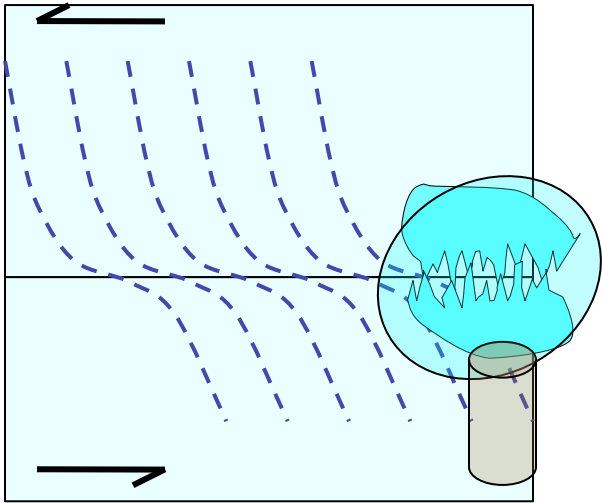


$\tau(x) \propto$ Imposed Shear

\Leftrightarrow *Stored elastic energy* in the material



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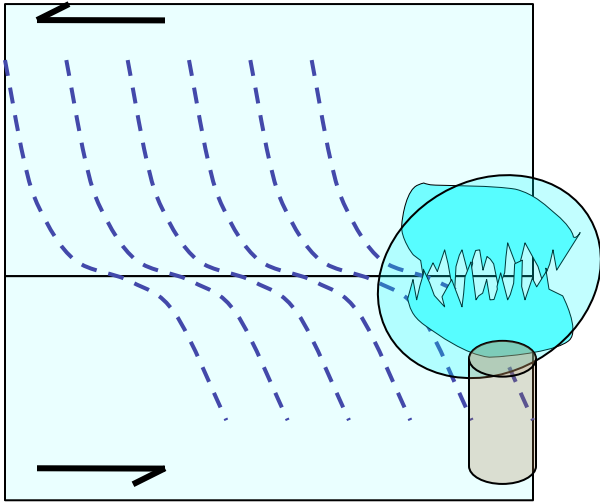


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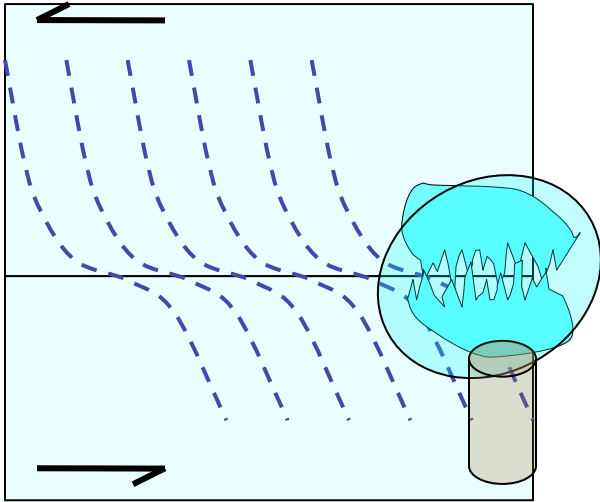
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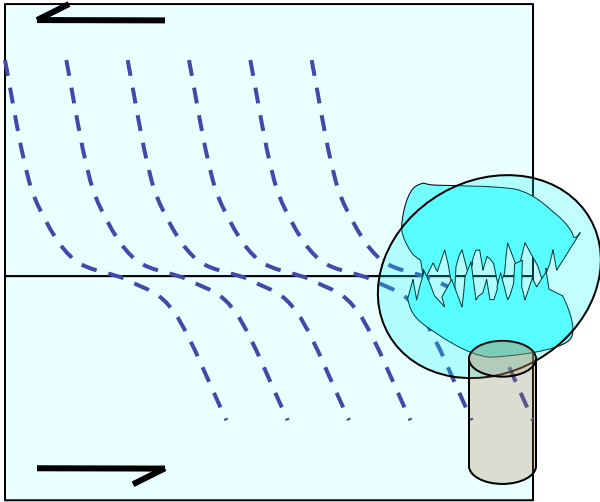
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+ A key difference with *pure* fracture:

Slip surface resistance \Leftrightarrow *frictional resistance* of the “free” crack faces

ASK ME ABOUT: O. Ben-David, S. M. Rubinstein and J. F., *Nature* **463**, 76 (2010)

Why are there different rupture modes (a hand-waving explanation)?

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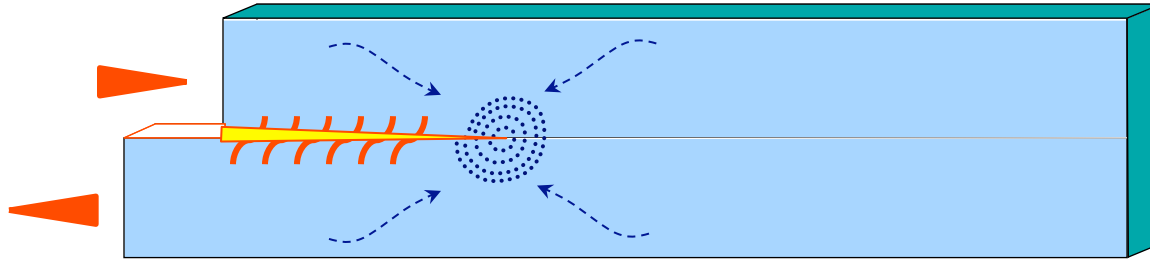
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Energy source

Dissipative source

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<u>Mode</u>	<u>Energy source</u>	<u>Dissipative source</u>
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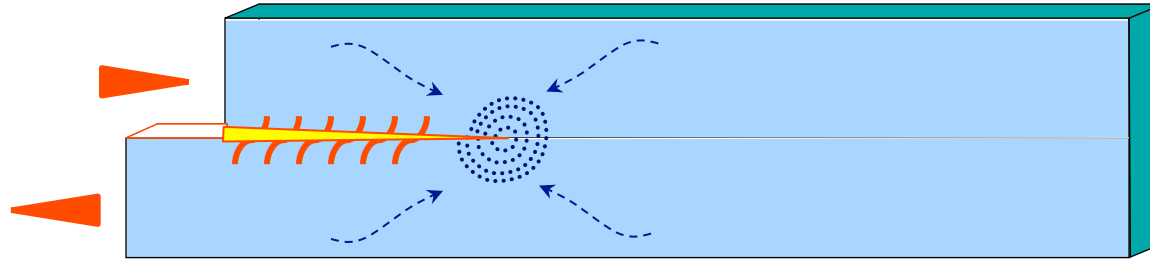
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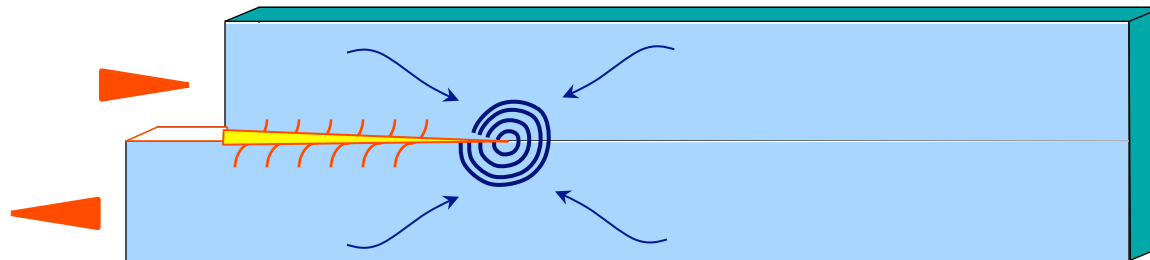
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Sub-Rayleigh

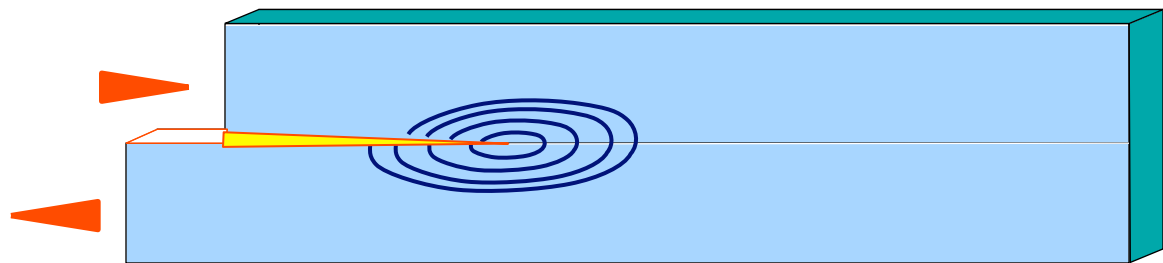
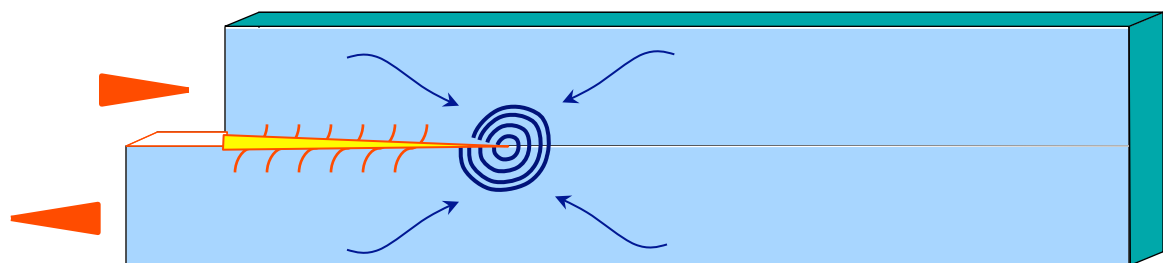
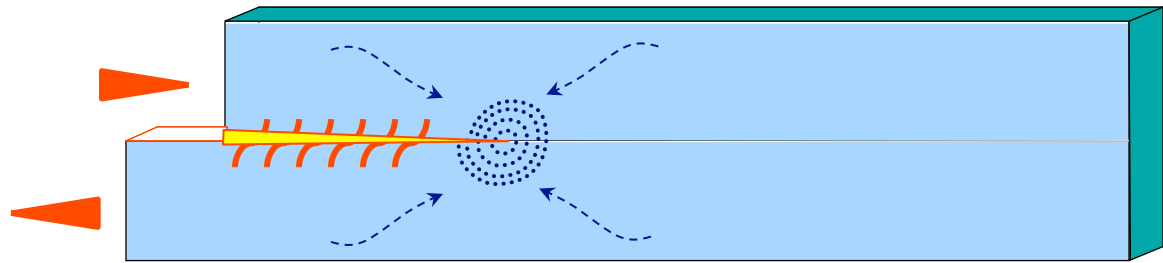
remote elastic fields
singular rupture tip dominant
 (V limited by V_R)



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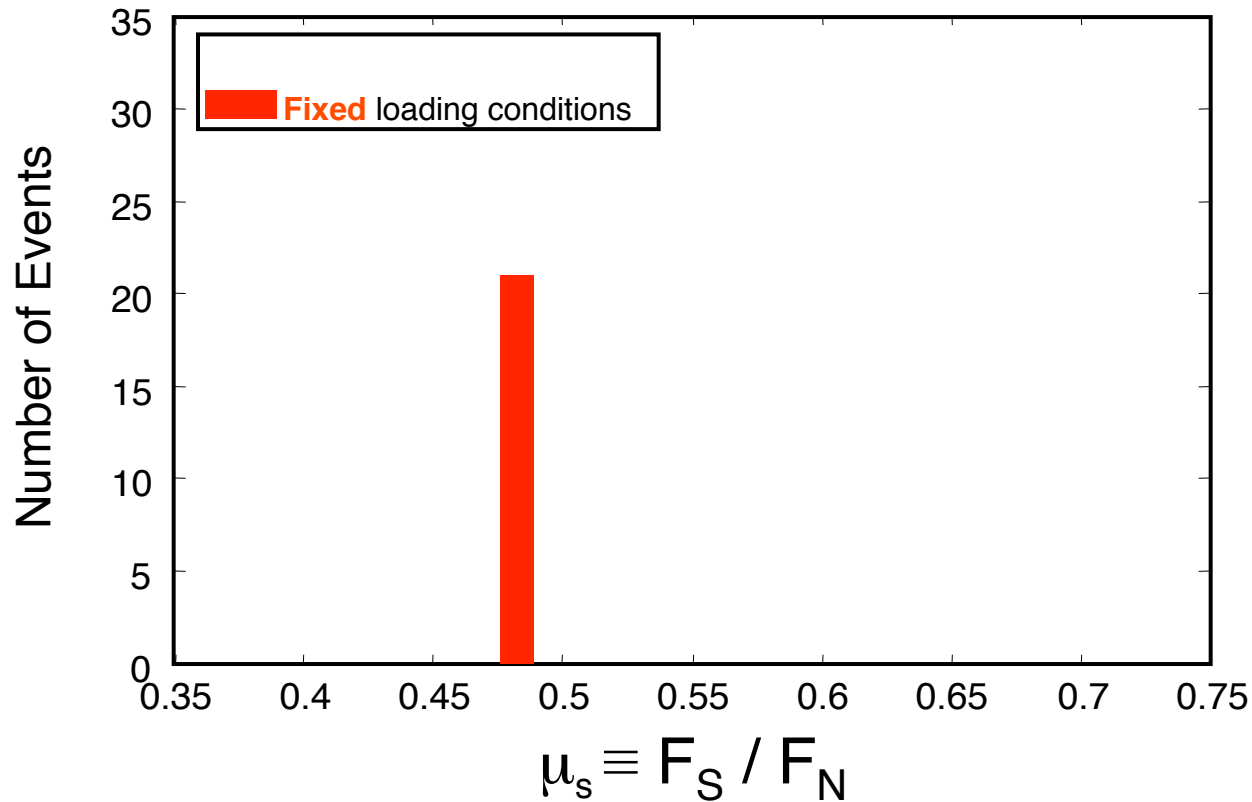
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Super-shear	LOCAL elastic fields (V unlimited by V_R ⇔ no energy transport from remote locations)	singular rupture tip dominant	$\frac{\tau(x)}{\sigma(x)} > 0.8$



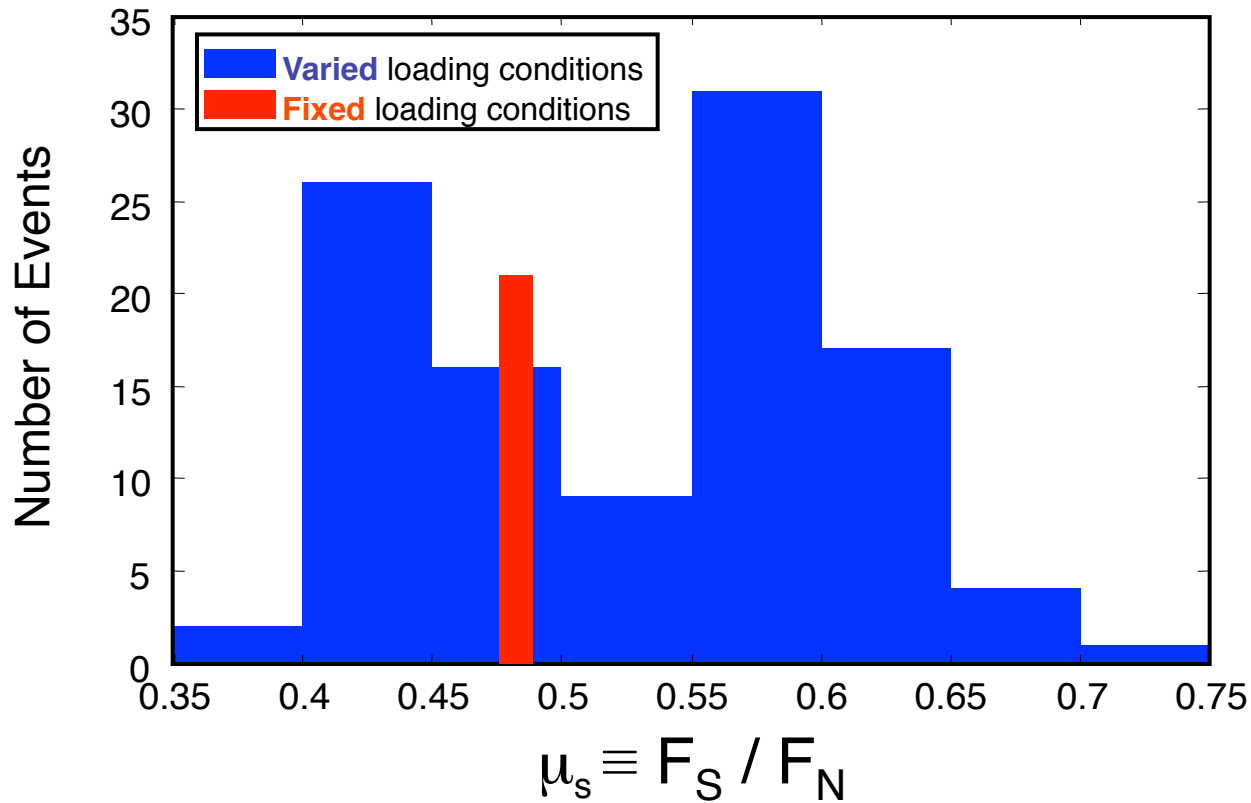
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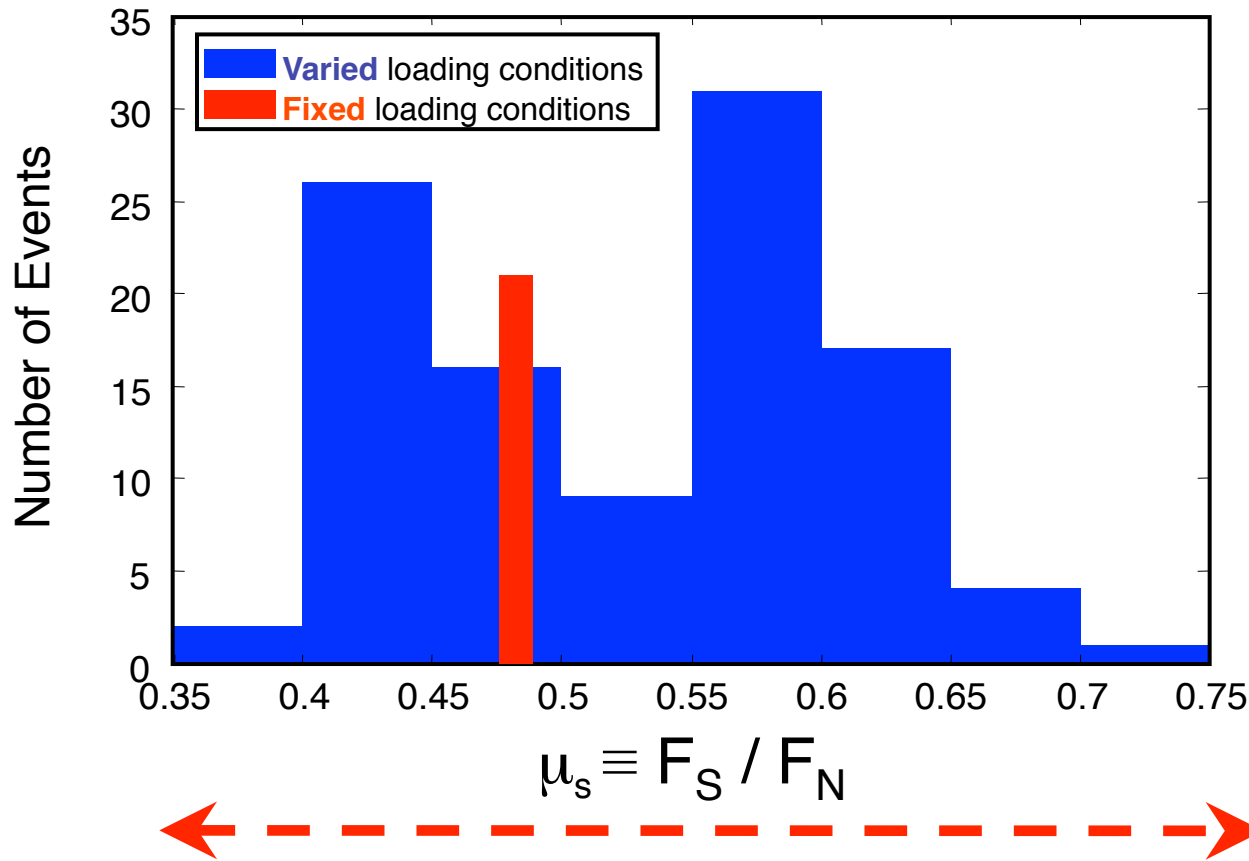
For *given loading conditions* μ_s is *entirely reproducible*

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For *different* loading conditions μ_s is *widely scattered*

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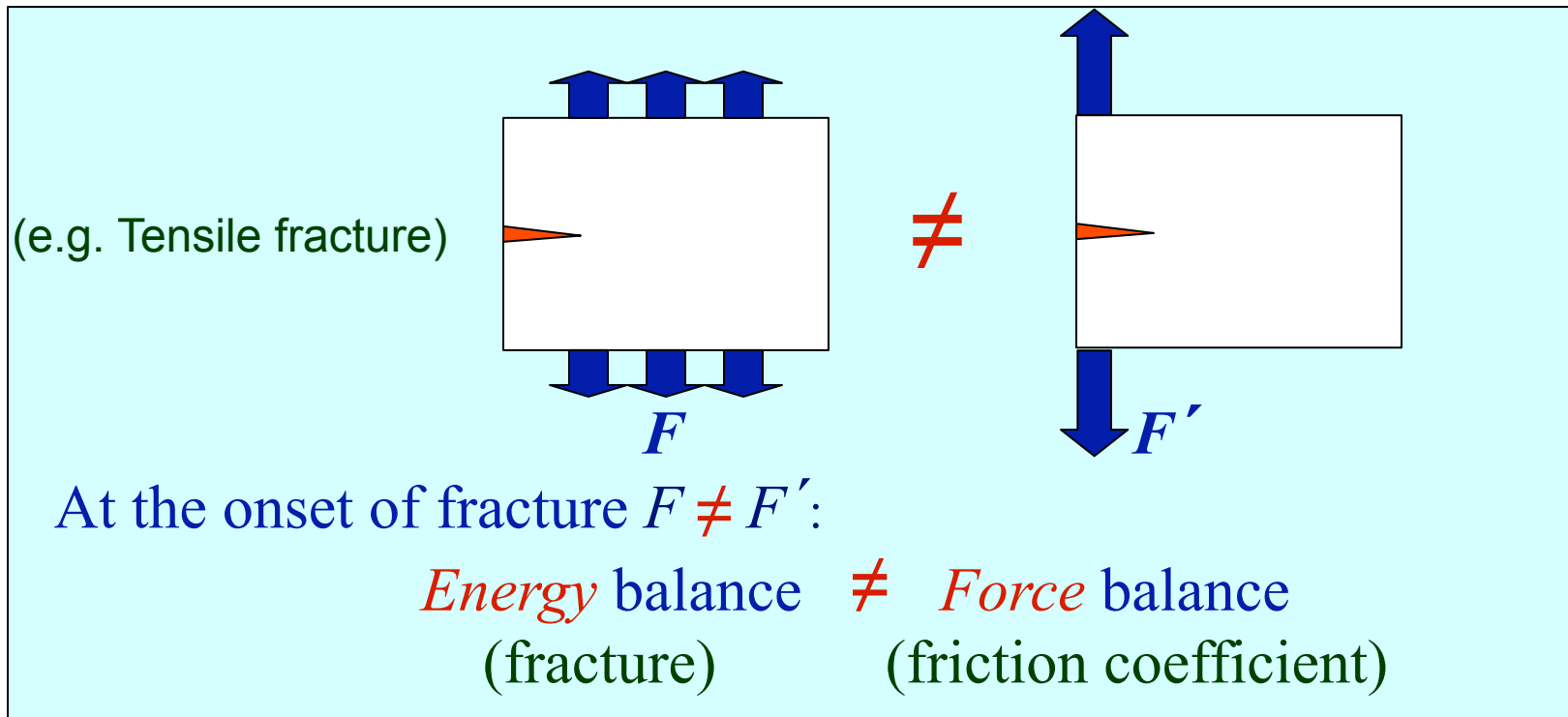
μ_s varies by over a *factor of 2* with the (pre-slip) stress distribution
→ μ_s is far from a *constant* (and in fact is ill-defined)!

μ_s is *not* a material constant

Does this make sense?

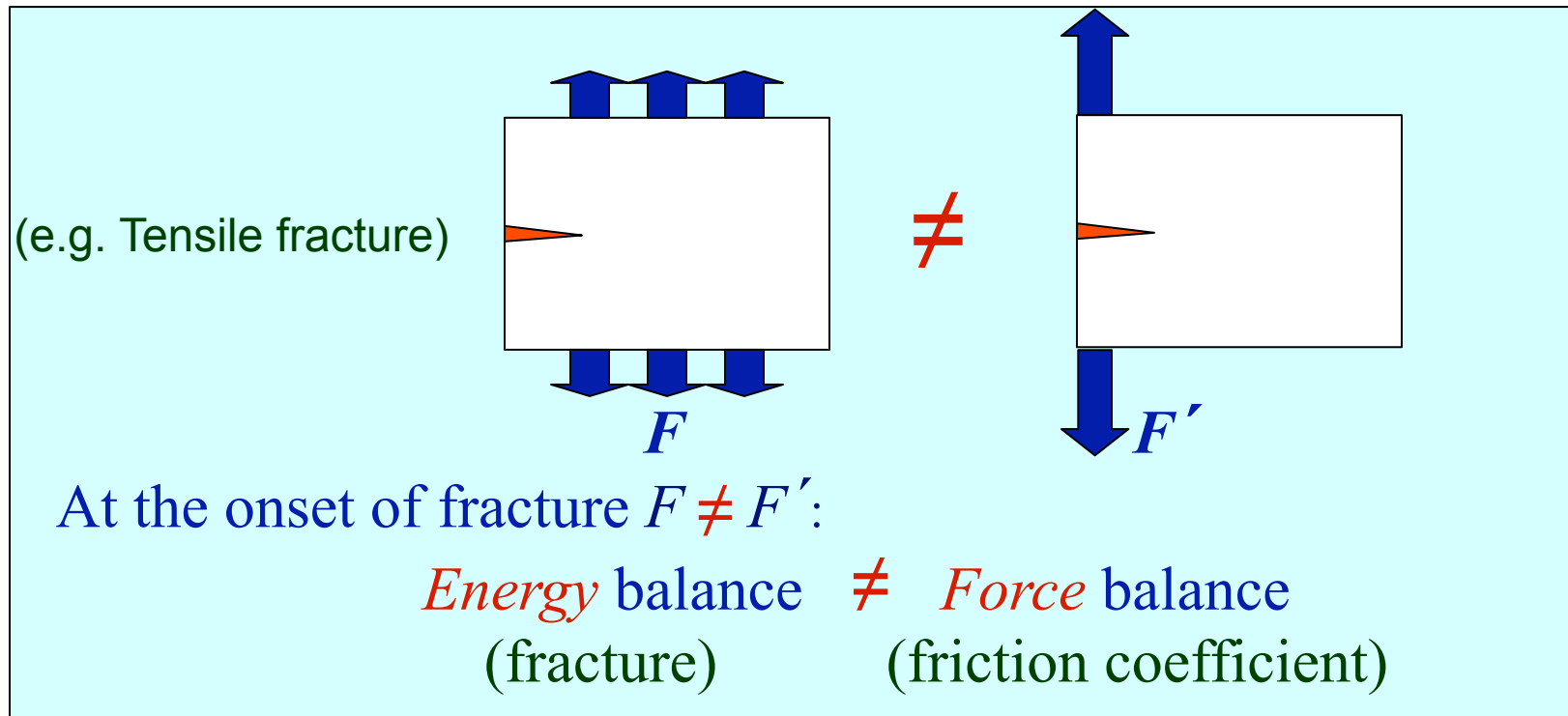
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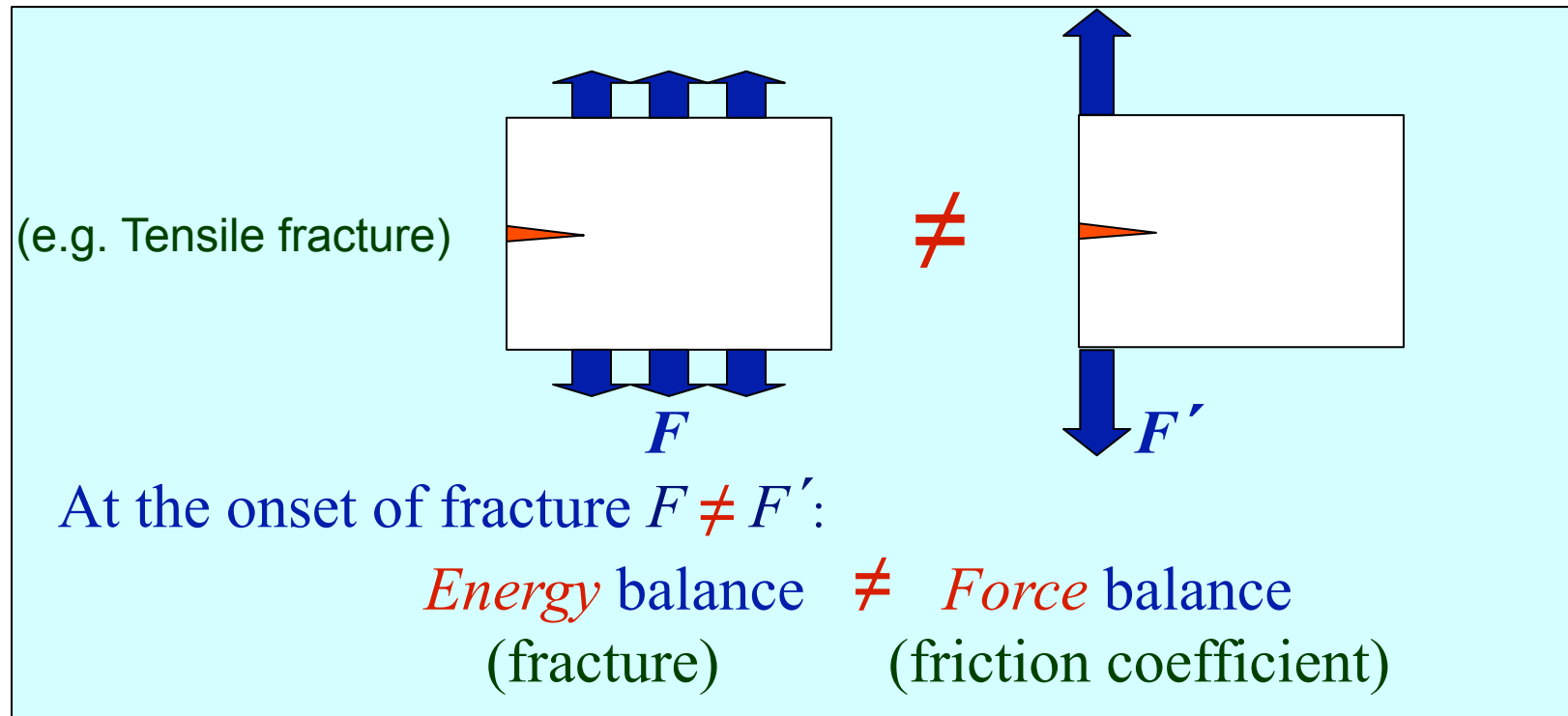
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→ μ_s is a characteristic *scale* of the overall *stored/fracture energy*

Summary: The effects of nonuniform stresses and interface strength

Inhomogeneous stresses *always exist* – even under “uniformly” applied loads

Inhomogeneities result from:

Interface geometry or material contrasts (e.g. asperities)

Non-uniform loading (internal stresses or externally applied)

Dynamically generated (by previous slip events)

Summary: The effects of nonuniform stresses and interface strength

Inhomogeneities control the amount of **energy stored *prior*** to slip initiation
*(Locally, a system can be well **beyond** the global threshold, μ_s , for static friction!)*

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- A spatially *local* “Friction Coefficient” is not a useful concept
- *Big Question*: What **is** the *proper* theoretical framework for predicting the **onset of frictional motion**???

Relevance to earthquakes: The dynamics of fault nucleation

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Sub-Rayleigh fronts \Leftrightarrow “Standard” earthquakes ($0.2V_R < V < 0.9V_R$)

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Slow earthquakes² = slow detachment fronts?

Characteristics of “slow” fronts:

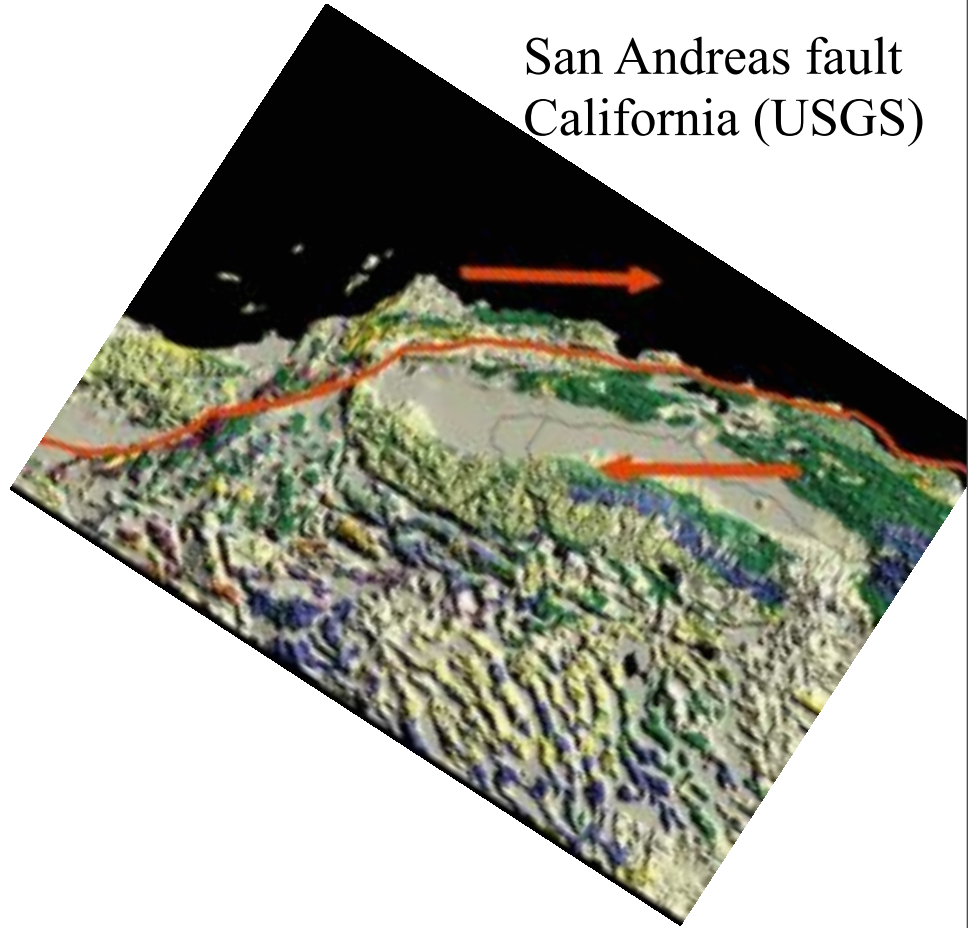
- May occur frequently
- Significant slip/strain release
- “Silent” – having a weak atypical acoustic (seismic) signature.

¹ Bouchon, M. et al. Geophys. Res. Lett. **28**, 2723–2726 (2001).

² Crescentini, L., Amoruso, A. & Scarpa, R. Science **286**, 2132–2134 (1999);
Linde, A. T. & Sacks, I. S. Earth and Planetary Science Letters **203**, 265–275 (2002).
Rogers, G. & Dragert, H. Science **300**, 1942–1943 (2003).

Earthquakes *are* Friction

San Andreas fault
California (USGS)



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Friction *is* mediated by **rupture fronts**

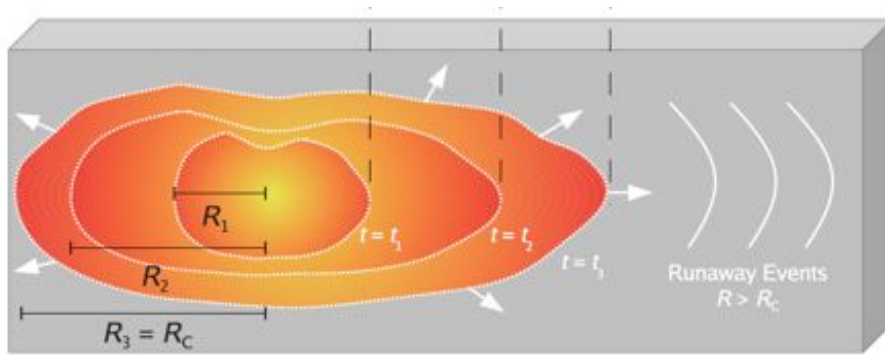
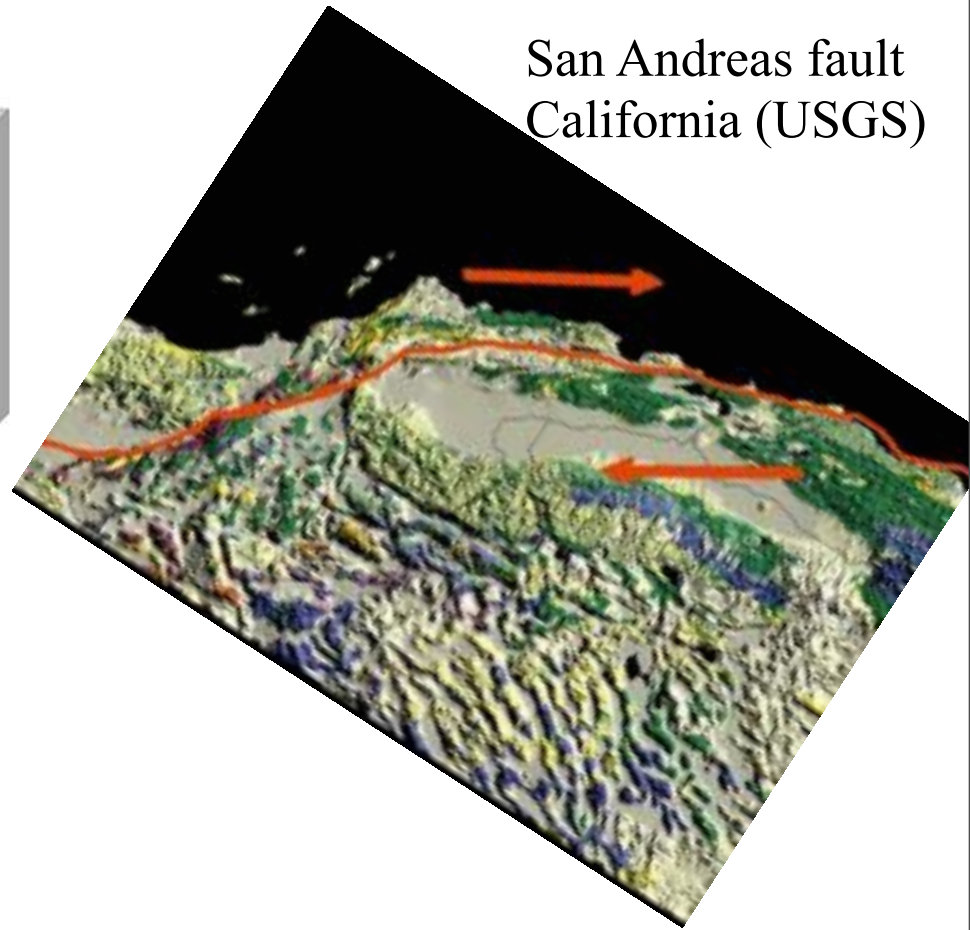


Figure 13. (top) Stress versus distance from the edge of (bottom) ruptures growing in elastic solid. Ruptures with a critical size R_c produce dynamically stress comparable to the static friction τ_s , leading to runaway events.

Y. Benzion (2008)



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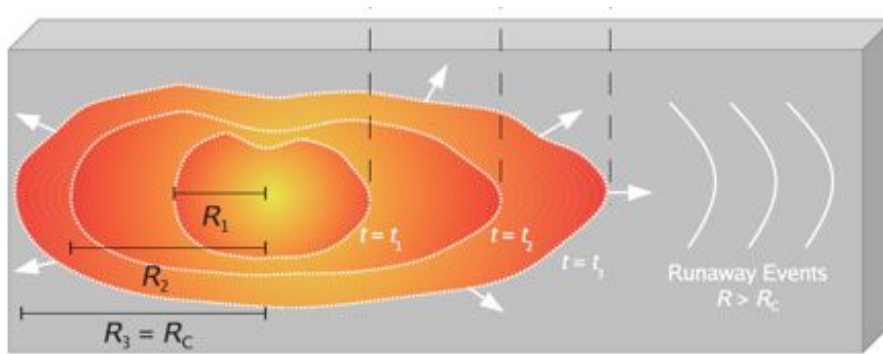


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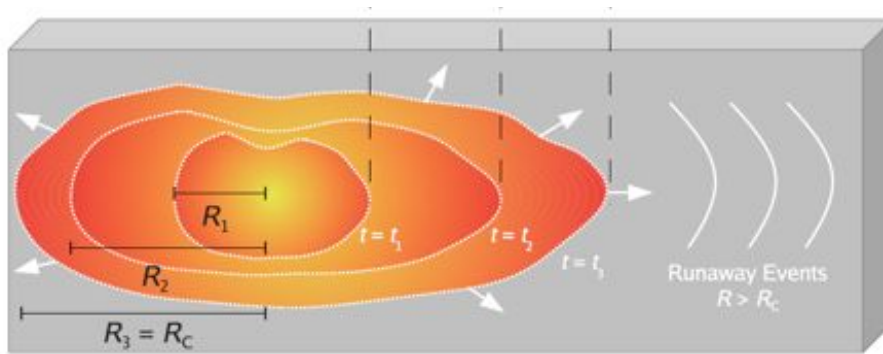


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- These measurements might provide us with the **tools...**

Thank you!